

# About $h_{JEi}$ Parameter Extraction...



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# Outline

- ▣ Preamble

- ▣  $h_{jEi}$  extraction method at low current densities

  - ▣ Model

  - ▣ Extraction method and issue

  - ▣ Results

- ▣  $h_{jEi}$  extraction method at medium current densities

  - ▣ Model

  - ▣ Extraction method and issue

  - ▣ Results

- ▣ Summary

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  - ❏ It is **Science** because HICUM is an advanced physics-based compact bipolar transistor model.
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**Why make simple when we can make complicated?!**



Image: <http://zesonic.free.fr/devises.htm>

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      - For non-expert users, HICUM looks like this →
- Why make simple when we can make complicated?!**
- A very good knowledge of the model (capabilities and limits) is mandatory for developing reliable (both accurate and physical parameters) extraction procedures.



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- ❏ Is HICUM/L2 parameter extraction *Science* or *Art*?... It is **Both...**
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    - How to obtain both precise and physical model parameters? (i) from measurements more or less accurate, (ii) from model more or less difficult to understand, with sometime not enough degrees of freedom for decoupling DC and AC characteristics.



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❏ Application to the extraction of  $h_{jEi}$



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# What is $h_{jEi}$ ?

## Definition and typical values

- $h_{jEi}$  is the BE depletion charge weighting factor in  $S_iG_e$  bipolar transistors (HBTs).

$S_i$  BJTs  $\rightarrow Q_{jEi}$

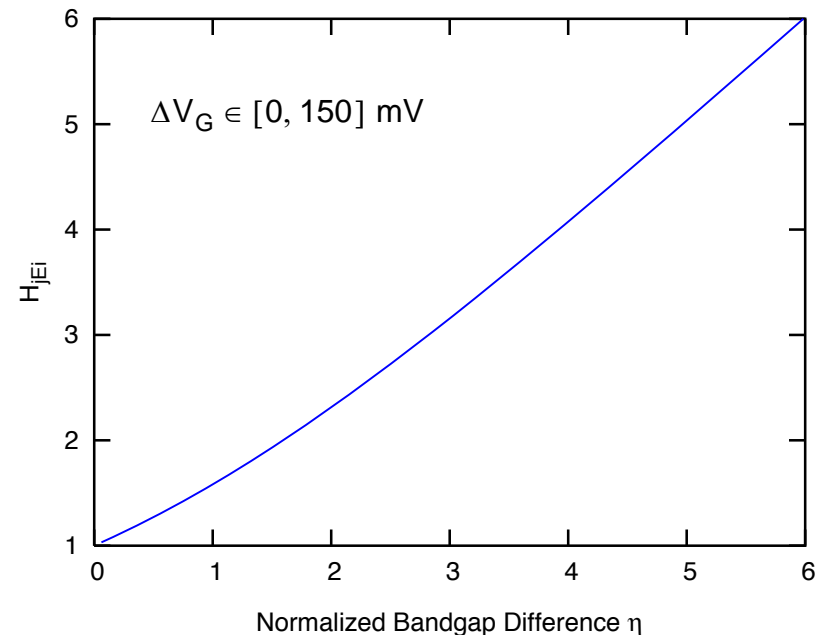
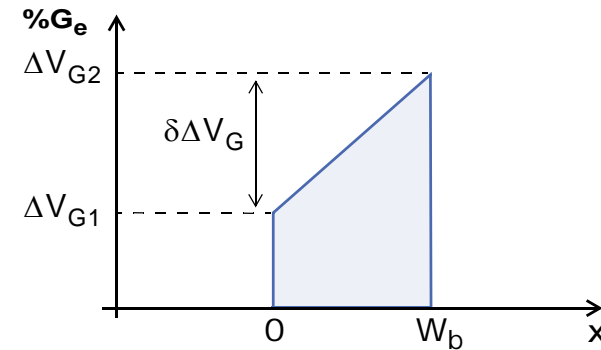
$S_iG_e$  HBTs  $\rightarrow h_{jEi} \cdot Q_{jEi}$

- $h_{jEi}$  can be calculated, at low current densities, from [1]

$$h_{jEi} \approx \frac{\eta \cdot e^\eta}{e^\eta - 1} \quad \text{with} \quad \eta = \frac{\delta\Delta V_G}{V_T} \quad \text{as the normalized band-}$$

gap difference between beginning and end of the base region.

- Dependence of  $h_{jEi}$  as function of  $\eta$  for a relevant range of application  $\rightarrow$
- For  $S_i$  BJTs or  $S_iG_e$  HBTs with a  $G_e$  box profile  $h_{jEi}$  is equal to 1.
- For  $S_iG_e$  HBTs with graded  $G_e$  profile  $h_{jEi}$  is normally greater than 1.



# $h_{jEi}$ Extraction and Issue: Part I Low Currents

## Expression of the collector current at low current densities

- HICUM/L2
- Low injection, voltage drop in series resistances negligible and  $V_{BC} = 0V$

$$I_C \approx I_{CF} \approx \frac{C_{10} \cdot e^{\frac{V_{BEi}}{V_T}}}{Q_{p0} + h_{jEi} \cdot Q_{jEi}} \quad \text{non-ideality factor } M_{CF} \text{ assumed equal to 1} \quad (1)$$

## Extraction strategy

- From (1) we can write

$$Q_{p0} + h_{jEi} \cdot Q_{jEi} = \frac{C_{10} \cdot e^{\frac{V_{BEi}}{V_T}}}{I_C} \quad \text{and finally} \quad Q_{jEi} = \frac{C_{10}}{h_{jEi}} \cdot \frac{e^{\frac{V_{BEi}}{V_T}}}{I_C} - \frac{Q_{p0}}{h_{jEi}} \quad (2)$$

- At low current densities, the internal BE depletion charge  $Q_{jEi}$  vs. the normalized collector current

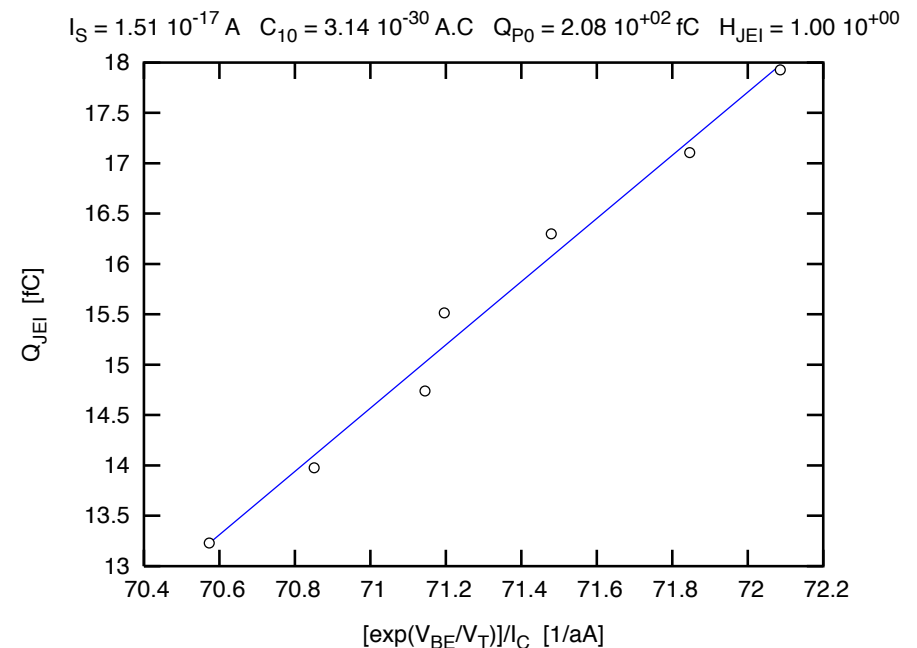
$$I_{CN} = I_C / e^{\frac{V_{BEi}}{V_T}} \text{ is linear, with a slope } s = \frac{C_{10}}{h_{jEi}} \text{ and an intercept } i = -\frac{Q_{p0}}{h_{jEi}}$$

## Extraction issues

- From (2), a linear regression allows to directly obtain only the ratios  $C_{10*}$  and  $Q_{P0*}$

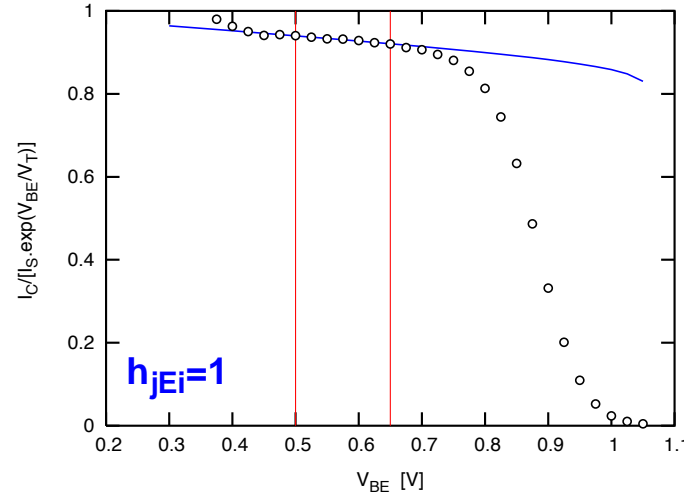
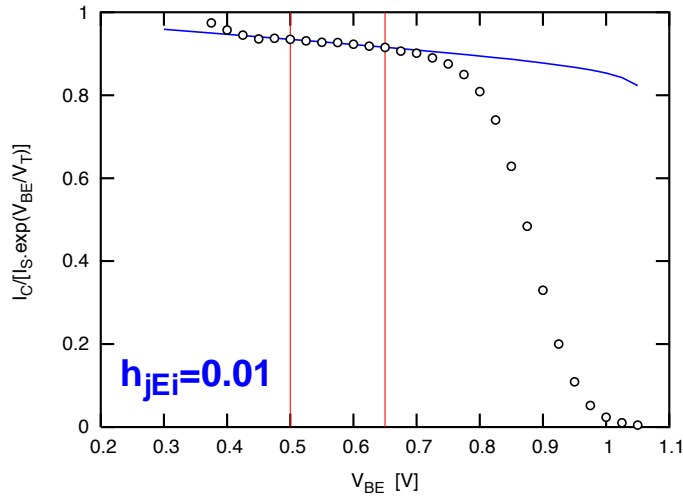
$$C_{10*} = s = \frac{C_{10}}{h_{jEi}} \quad \text{and} \quad Q_{P0*} = -i = \frac{Q_{p0}}{h_{jEi}}$$

- With this methodology, because of the HICUM hole charge formulation, it is impossible to distinguish  $C_{10}$  from  $h_{jEi}$ , and  $Q_{P0}$  from  $h_{jEi}$ . There are as many  $C_{10}$  and  $Q_{P0}$  parameters there are values of  $h_{jEi}$  which give exactly the same accuracy on  $I_C$  at low and medium current densities.
- In addition to this problem, the internal BE depletion charge must be accurately known (from the intrinsic BE junction capacitance).
  - $C_{10}$  and  $Q_{P0}$  are directly correlated to the values of  $C_{JEI}$ ,  $V_{DEI}$  and  $Z_{EI}$ .
  - Therefore, reliable (physics-based and accurate) parameter extraction is difficult on single-geometry transistor approach.
- The parameters are also strongly dependent on the temperature (but not specific to the HICUM model). A solution has been proposed by Z. Huszka [2] in order to obtain the temperature value directly from the measurements. To be tested.

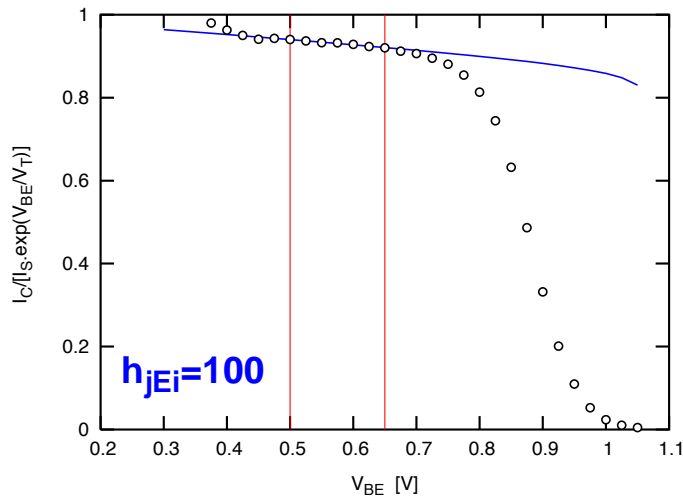


# Effect of $h_{jEi}$ on $C_{10}$ and $Q_{P0}$ Parameter Extraction

Several trials:  $h_{jEi} = 1, 0.01, 100$



- Normalized collector current at  $V_{BC} = 0V$  and  $T = 27^\circ C$ .
- High current parameters and series resistances not yet extracted.



Parameter	$h_{jEi} = 1$	$h_{jEi} = 0.01$	$h_{jEi} = 100$
$C_{10} = C_{10} \cdot h_{jEi}$ (A.C)	$2.65 \cdot 10^{-30}$	$2.73 \cdot 10^{-32}$	$2.64 \cdot 10^{-28}$
$Q_{P0} = Q_{P0} \cdot h_{jEi}$ (fC)	$1.76 \cdot 10^2$	$1.82 \cdot 10^0$	$1.76 \cdot 10^4$
$I_S = C_{10} / Q_{P0}$ (A)	$1.50 \cdot 10^{-17}$	$1.50 \cdot 10^{-17}$	$1.50 \cdot 10^{-17}$

- Same fit but with different values of  $C_{10}$ ,  $Q_{P0}$  correlated to  $h_{jEi}$ .
- In all cases, same  $I_S$ .

# Conclusion Part I: Low Current Study

- ❏ It is not possible to distinguish  $C_{10}$ ,  $Q_{P0}$ ,  $h_{jEi}$  (one of these three parameters must be known in order to determine the two others) from extraction on DC characteristics at low currents densities
  - ❏ Perhaps other extraction methods could be used?
  - ❏ All suggestions and proposals are welcome...
- ❏ Moreover, (i) the temperature must be accurately known (as many sets of model parameter than input temperature), (ii) the non-ideality factor of the forward transfer current  $M_{CF}$  must be set to 1, and (iii) the internal BE depletion charge has to be known as accurate as possible.
- ❏ A suggestion is to determine  $Q_{P0}$  from *tetrode* measurements [3], and than to optimize  $C_{10}$  and  $h_{jEi}$  from the normalized collector current.



# Determination of $\overline{Q_{P0}}$ from Tetrode Measurements

- Tetrode measurements performed at different  $V_{BE}$  allow to determine  $\overline{Q_{P0}}$  from the bias dependence of the internal base sheet resistance  $R_{SBI}$

$$R_{SBI} \approx \frac{R_{SBI0}}{\overline{Q_{P0}} + Q_{jEi} + Q_{jCi}} \quad (3)$$

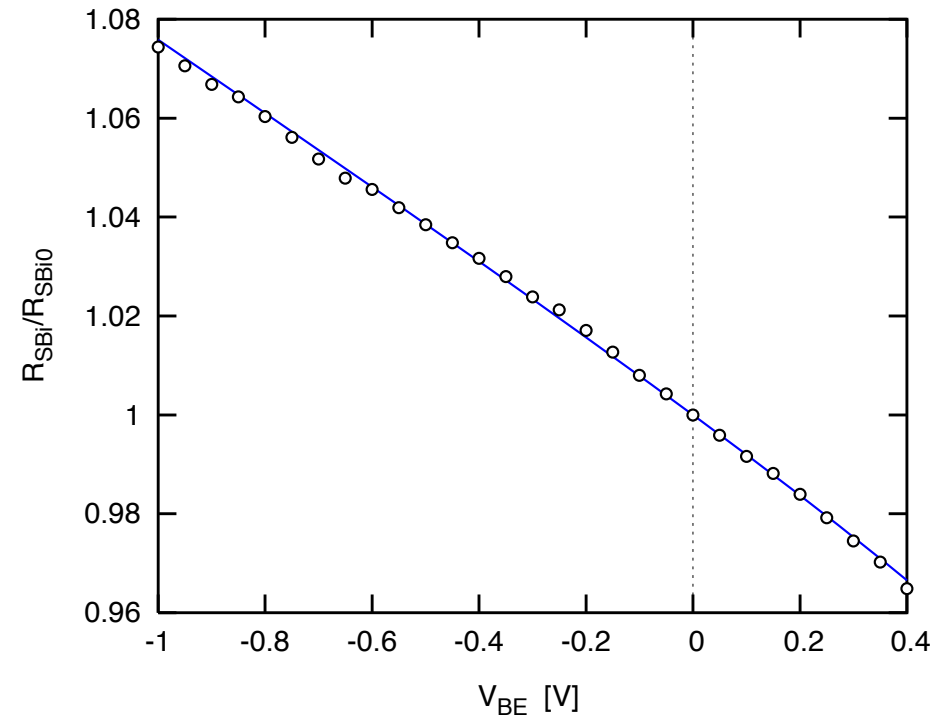
- Rearranging this equation leads

$$\frac{1}{R_{SBI}} \approx \frac{\overline{Q_{P0}}}{R_{SBI0}} + \frac{Q_{jEi} + Q_{jCi}}{R_{SBI0}} \quad (4)$$

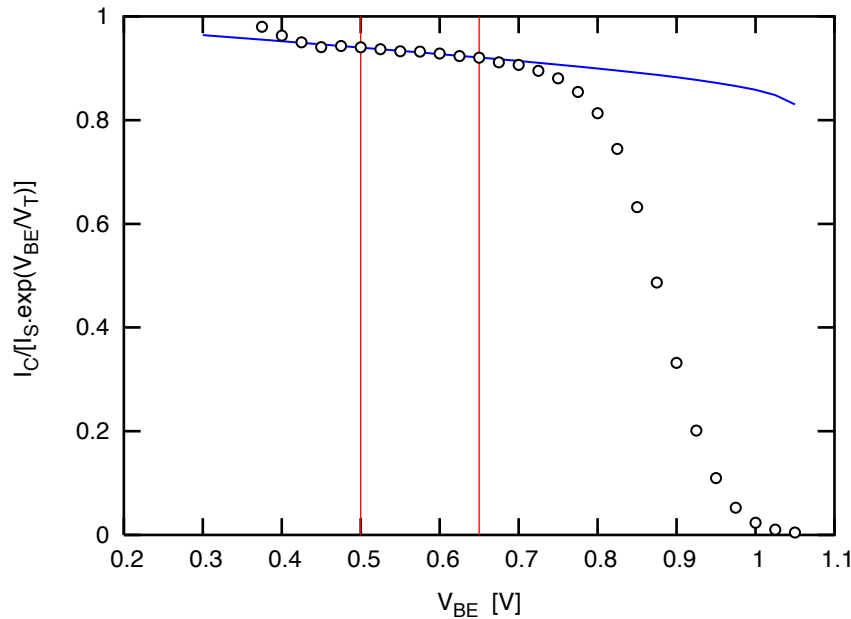
A linear regression of  $1/R_{SBI}$  vs.  $Q_{jEi} + Q_{jCi}$  gives  $\overline{Q_{P0}}$  and  $R_{SBI0}$

$$\begin{cases} \text{slope} = s = \frac{1}{R_{SBI0}} & \Rightarrow R_{SBI0} = \frac{1}{s} \\ \text{inter} = i = \frac{\overline{Q_{P0}}}{R_{SBI0}} & \Rightarrow \overline{Q_{P0}} = \frac{i}{s} \end{cases}$$

$$R_{SBI} = 1430 \, \Omega/\text{sq.} \quad \overline{Q_{P0}} = 75 \, \text{fC}/\mu\text{m}^2$$



## 🔧 $C_{10}$ and $h_{JEi}$ extraction knowing $Q_{P0}$



- $Q_{P0} = \overline{Q_{P0}} \cdot A_{\text{Eff}} = 237 \text{ fC}$

Parameter	$h_{JEi} = 1.35$	$h_{JEi} = 1$	$h_{JEi} = 0.01$	$h_{JEi} = 100$
$C_{10} = C_{10} \cdot h_{JEi}$ (A.C)	$3.57 \cdot 10^{-30}$	$2.65 \cdot 10^{-30}$	$2.73 \cdot 10^{-32}$	$2.64 \cdot 10^{-28}$
$Q_{P0} = Q_{P0} \cdot h_{JEi}$ (fC)	$2.37 \cdot 10^2$	$1.76 \cdot 10^2$	$1.82 \cdot 10^0$	$1.76 \cdot 10^4$
$I_S = C_{10}/Q_{P0}$ (A)	$1.50 \cdot 10^{-17}$	$1.50 \cdot 10^{-17}$	$1.50 \cdot 10^{-17}$	$1.50 \cdot 10^{-17}$

- Same fit, same  $I_S$ , but with different values of  $C_{10}$ ,  $Q_{P0}$  correlated to  $h_{JEi}$

# $h_{jEi}$ Extraction and Issue: Part II Medium Currents

## Expression of the collector current at medium current densities

- Medium current densities means *before the  $f_T$  peak and at the beginning of the DC current gain fall-off.*
- $V_{BC} = 0V$  and non-ideality factor  $M_{CF}$  assumed equal to 1

$$I_C \approx I_{TF} \approx \frac{C_{10} \cdot e^{\frac{V_{BEi}}{V_T}}}{Q_{pT}} \quad \text{with } Q_{pT}, \text{ the transfer hole charge at } V_{BC} = 0V \text{ given by} \quad (5)$$

$$Q_{pT} = \underbrace{Q_{p0} + h_{jEi} \cdot Q_{jEi}}_{Q_{pLow}} + Q_F = Q_{pLow} + Q_F \quad (6)$$

- At medium current densities the forward diffusion charge  $Q_F$  can be written

$$Q_F \approx Q_{F0} = \int_0^{I_{TF}} T_F di = T_{F0} \cdot I_{TF} \quad (7)$$

$T_{F0}$  is the forward transit time at low and medium currents and  $V_{BC}=0V$ , assumed to be constant in this range of operation.

From (5) we can finally write

$$Q_{F0} = T_{F0} \cdot I_{TF} = T_{F0} \cdot \frac{C_{10} \cdot e^{\frac{V_{BEi}}{V_T}}}{Q_{pT}} \quad (8)$$

From (6) and (8) leads

$$Q_{pT} = Q_{pLow} + Q_{F0} = Q_{pLow} + T_{F0} \cdot \frac{C_{10} \cdot e^{\frac{V_{BEi}}{V_T}}}{Q_{pT}} \Leftrightarrow Q_{pT}^2 + Q_{pLow} \cdot Q_{pT} - T_{F0} \cdot C_{10} \cdot e^{\frac{V_{BEi}}{V_T}} = 0 \quad (9)$$

Solving this quadratic equation gives (negative solution ignored because  $Q_{pT}$  is greater than 0)

$$Q_{pT} = \frac{Q_{pLow}}{2} + \sqrt{\left(\frac{Q_{pLow}}{2}\right)^2 + T_{F0} \cdot C_{10} \cdot e^{\frac{V_{BEi}}{V_T}}} = \frac{Q_{p0} + h_{jEi} \cdot Q_{jEi}}{2} + \sqrt{\left\{\frac{Q_{p0} + h_{jEi} \cdot Q_{jEi}}{2}\right\}^2 + T_{F0} \cdot C_{10} \cdot e^{\frac{V_{BEi}}{V_T}}} \quad (10)$$

or by putting  $Q_{p0}$  in factor

$$Q_{pT} = Q_{p0} \cdot \left\{ \frac{1 + h_{jEi} \cdot q_{jEi}}{2} + \sqrt{\left\{\frac{Q_{p0} + h_{jEi} \cdot q_{jEi}}{2}\right\}^2 + \underbrace{\frac{T_{F0}}{Q_{p0}}}_{1/I_{KF}} \cdot \underbrace{\frac{C_{10}}{Q_{p0}}}_{I_S} \cdot e^{\frac{V_{BEi}}{V_T}}} \right\} \quad (11)$$

- We obtain finally the expression of the collector current at medium current densities by reinserting (11) in (5)

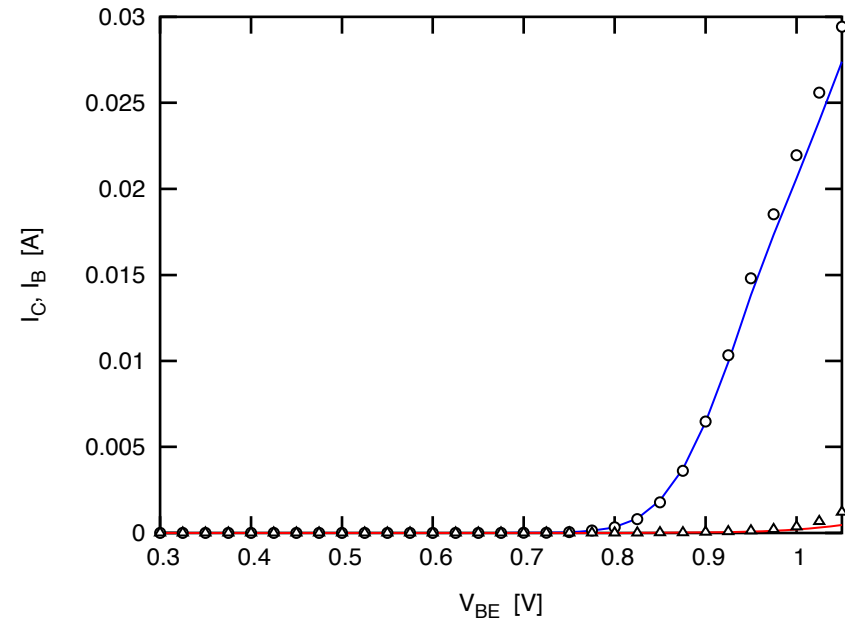
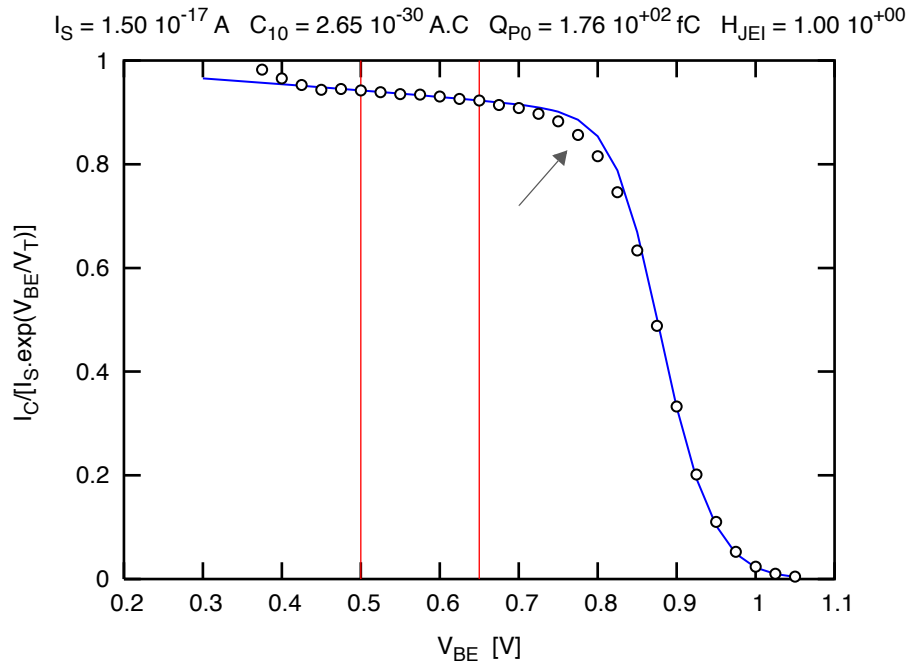
$$I_C = \frac{I_S \cdot e^{\frac{V_{BEi}}{V_T}}}{\frac{1 + h_{jEi} \cdot q_{jEi}}{2} + \sqrt{\left\{\frac{1 + h_{jEi} \cdot q_{jEi}}{2}\right\}^2 + \frac{I_S}{I_{KF}} \cdot e^{\frac{V_{BEi}}{V_T}}}} \quad \text{with} \quad \begin{cases} I_S = C_{10}/Q_{p0} \\ I_{KF} = Q_{p0}/T_{F0} \\ q_{jEi} = Q_{jEi}/Q_{p0} \end{cases} \quad (12)$$

# Comments

- ❏ Expression (12) is similar to the one of SGP model formulation, excepted that the forward knee current  $I_{KF}$ , which is a model parameter in SGP model, is defined as the ratio of the zero bias hole charge  $Q_{P0}$  to the low current forward transit time  $T_{F0}$ .
- ❏ This formulation is more physics, but a wrong combination of  $Q_{P0}$  and  $T_{F0}$  leads a bad fit of DC characteristics at high current densities.
- ❏ Therefore, the difficulty (or even the impossibility), to decouple  $C_{10}$ ,  $Q_{P0}$  and  $h_{jEi}$  from DC characteristics at low currents must have a strong impact a medium and high current densities.
- ❏ Verification →


# Effect of $h_{jEi}$ , $C_{10}$ and $Q_{p0}$ on DC Characteristics at Medium and High Current Densities

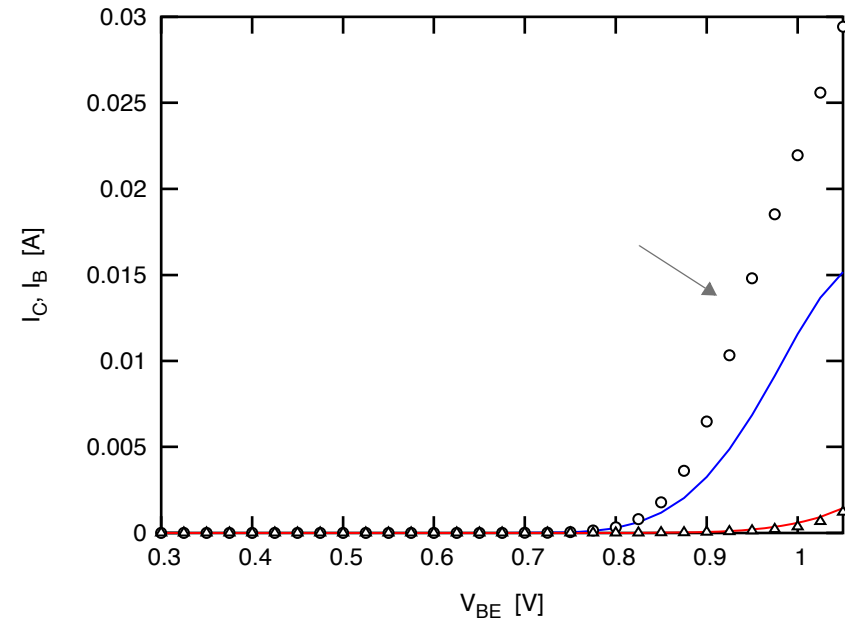
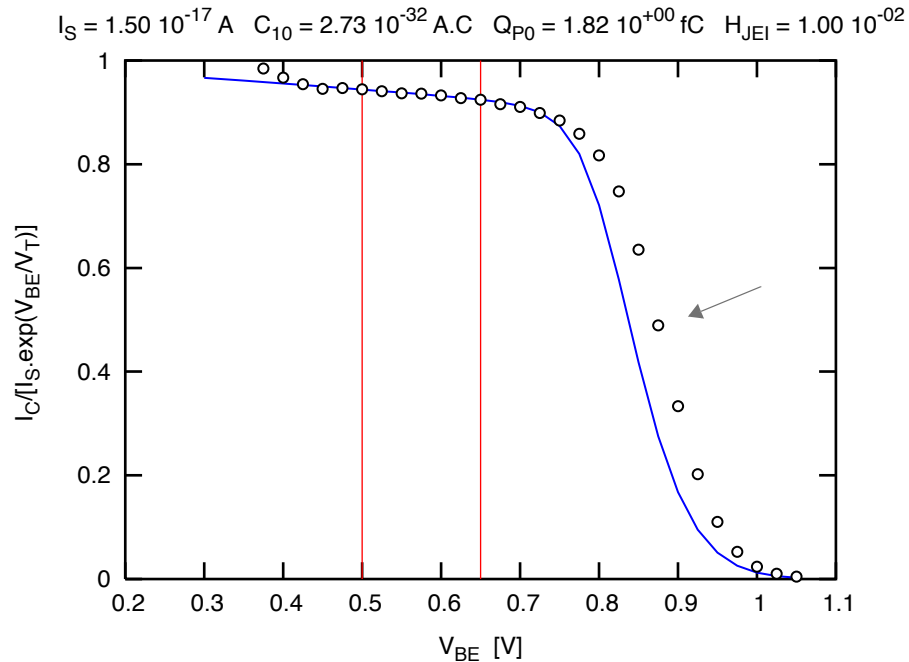
  $h_{jEi} = 1$



- With  $h_{jEi} = 1$ , after the high current parameter extraction (transit time, series resistances...), the fit on DC characteristics is satisfactory, with a little loss of accuracy around  $V_{BE} = 0.8$  V.

# Effect of $h_{jEi}$ , $C_{10}$ and $Q_{P0}$ on DC Characteristics at Medium and High Current Densities

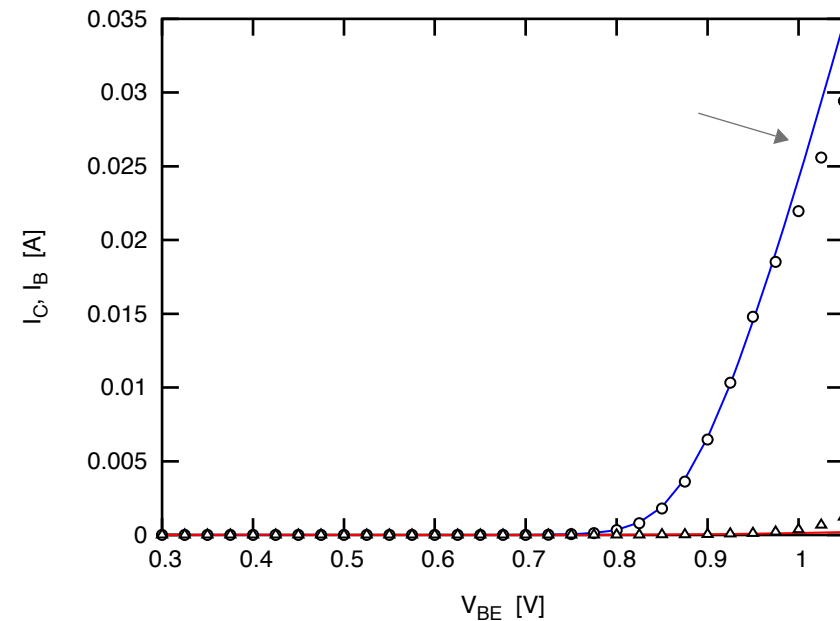
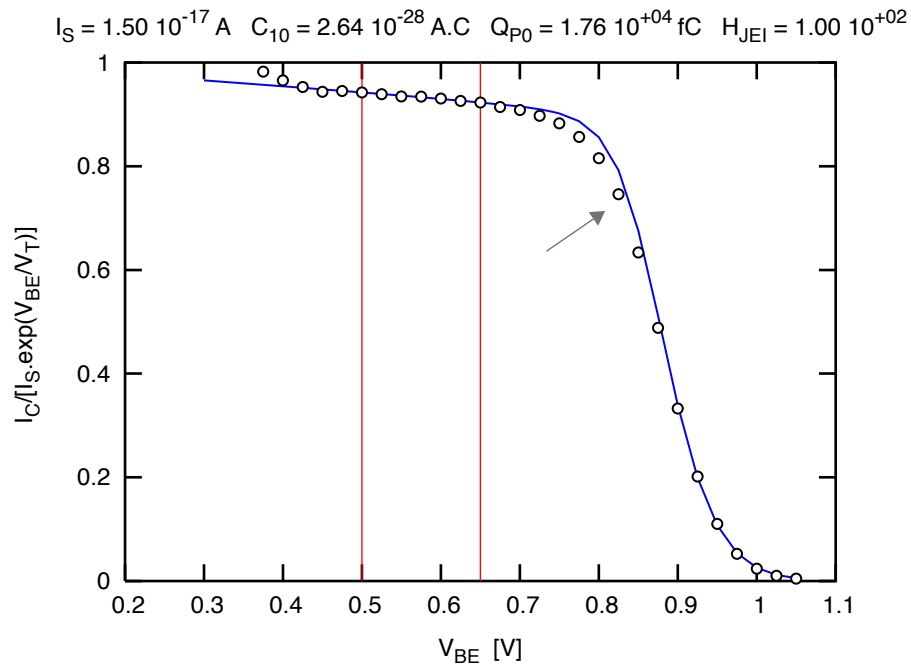
  $h_{jEi} = 0.01$



- With  $h_{jEi} = 0.01$ , both  $C_{10}$  and  $Q_{P0}$  are underestimated by approximately a factor of **0.01**. There is no impact on DC characteristics at low currents ( $I_S = C_{10}/Q_{P0}$ ), but as expected, there is a strong effect at high currents due to an underestimation of the forward knee ( $I_{KF} = Q_{P0}/T_{F0}$ ) current by approximately a factor of **0.01**.

# Effect of $h_{jEi}$ , $C_{10}$ and $Q_{P0}$ on DC Characteristics at Medium and High Current Densities

  $h_{jEi} = 100$

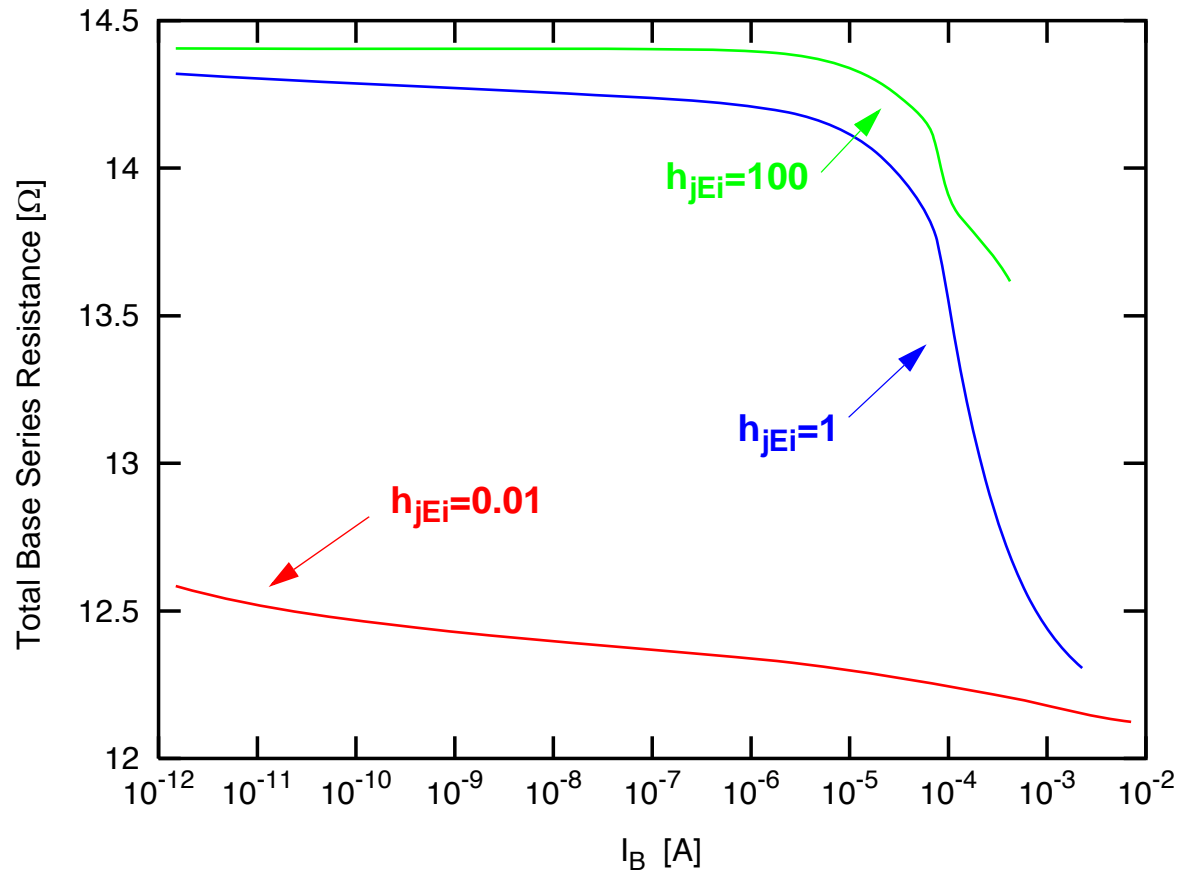


- With  $h_{jEi} = 100$ , both  $C_{10}$  and  $Q_{P0}$  are overestimated by approximately a factor of **100**. There is no impact on DC characteristics at low currents ( $I_S = C_{10}/Q_{P0}$ ), but as expected, there is an effect at high currents due to an overestimation of the forward knee current ( $I_{KF} = Q_{P0}/T_{F0}$ ) by approximately a factor of **100**. This effect is less visible than for  $h_{jEi} = 0.01$ , because in this case, at high currents the DC characteristics are no more controlled by the too high forward knee current, but rather by the voltage drop in resistances ( $R_E$ ,  $r_{bb'}$ ).



# Impact on Base Series Resistance

- Despite  $h_{jEi}$  as no effect on the collector current at low current densities, it strongly affects the internal base resistance which is very sensitive to the value of  $Q_{P0}$ . Any value of  $h_{jEi}$  cannot be used.



## Conclusion Part II : Medium Current Study

- As predicted, if the value of  $T_{F0}$ , determined from  $f_T$  characteristics at low and medium current densities, is assumed to be exact, we cannot use any value for  $Q_{P0}$ .
- The value of  $h_{jEi}$  does not affect the collector current at low and medium current densities, because the saturation current  $I_S$  defined as  $C_{10}$  over  $Q_{P0}$ , is independent on  $h_{jEi}$  ( $C_{10}$  and  $Q_{P0}$  are both proportional to  $h_{jEi}$ ).
- In the opposite, the fall-off of the DC current gain at medium current densities, which depends on the knee current defined as  $Q_{P0}$  over  $T_{F0}$ , is now strongly dependent on  $h_{jEi}$  which only affects the value of  $Q_{P0}$ .

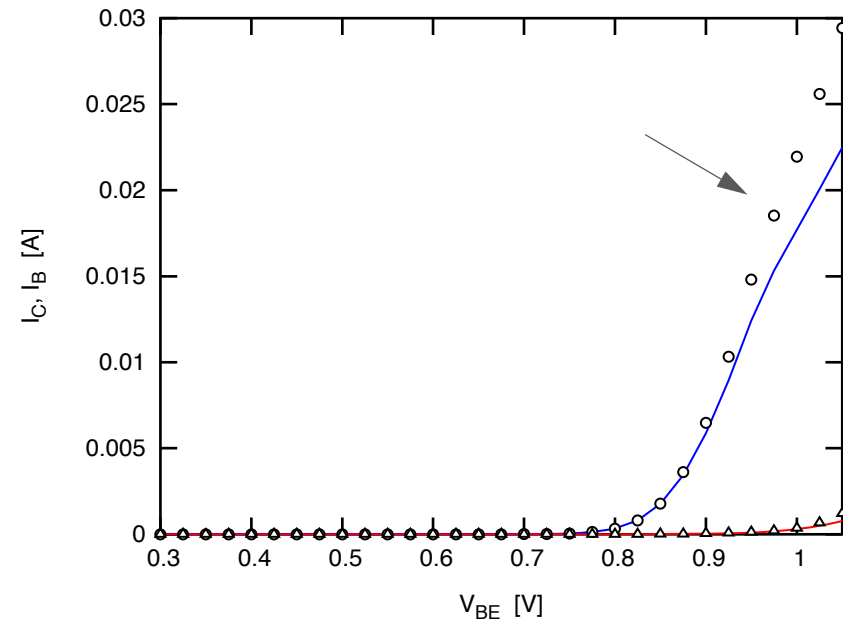
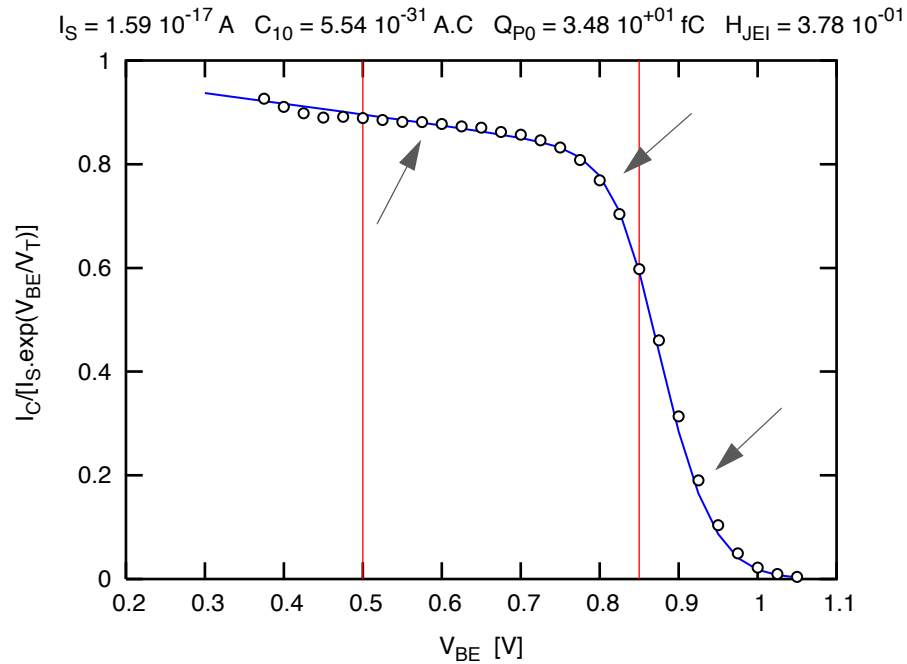
Parameter	$h_{jEi} = 1$	$h_{jEi} = 0.01$	$h_{jEi} = 100$
$C_{10} = C_{10} \cdot h_{jEi}$ (A.C)	$2.65 \cdot 10^{-30}$	$2.73 \cdot 10^{-32}$	$2.64 \cdot 10^{-28}$
$Q_{P0} = Q_{P0} \cdot h_{jEi}$ (fC)	$1.76 \cdot 10^2$	$1.82 \cdot 10^0$	$1.76 \cdot 10^4$
$I_S = C_{10}/Q_{P0}$ (A)	$1.50 \cdot 10^{-17}$	$1.50 \cdot 10^{-17}$	$1.50 \cdot 10^{-17}$
$I_{KF} = Q_{P0}/T_{F0}$ (A)	$128 \cdot 10^{-3}$	$1.33 \cdot 10^{-3}$	$12.8 \cdot 10^0$

# An Other Alternative to the Determination of $h_{jEi}$ ?

- From these analysis, the following proposal was suggested in [4]
  - Knowing  $T_{F0}$ , optimization of  $Q_{P0}$  in order to have the right fall-off of the forward DC current gain at medium current densities.
  - Now, knowing  $Q_{P0}$ ,  $C_{10}$  and  $h_{jEi}$  can be determined, without ambiguity, from the normalized collector current at low current densities, as explained in part I.
- The idea is interesting, but is it the *ultimate* method to accurately *decouple*  $C_{10}$ ,  $Q_{P0}$  and  $h_{jEi}$ ?
  - Not possible to be accurate both at medium and low current densities.
  - $h_{jEi}$  value perhaps unrealistic?
  - Is it a model (is  $h_{jEi}$  bias dependent?) or an extraction issue?
- The boundaries used for the optimization of  $Q_{P0}$  at high current must be carefully chosen, (i) not too low in order to have an impact of the knee current, (ii) not too high in order to be not affected by other high-current secondary effects (self-heating...).

# Results

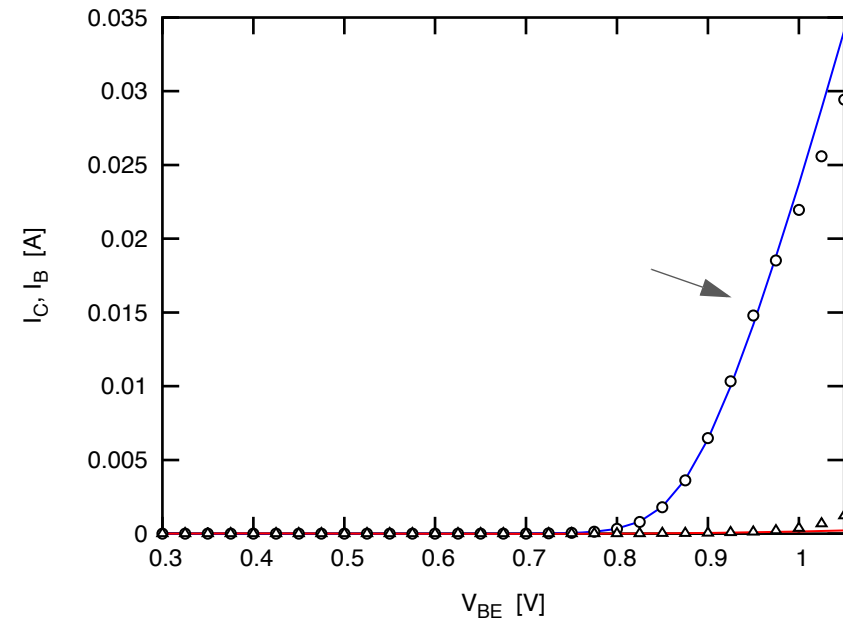
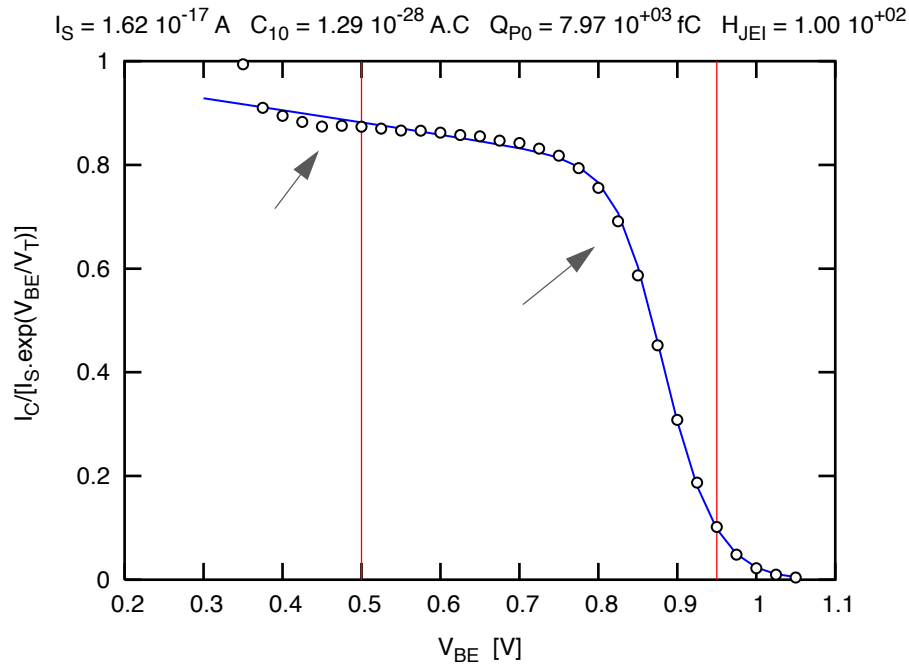
## Optimization between $V_{BE} = 0.5$ to $0.85$ V



- Better fit around  $V_{BE} = 0.80$  V
- But  $h_{JEI}$  less than 1 (non-physical?). Consequently, underestimation of  $C_{10}$  and  $Q_{P0}$ .
- Slope of the normalized collector current is too high at low current ( $I_S = 1.59 \cdot 10^{-17}$  instead of  $1.50 \cdot 10^{-17}$  A).
- High injection parameter need to be re-optimized in order to improve the accuracy at very high current densities.

# Results

## Optimization between $V_{BE} = 0.5$ to $0.95$ V



- Better fit around and after  $V_{BE} = 0.80$  V
- **But** unrealistic parameters:  $h_{JEI}$  is too high, stuck to its maximum value (100). Consequently, overestimation of  $C_{10}$  and  $Q_{P0}$ .
- Slope of the normalized collector current is too high at low current ( $I_S = 1.62 \cdot 10^{-17}$  instead  $1.50 \cdot 10^{-17}$  A).

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- ❏ **Any suggestions, ideas, proposals are welcome!...**
- ❏ In the meantime, some advice
  - Either set  $h_{jEi}$  to **1**, it is better than to use a non-physical value, especially after for determining  $C_{10}$  and  $Q_{P0}$ .
  - Or, to determine  $Q_{P0}$  from tetrode measurements or TCAD simulations and than to optimize  $C_{10}$  and  $h_{jEi}$  from the normalized collector current  $I_{CN} = I_C / e^{\frac{V_{BE}}{V_T}}$  in the low current region.
  - Avoid to fit  $h_{jEi}$  at medium current densities, that improve a little bit the accuracy in this region to the detriment of the physics, this parameter being in this case often underestimated.

# And to Conclude...



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→ If there is no solution it is perhaps because there is no problem...



Image: <http://zesonic.free.fr/devises.htm>

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