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# Thermal Capacitance $c_{th}$ – its Determination and Influence on Transistor and Circuit Performance

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# Overview

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- Motivation
  - D/A Converter Issues
  - Previous Assumptions
- Thermal Time Constant  $\tau_{TH} = r_{th} \times c_{th}$ 
  - Definition
  - Measurement Methods
- Simulation Results for Output Admittance
- $c_{th}$  Extraction for Different IHP HBT Types
- Summary

# Overview

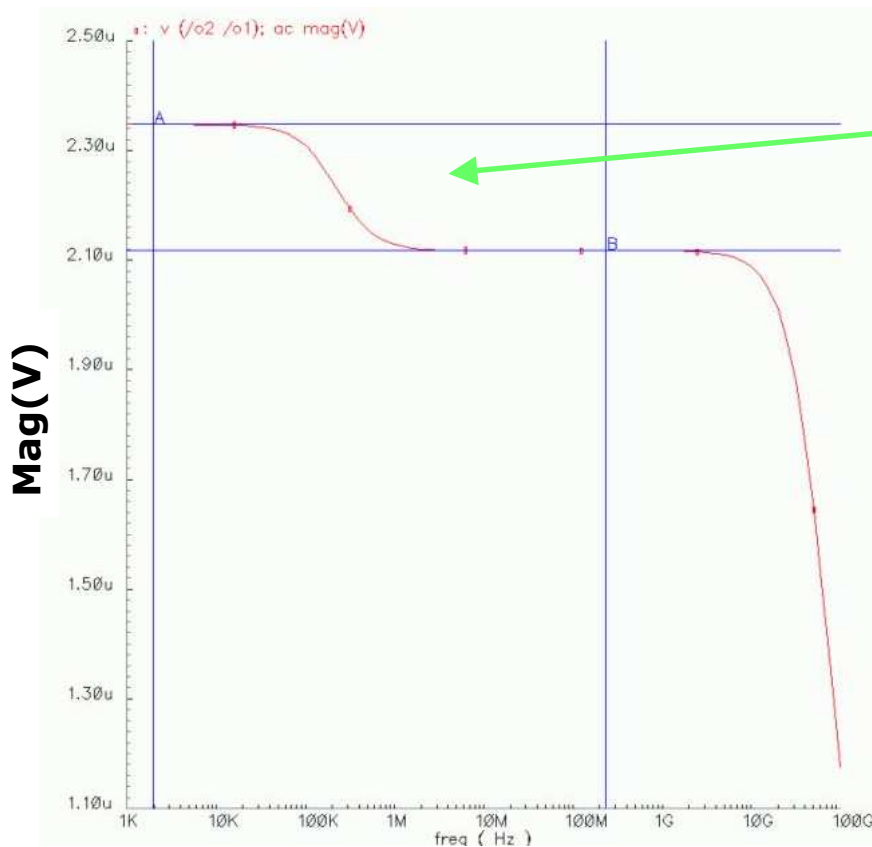
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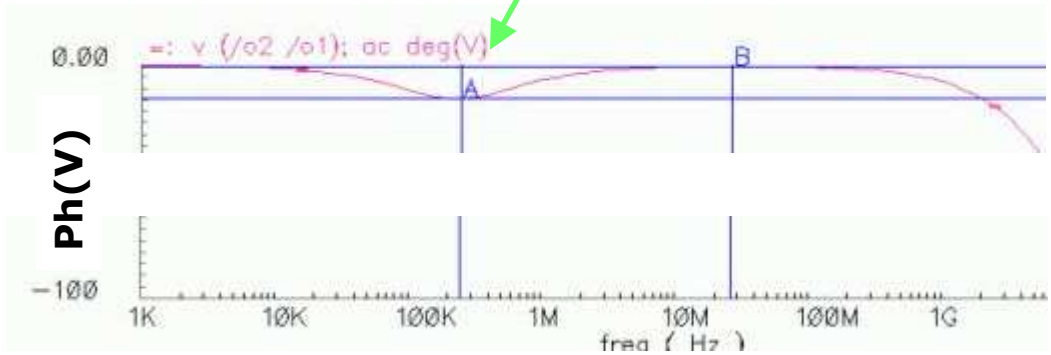
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# Motivation

- Fast A/D converters are currently a “hot topic” for IHP customers
  - I received similar questions from different designers
  - main issue: “particular behavior of ac response of bipolar differential pair”



“Step” in magnitude and “sink” in phase of frequency response.  
Cause? cth ?!  
How accurate is model for cth ?



# Previous Assumptions

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- For all IHP HBT VBIC models  $c_{th} > 0$ .
  - Based on pulsed measurements of thermal time constant
$$\tau_{TH} = r_{th} \cdot c_{th}$$
(F. Korndörfer, AK Bipolar 2006):
    - $c_{th} \sim 400$  pJ/K for H1-HS HBT with emitter number  $NX=8$
    - Assumption:  $\tau_{TH} \sim 850$  ns = constant for  $NX=1 - 8$
    - For all other HBT we chose
$$c_{th} \sim 100$$
 pJ/K and  $r_{th} \cdot c_{th} = \text{const.}$
    - Therefore, if  $r_{th} \sim NX^{-0.8} \rightarrow c_{th} \sim NX^{0.8}$
- But: one customer complained that  $\tau_{TH}$  must be function of HBT size

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# Self Heating I

- Power dissipation  $p(t)$  leads to increase of HBT junction temperature:

$$p(t) = \frac{dW_{th}(t)}{dt} + p_{th}(t) = C_{TH} \frac{d\Delta T(t)}{dt} + \frac{\Delta T(t)}{R_{TH}}$$

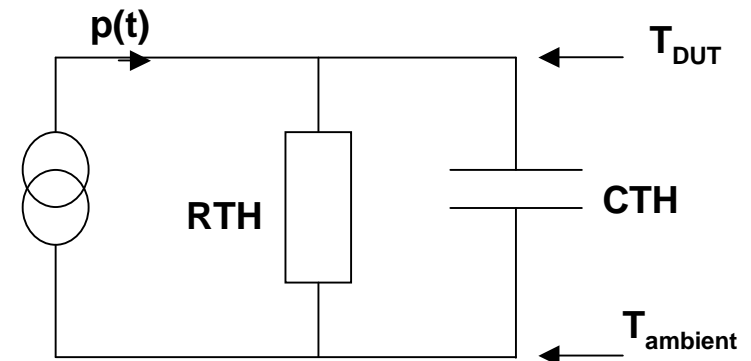
$$\Delta T = T_{DUT} - T_{ambient}$$

- Transient temperature response is determined by thermal time constant :

$$\Delta T(t) = P(t \rightarrow \infty) \cdot R_{TH} \cdot \left( 1 - \exp\left[ -\frac{t}{\tau_{TH}} \right] \right),$$

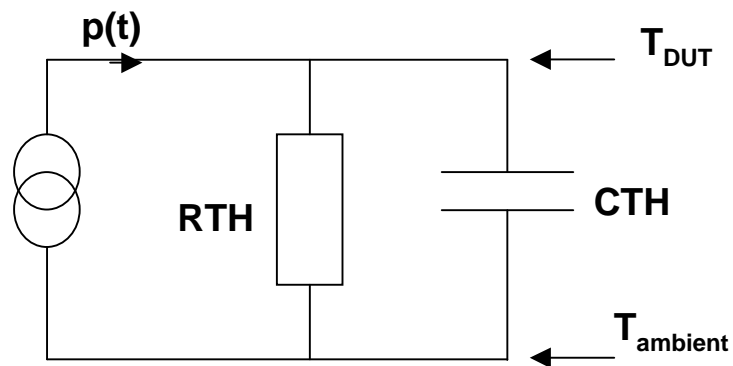
$$\tau_{TH} = R_{TH} \cdot C_{TH}$$

$$[\text{K/W}] \cdot [\text{J/K}]$$



# Self Heating II

- In compact models  $\Delta T$  is calculated by using a simplified thermal network with only one thermal time constant



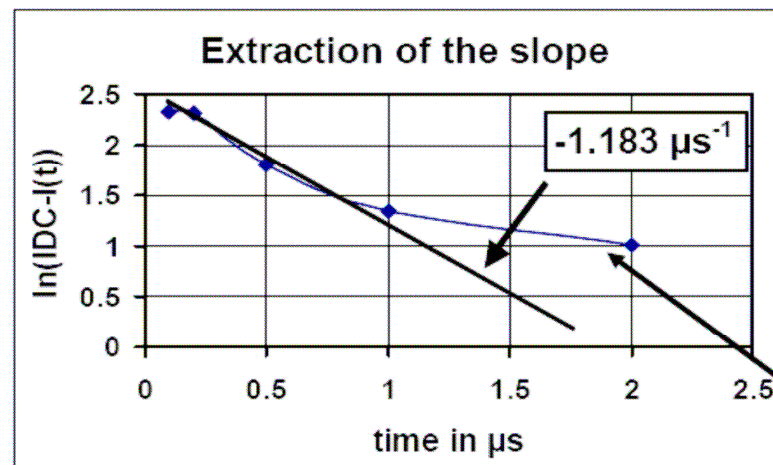
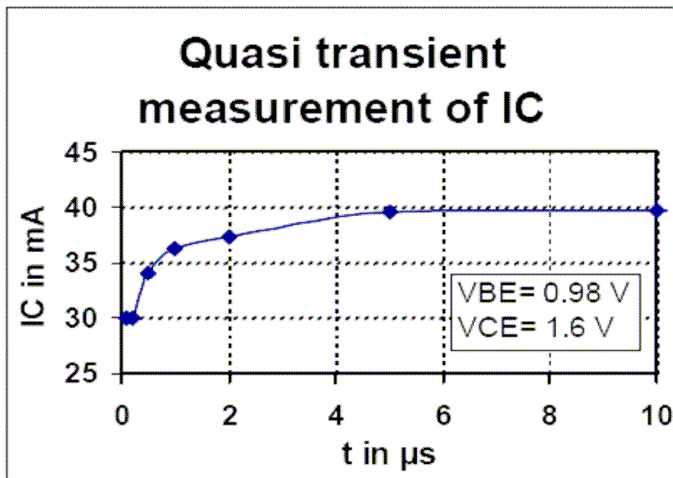
- Thermal resistance  $r_{th}$  can easily be measured with DC analyzer



# 1<sup>st</sup> Approach: Pulsed Measurements



- Concept presented at 2006 AK Bipolar (F. Korndörfer)
  - dynamic I(V) analyzer → 100ns – 1ms pulse width
  - DUT: SG25H1 HS-HBT ( $f_T = 180$  GHz)



second time constant is visible

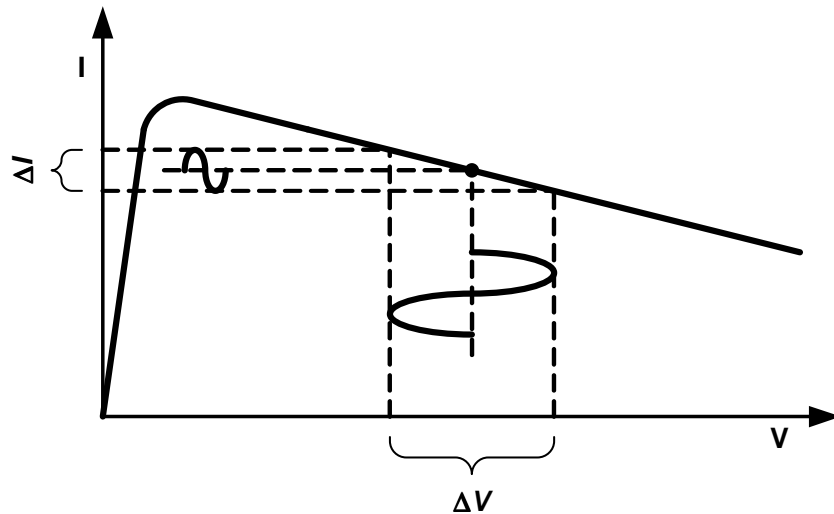
$$\tau_{TH} = -\frac{1}{m} \approx 0.85 \mu\text{s}$$

With given  $\tau_{th}$  this lead to  $c_{th} \sim 400$  pJ/K for largest DUT with 8 emitter in BEC configuration.

## 2<sup>nd</sup> Approach: Impedance Analyzer



- Output characteristic with fixed IB
  - Based on concept by Bruce et al., Electronics Letters 33(2), 1997



$$g_{\text{OUT}} = \Re\{Y_{\text{OUT}}\} = \frac{dI}{dV} \approx \frac{\Delta I}{\Delta V}$$

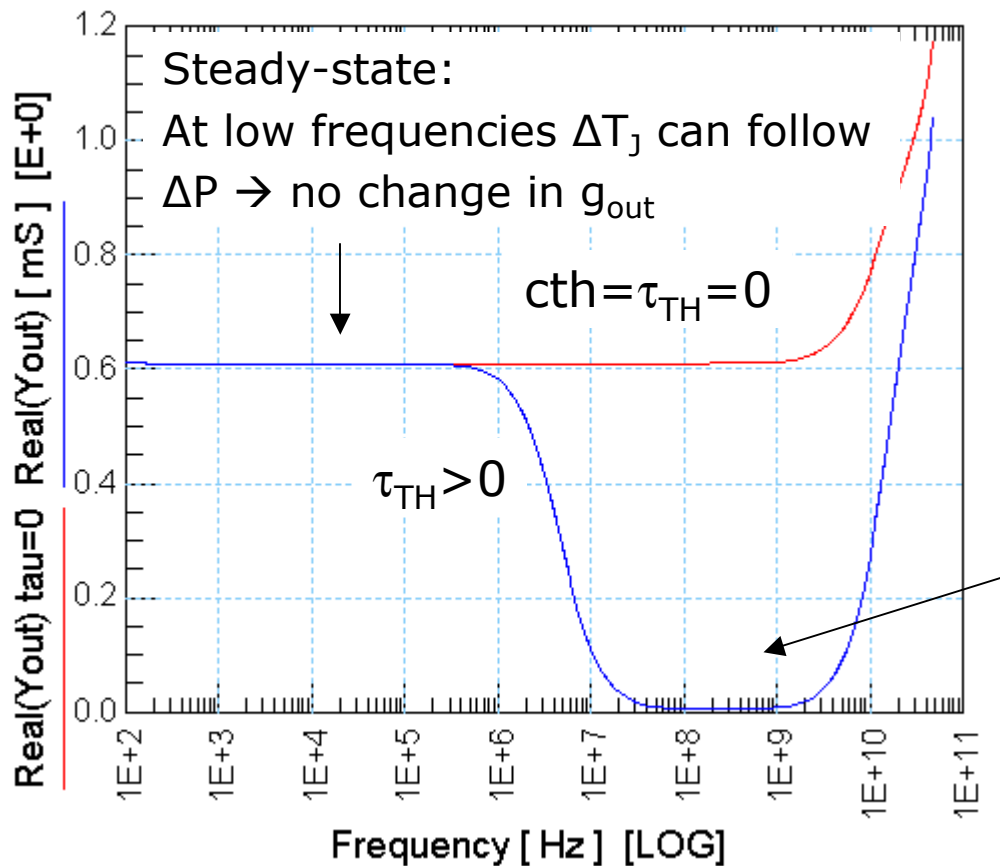
### Approach:

Use impedance analyzer to measure  $\text{Real}(Y_{\text{out}})$  as function of frequency and find the transition between steady-state and transient mode.

# $Y_{out}$ Transient Behavior (Simulation)



VBIC simulation example for  $g_{out} = \text{Re}(Y_{out}) = \text{Re}(Y_{22} + Y_{12})$  with fixed  $I_B$



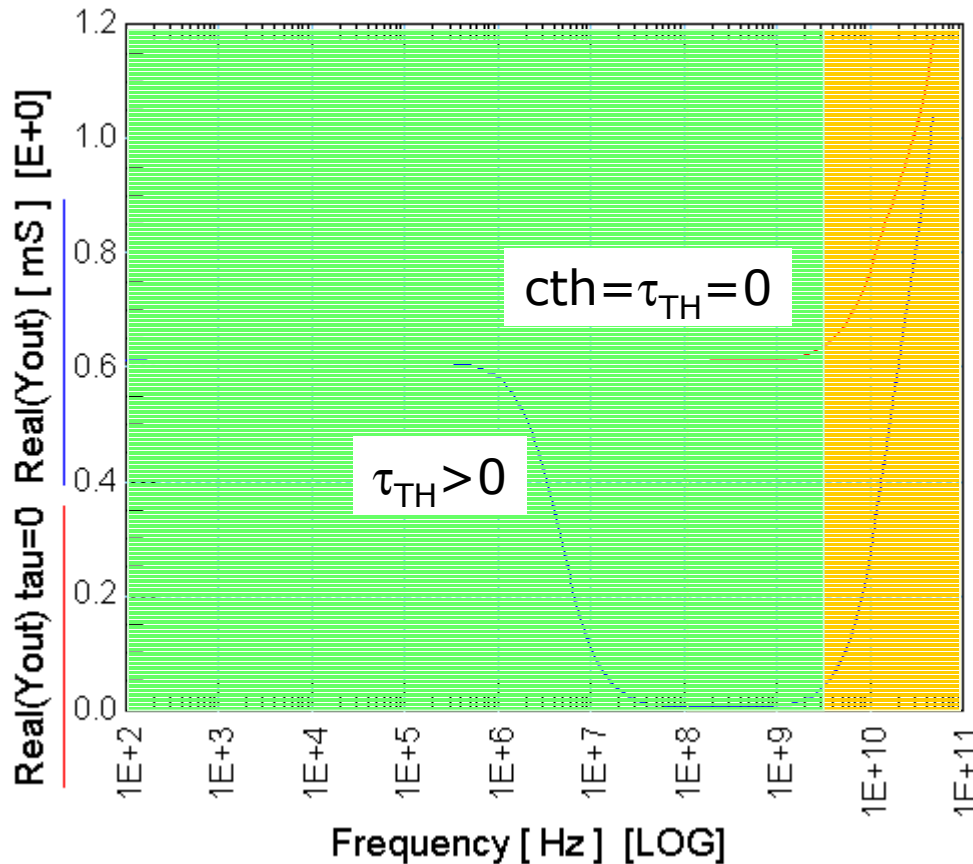
- Measurement of  $g_{out}$ 
  - from slope of  $Y_{out}$  in MHz range
  - extraction of  $\tau_{TH}$  possible

Transient mode:  
At high frequencies  $\Delta T_j$  cannot follow  
→  $g_{out}$  reaches its intrinsic value

# $Y_{out}$ Transient Behavior (Simulation)



VBIC simulation example for  $g_{out} = \text{Re}(Y_{out}) = \text{Re}(Y_{22} + Y_{12})$  with fixed  $I_B$



- Measurement of  $g_{out}$

- Frequency range  $< 3$  GHz:  
Impedance analyzer  
→ Ongoing work not yet to be published
- Frequencies  $> 100$  MHz:  
Network analyzer

# Overview

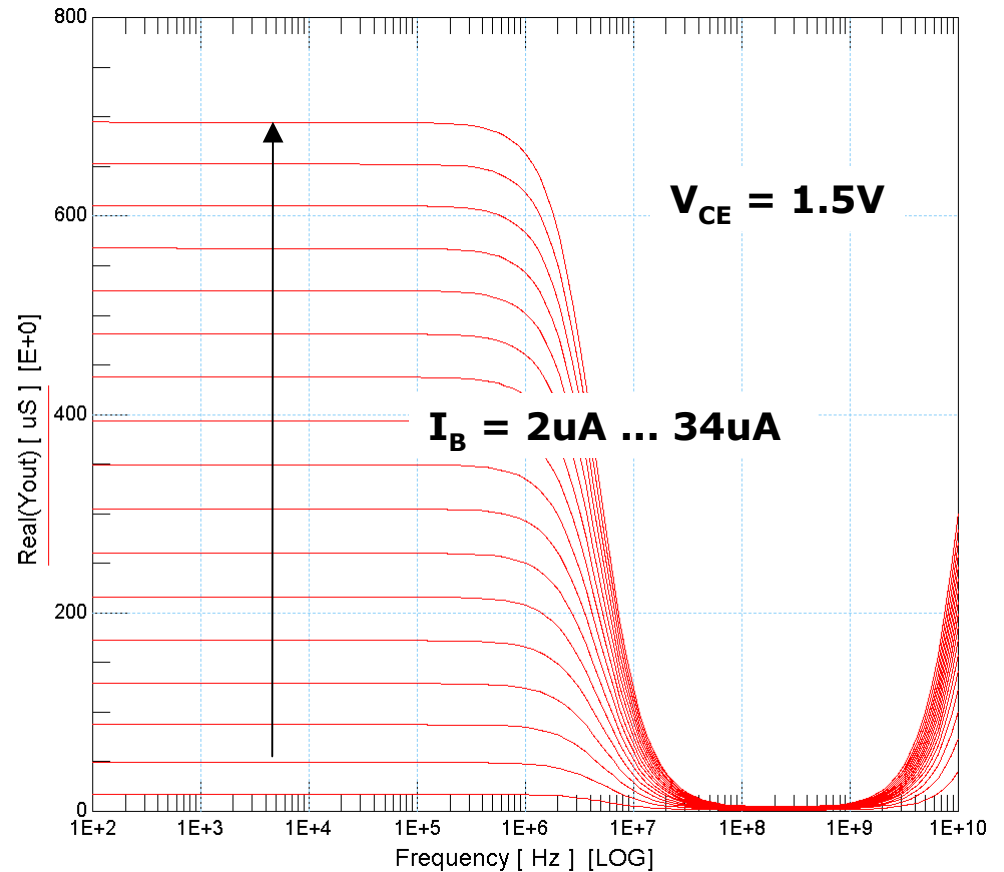
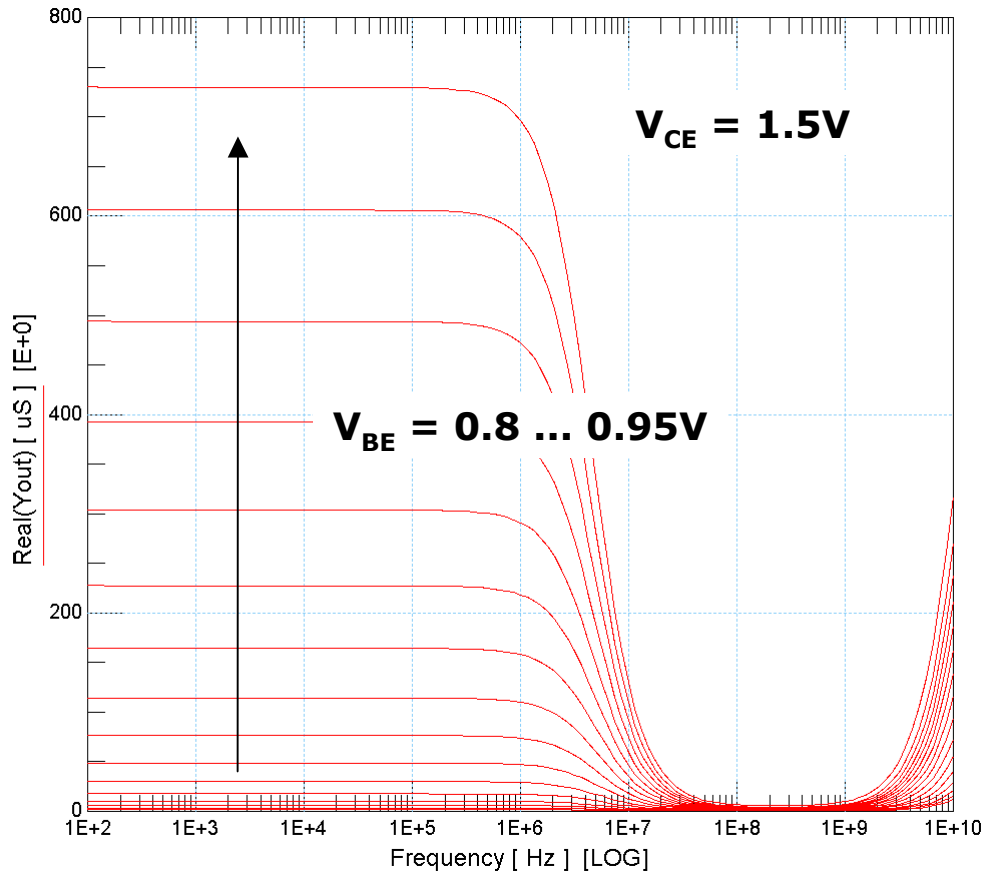
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# Output Admittance Simulations I



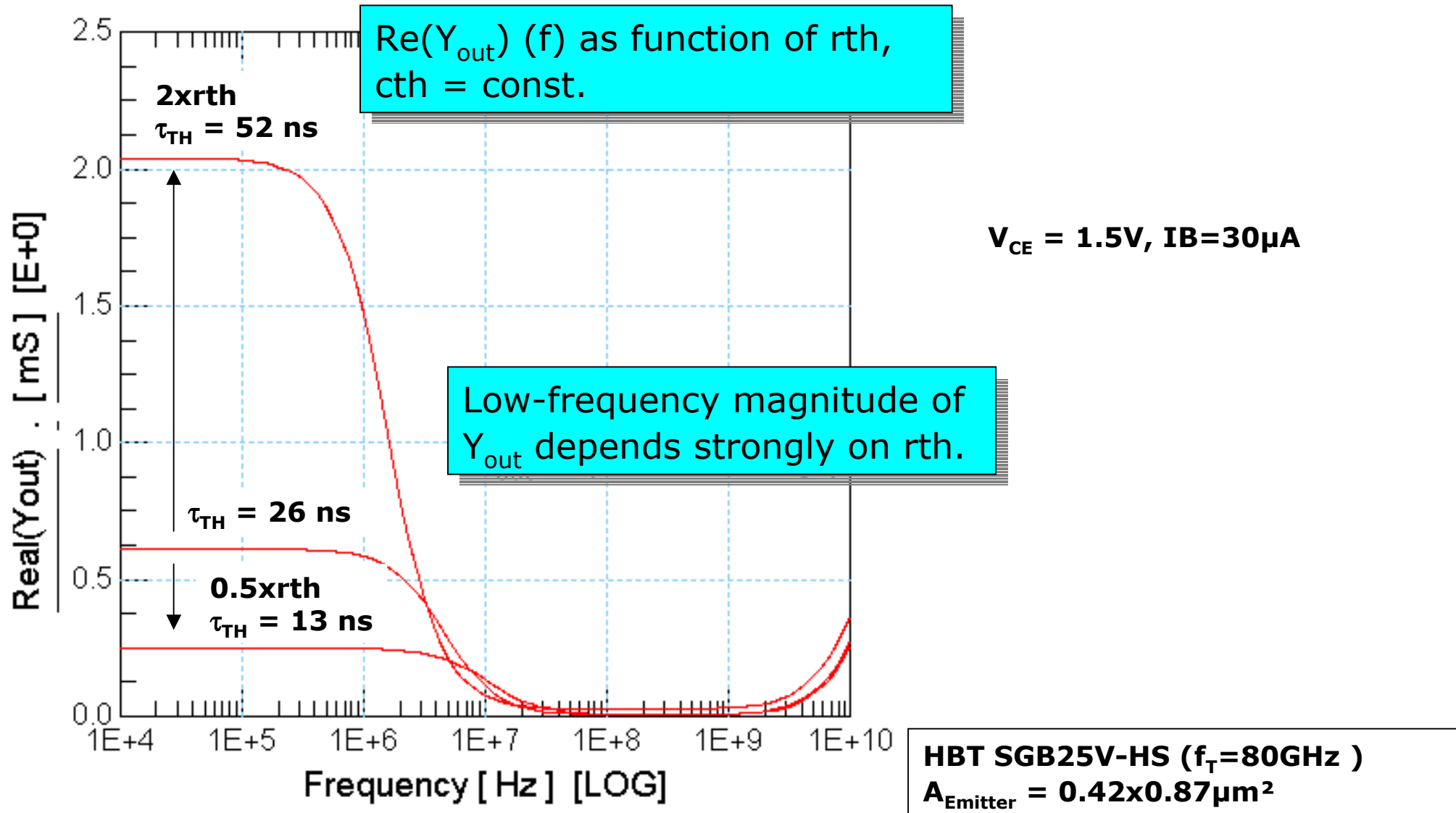
**Re( $Y_{out}$ ) (f) as function of operating point**



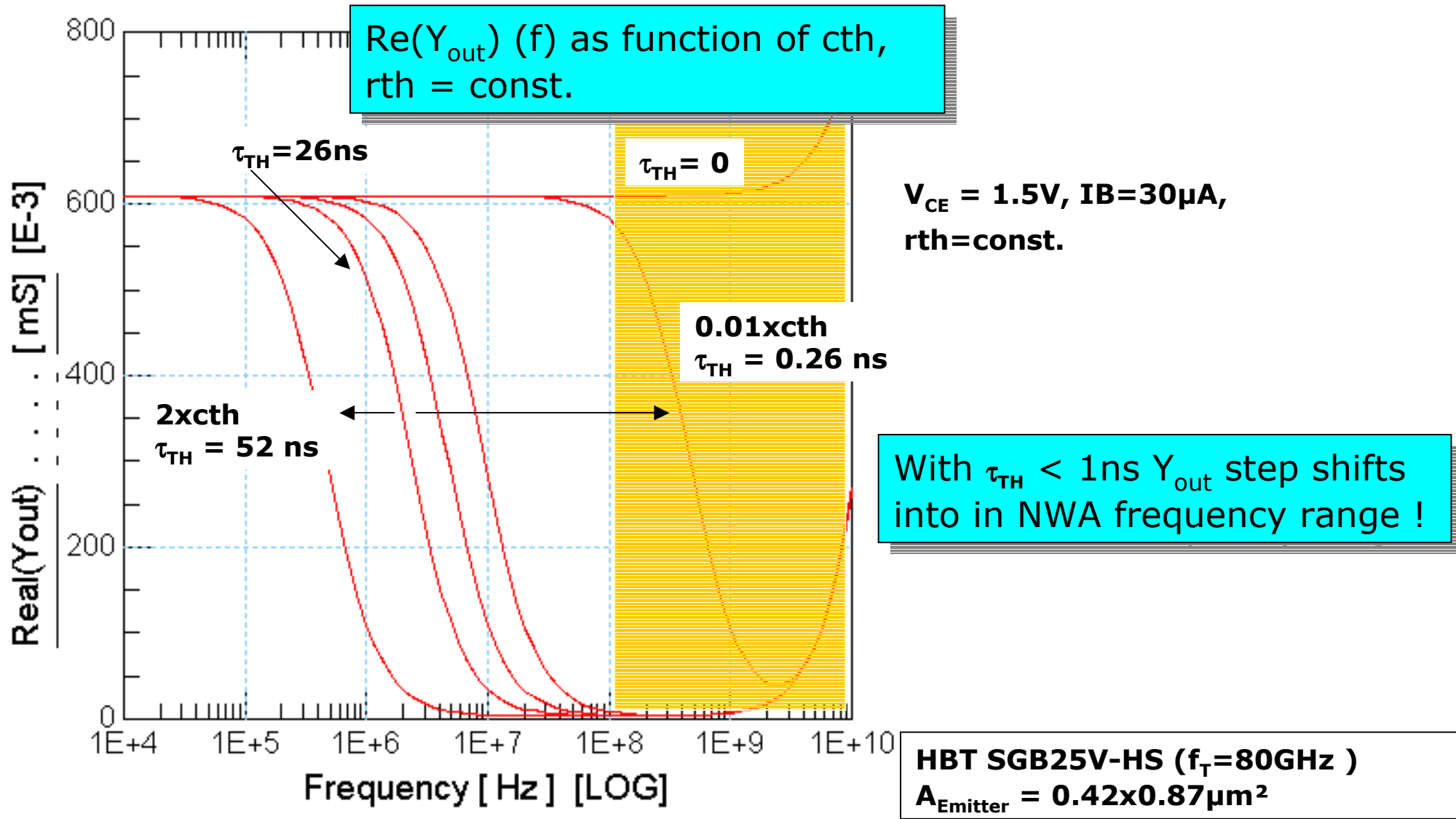
**HBT SGB25V-HS ( $f_T=80\text{GHz}$ )**

**$A_{\text{Emitter}} = 0.42 \times 0.87 \mu\text{m}^2$ ;  $r_{th}=3.900\text{K/W}$ ,  $cth = 6.7\text{pJ/K} \rightarrow \tau_{TH}=26\text{ns}$**

# Output Admittance Simulations II



# Output Admittance Simulations III

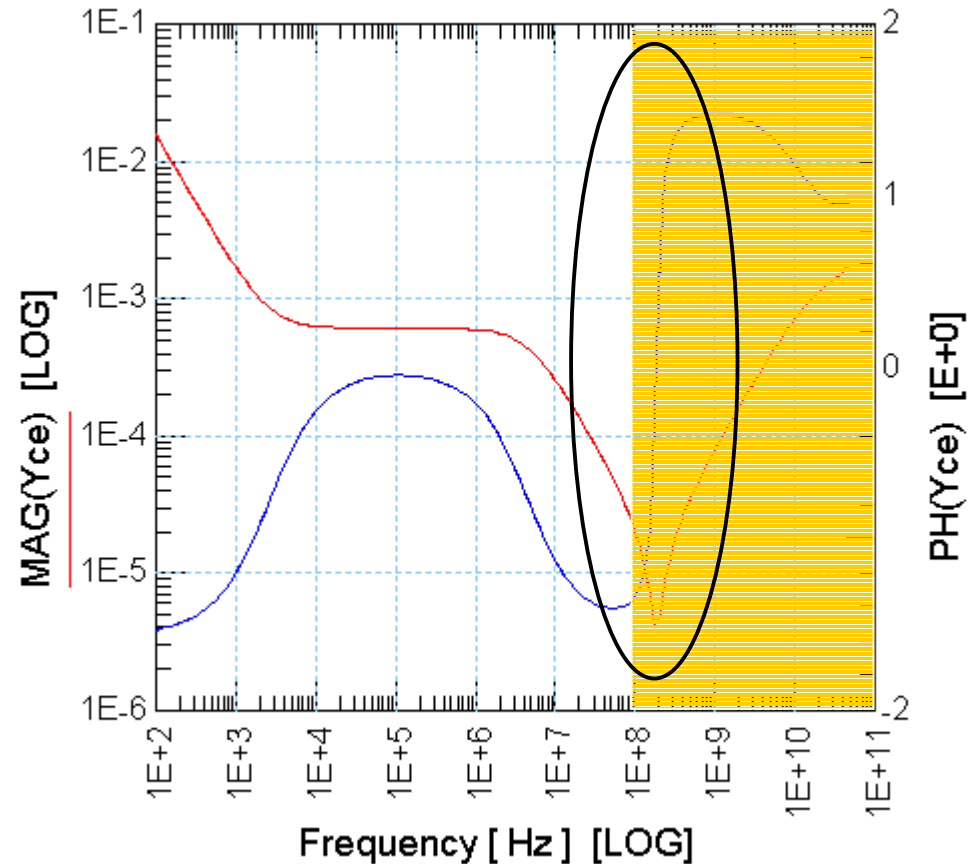
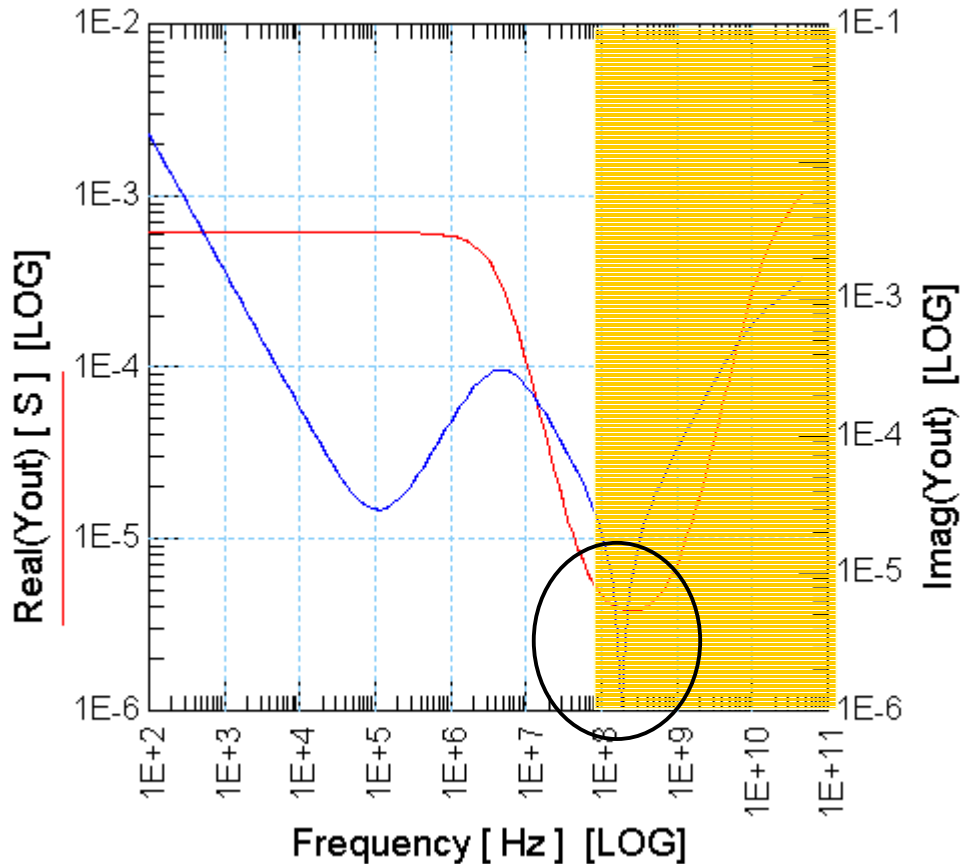




# Output Admittance Simulations IV



Real/Imag  $Y_{out}$  vs. Mag/Phase  $Y_{out}$



**HBT SGB25V-HS ( $f_T=80\text{GHz}$ )**  
 $A_{\text{Emitter}} = 0.42 \times 0.87 \mu\text{m}^2$   
 $V_{\text{CE}} = 1.5\text{V}$ ,  $I_B = 30 \mu\text{A}$ ,  $\tau_{\text{TH}} = 26\text{ns}$

(Oder) Germ

Because of minimum of  $\text{Mag}(Y_{out})$  and phase shift of  $\text{Ph}(Y_{out})$  at  $f > 100\text{MHz}$  extraction of  $c_{th}$  with NWA possible ?!

# Overview

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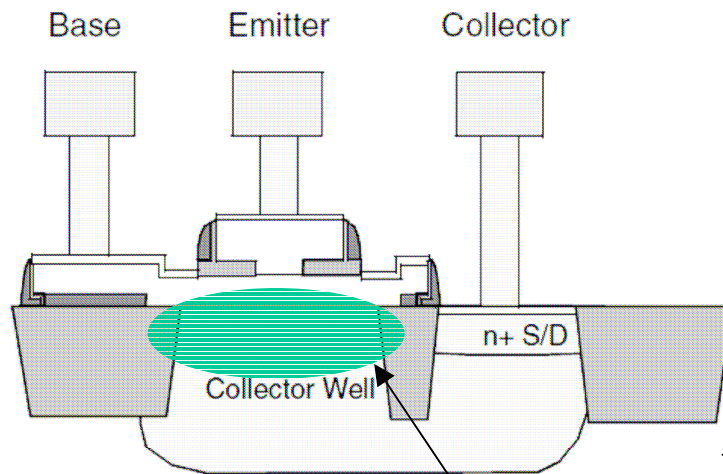
- Motivation
  - D/A Converter Issues
- Thermal Constant  $r_{th}$  x  $c_{th}$ 
  - Definition
  - Experimental Determination
- Simulation Results for Output Admittance
- **$c_{th}$  Extraction for Different IHP HBT Types**
- Summary

# Simulation Results – Test Devices

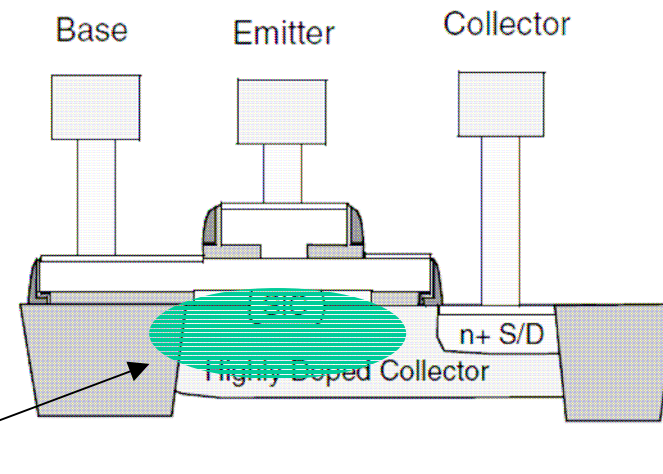
- Comparison of 5 different IHP HS-HBT types.

HBT-Type	Technology	fT [GHz ]	BVCE0 [ V ]	Layout	Minimum Emitter Size [ $\mu\text{m}^2$ ]		Active Bipolar Area [ $\mu\text{m}^2$ ]
SGB25V-HS	0.25 $\mu\text{m}$ BiCMOS	80	2.4	BEC	0.42x0.87	0.37	1.32
SG25H3-HS	0.25 $\mu\text{m}$ BiCMOS	110	2.2	BEC	0.3x0.92	0.28	0.81
SG25H1-HS-B	0.25 $\mu\text{m}$ BiCMOS	180	1.9	BEC	0.26x0.92	0.24	0.55
SG13-HS-CBEBEBC	0.13 $\mu\text{m}$ BiCMOS	250	1.75	CBEBEBC	0.16x1.04	0.17	0.44
SG13-HS-BEC	0.13 $\mu\text{m}$ BiCMOS	250	1.75	BEC	0.16x0.52	0.08	0.26

**STI BC separation**



**no STI BC separation**

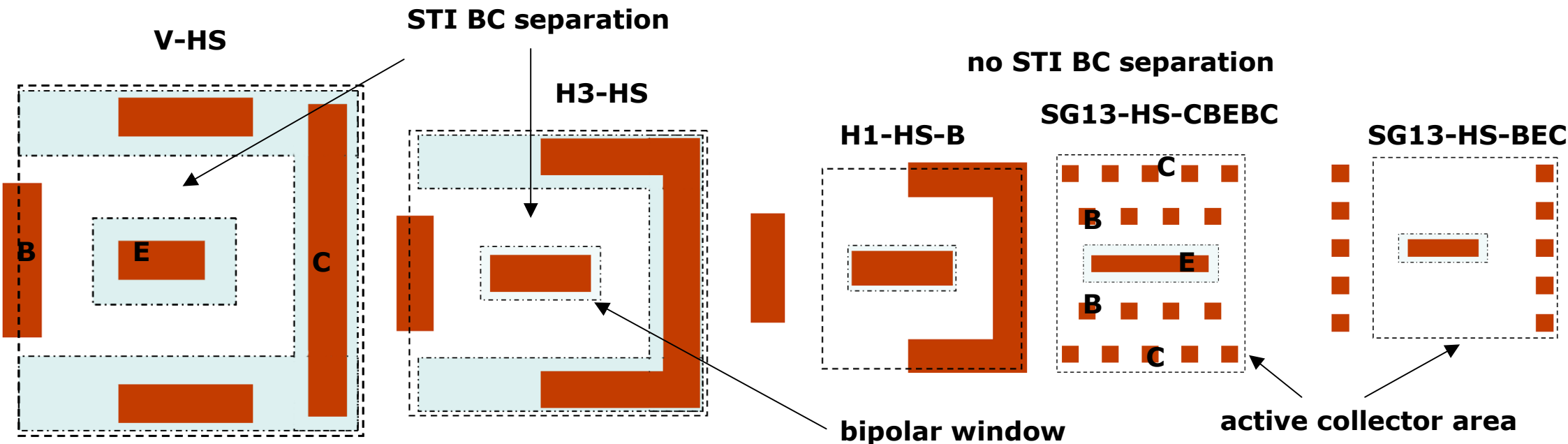


**active bipolar area**

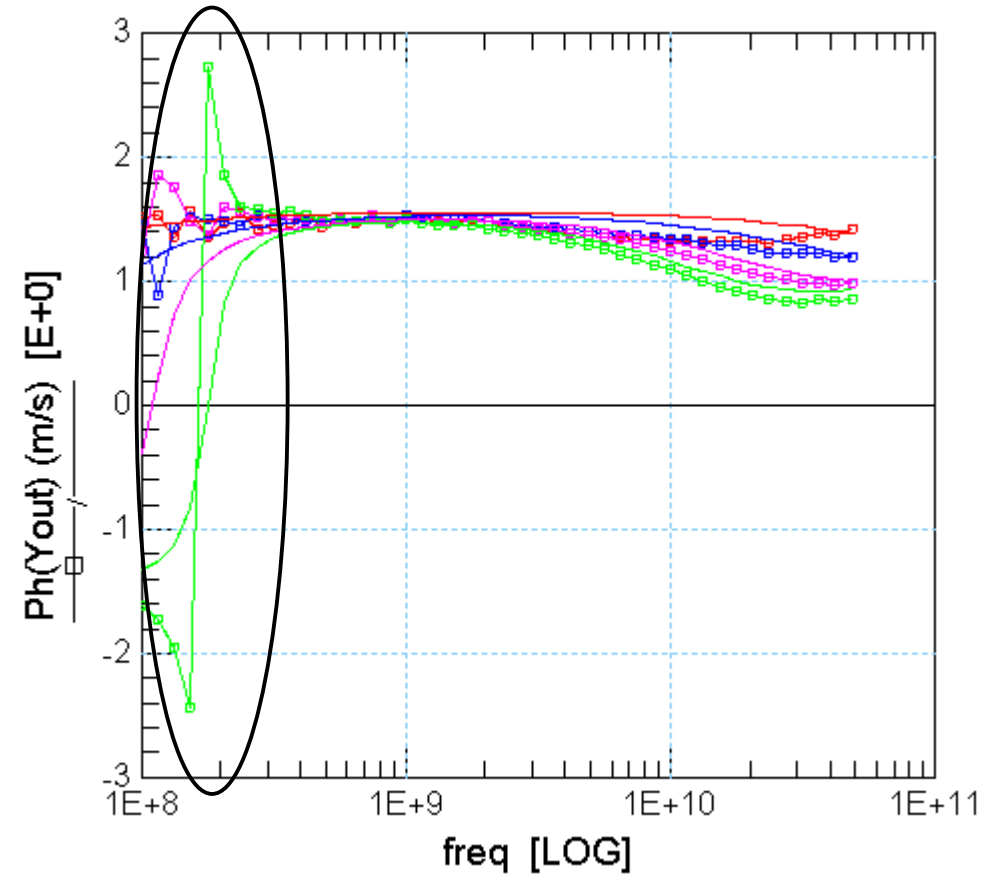
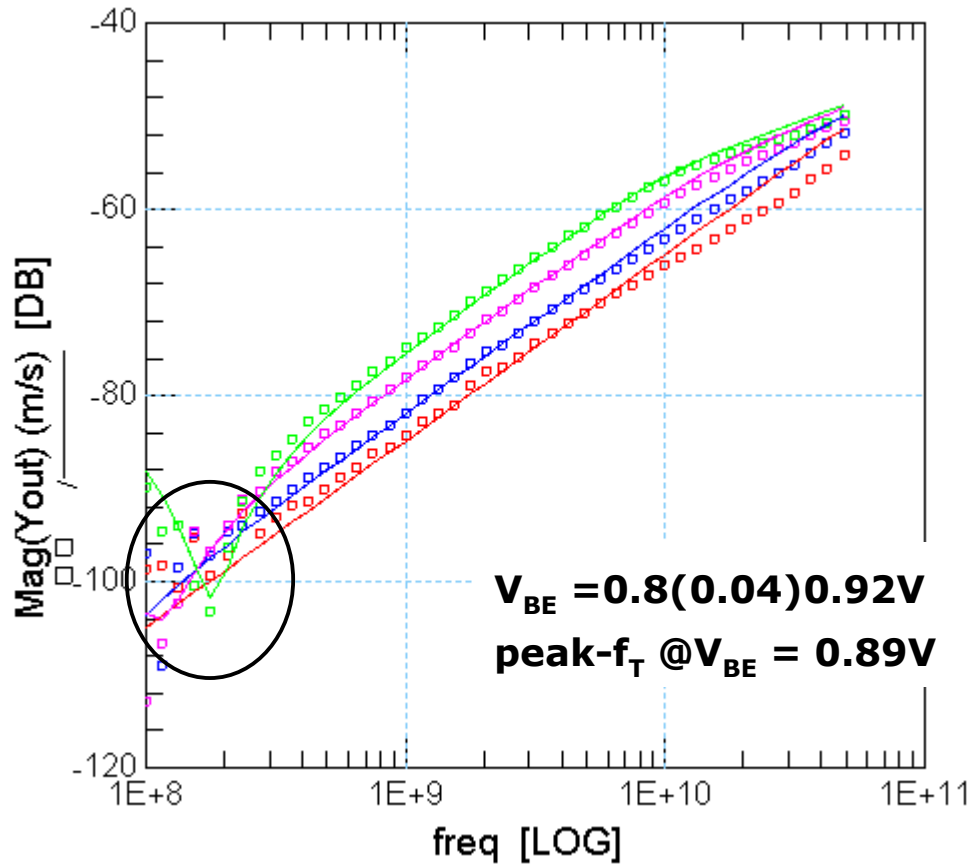
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SGB25V-HS	0.25 $\mu\text{m}$ BiCMOS	80	2.4	BEC	0.42x0.87	0.37	1.32
SG25H3-HS	0.25 $\mu\text{m}$ BiCMOS	110	2.2	BEC	0.3x0.92	0.28	0.81
SG25H1-HS-B	0.25 $\mu\text{m}$ BiCMOS	180	1.9	BEC	0.26x0.92	0.24	0.55
SG13-HS-CBEBC	0.13 $\mu\text{m}$ BiCMOS	250	1.75	CBEBC	0.16x1.04	0.17	0.44
SG13-HS-BEC	0.13 $\mu\text{m}$ BiCMOS	250	1.75	BEC	0.16x0.52	0.08	0.26



# SGB25V – HS-HBT



**HBT SGB25V-HS ( $f_T=80GHz$ )**  
 2 DUT parallel  
 $A_{Emitter} = 0.42 \times 0.87 \mu m^2$   
 $V_{CE} = 1.5V, \tau_{TH} = 26ns$

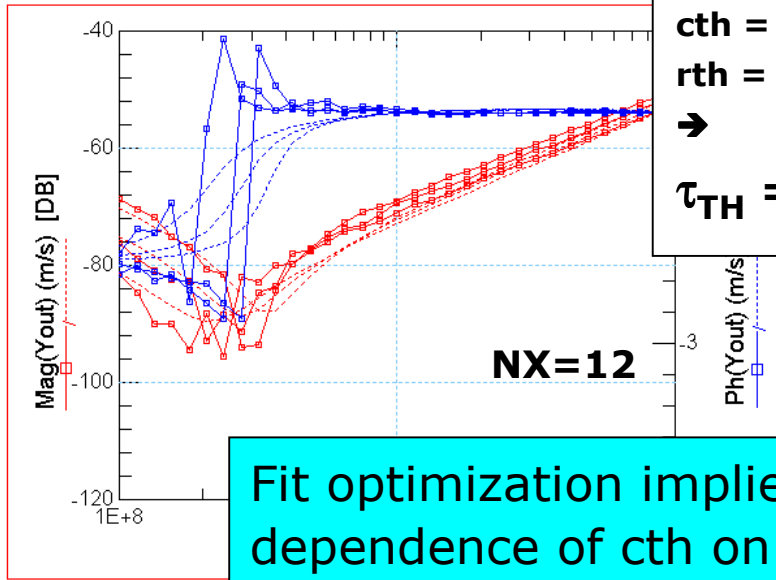
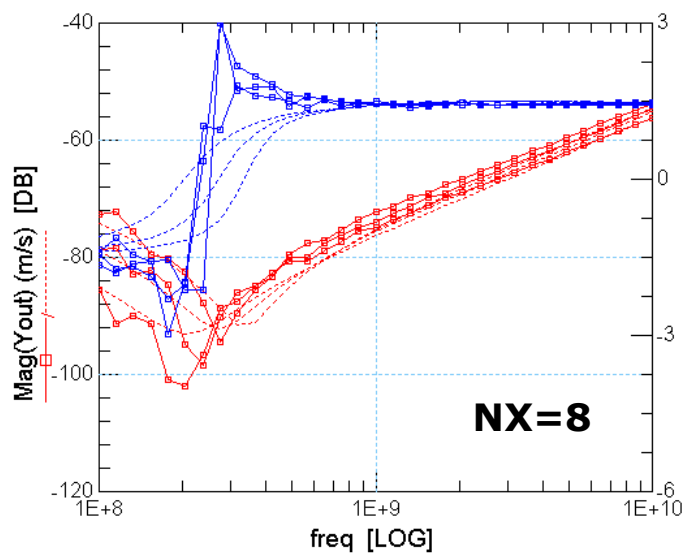
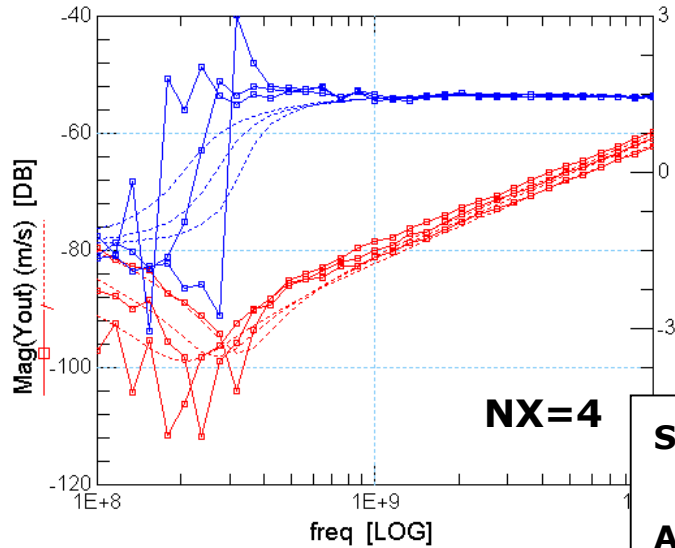
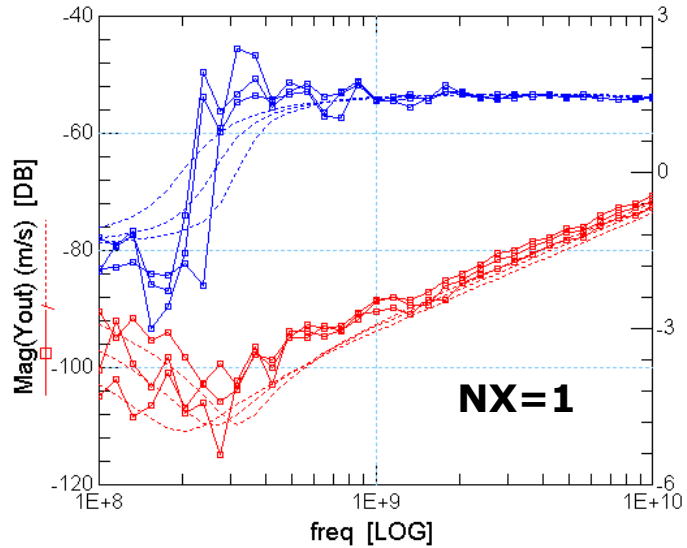
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Phase shift of  $Ph(Y_{out})$  and minimum of  $Mag(Y_{out})$  slightly above 100 MHz  $\rightarrow$  estimation of  $\tau_{TH} \sim 26ns$  possible !

# SG25H3 - HS-HBT ( $f_T = 110\text{GHz}$ )



$V_{CE} = 1.5\text{V}$ ,  
 $V_{BE} = 0.88(0.02)0.92\text{V}$   
 peak- $f_T$  @  $V_{BE} = 0.90\text{V}$

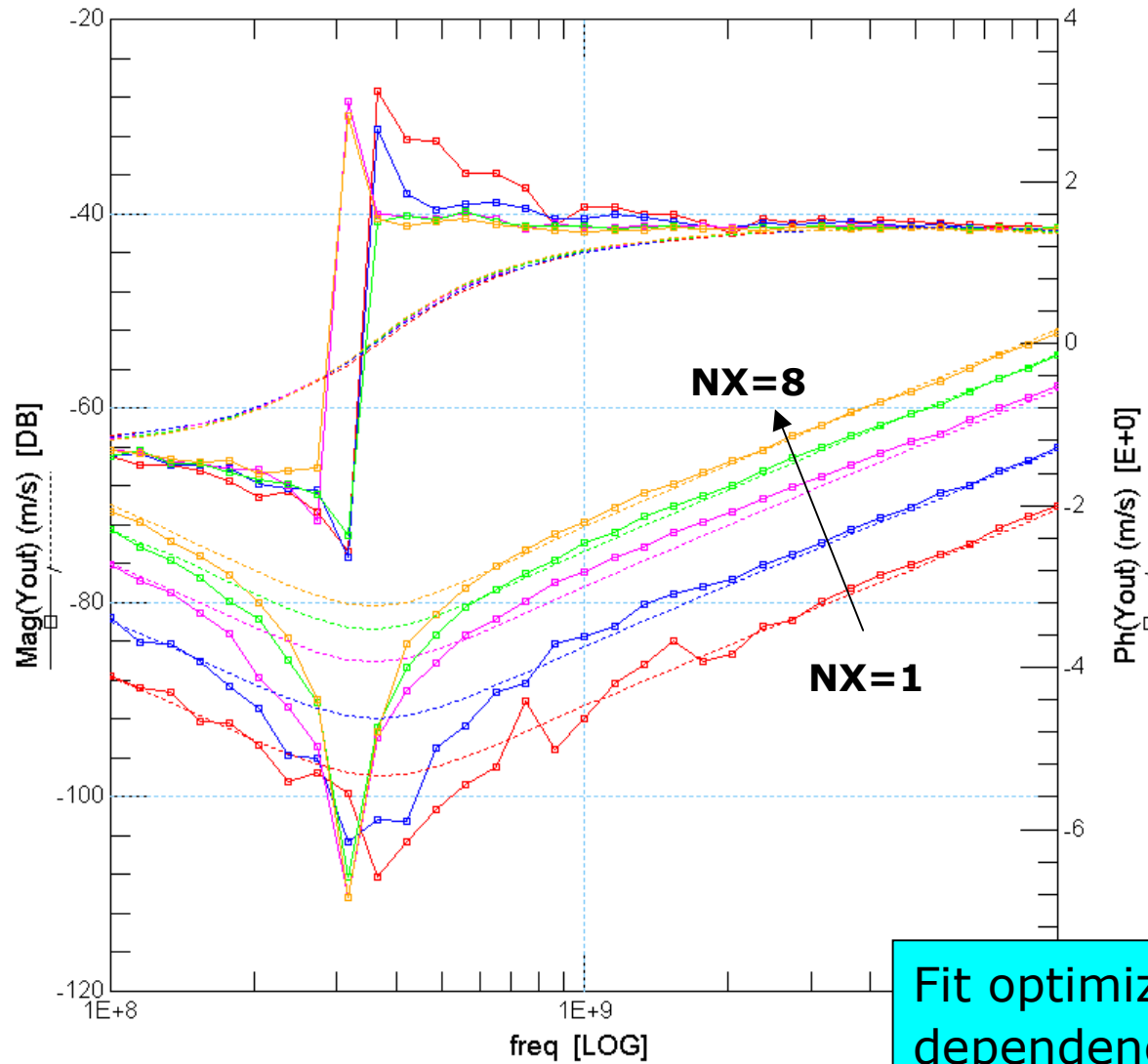


**Size: emitter number scaling -  
 BEC layout**

$A_{\text{Emitter}} = NX \times 0.3 \times 0.92 \mu\text{m}^2$   
 $cth = 2.25 \cdot 10^{-12} \cdot NX \text{ J/K}$   
 $r_{th} = 6498 \cdot NX^{-0.85} \text{ K/W}$   
 $\rightarrow$   
 $\tau_{TH} = 14.6 \cdot NX^{0.15} \text{ ns}$

Fit optimization implies a linear dependence of cth on emitter number and  $\tau_{TH} \sim NX^{0.15}$ .

# SG25H1 - HS-B ( $f_T=180\text{GHz}$ )

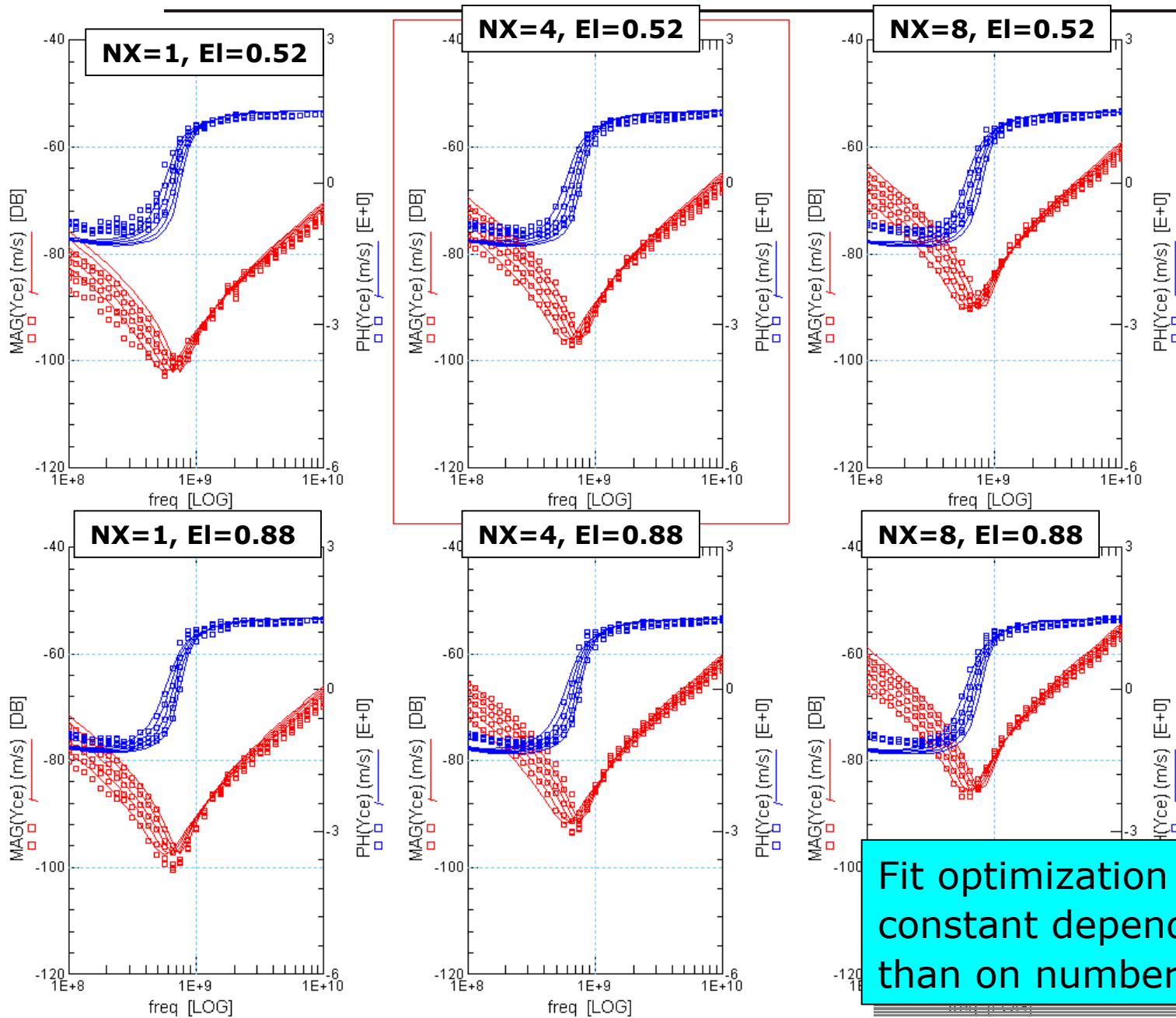


$V_{CE} = 1.5\text{V}$ ,  
 $V_{BE} = 0.91\text{V}$   
 peak- $f_T$  @  $V_{BE} = 0.91\text{V}$

Size: emitter number scaling -  
 BEC layout  
 $A_{\text{Emitter}} = NX \times 0.26 \times 0.92 \mu\text{m}^2$   
 $c_{th} = 1.4 \cdot 10^{-12} \cdot NX \text{ J/K}$   
 $r_{th} = 7430 \cdot NX^{-0.8} \text{ K/W}$   
 $\rightarrow$   
 $\tau_{TH} = 10 \cdot NX^{0.2} \text{ ns}$

Fit optimization implies a linear dependence of  $c_{th}$  on emitter number and  $\tau_{TH} \sim NX^{0.2}$ .

# SG13 – HS-BEC ( $f_T=250\text{GHz}$ )



$V_{CE} = 1.2\text{V}$ ,  
 $V_{BE} = 0.90(0.01)0.94\text{V}$   
 peak- $f_T$  @  $V_{BE} = 0.94\text{V}$

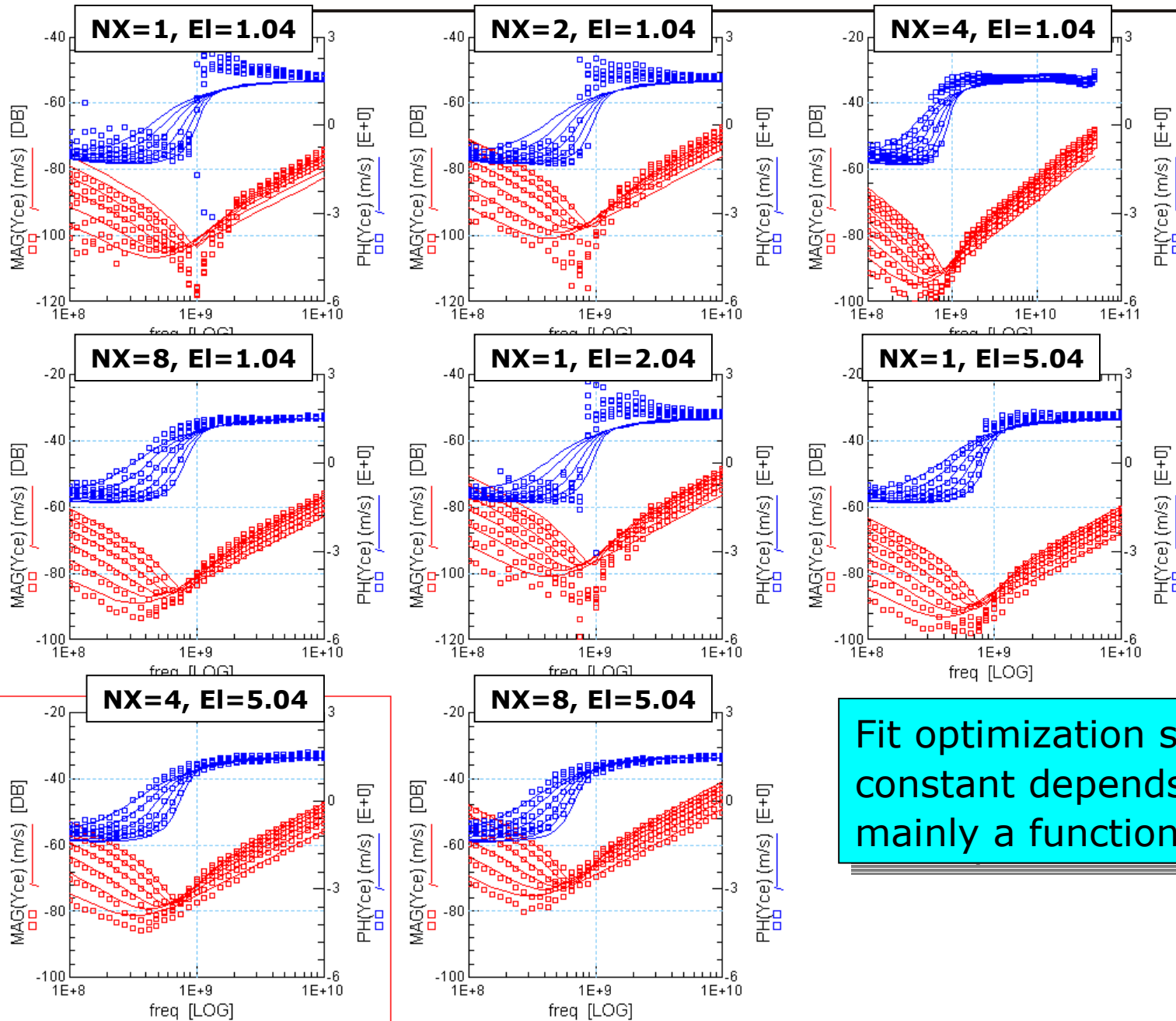
**Size: emitter number + length**  
**scaling – BEC layout**  
 $A_{\text{Emitter}} = NX \times 0.16 \times EI \mu\text{m}^2$   
 $cth = 0.50 \cdot 10^{-12} \cdot NX^{1.0} \cdot EI^{1.1} \text{ J/K}$   
 $r_{th} = 8602 \cdot NX^{-0.9} \cdot EI^{-0.9} \text{ K/W}$   
 $\rightarrow$   
 $\tau_{TH} = 4.3 \cdot NX^{0.1} \cdot EI^{0.2} \text{ ns}$

Fit optimization shows that thermal time constant depends more on emitter length than on number scaling.





# SG13 – HS-CBEBC ( $f_T = 250\text{GHz}$ )



$V_{CE} = 1.2\text{V}$ ,  
 $V_{BE} = 0.84(0.02)0.94\text{V}$   
peak- $f_T$  @  $V_{BE} = 0.94\text{V}$

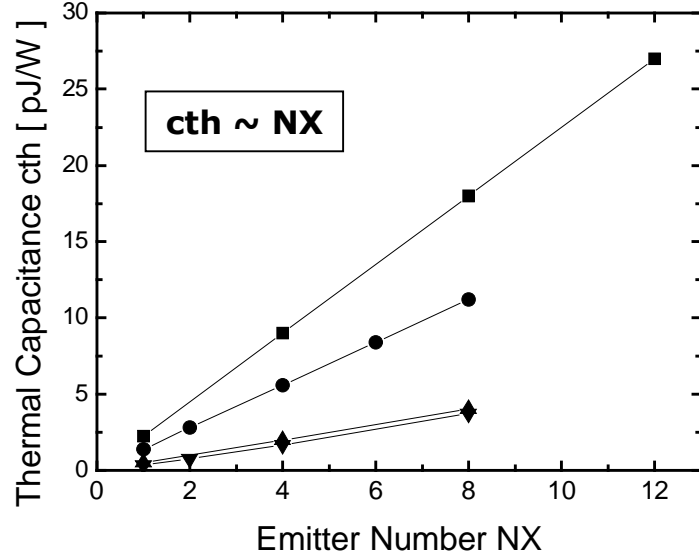
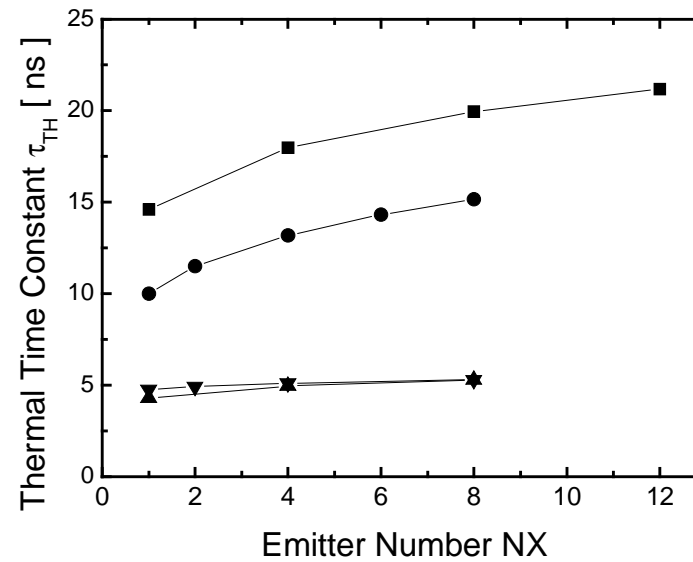
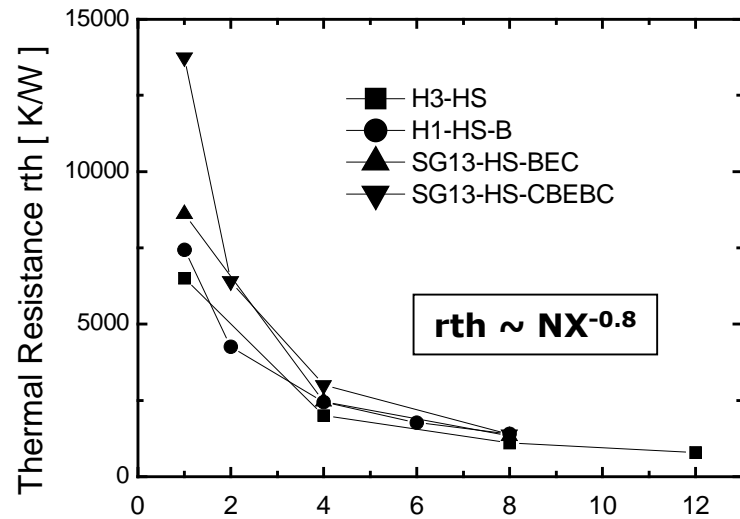
Size: emitter number + length  
scaling – CBEBC layout

$A_{\text{Emitter}} = NX \times 0.16 \times EI \mu\text{m}^2$   
 $cth = 0.34 \cdot 10^{-12} \cdot NX^{1.15} \cdot EI^{1.1} \text{ J/K}$   
 $rth = 13750 \cdot NX^{-1.1} \cdot EI^{-0.8} \text{ K/W}$

→  
 $\tau_{TH} = 4.76 \cdot NX^{0.05} \cdot EI^{0.3} \text{ ns}$

Fit optimization shows that thermal time constant depends weakly on NX and is mainly a function of emitter length.

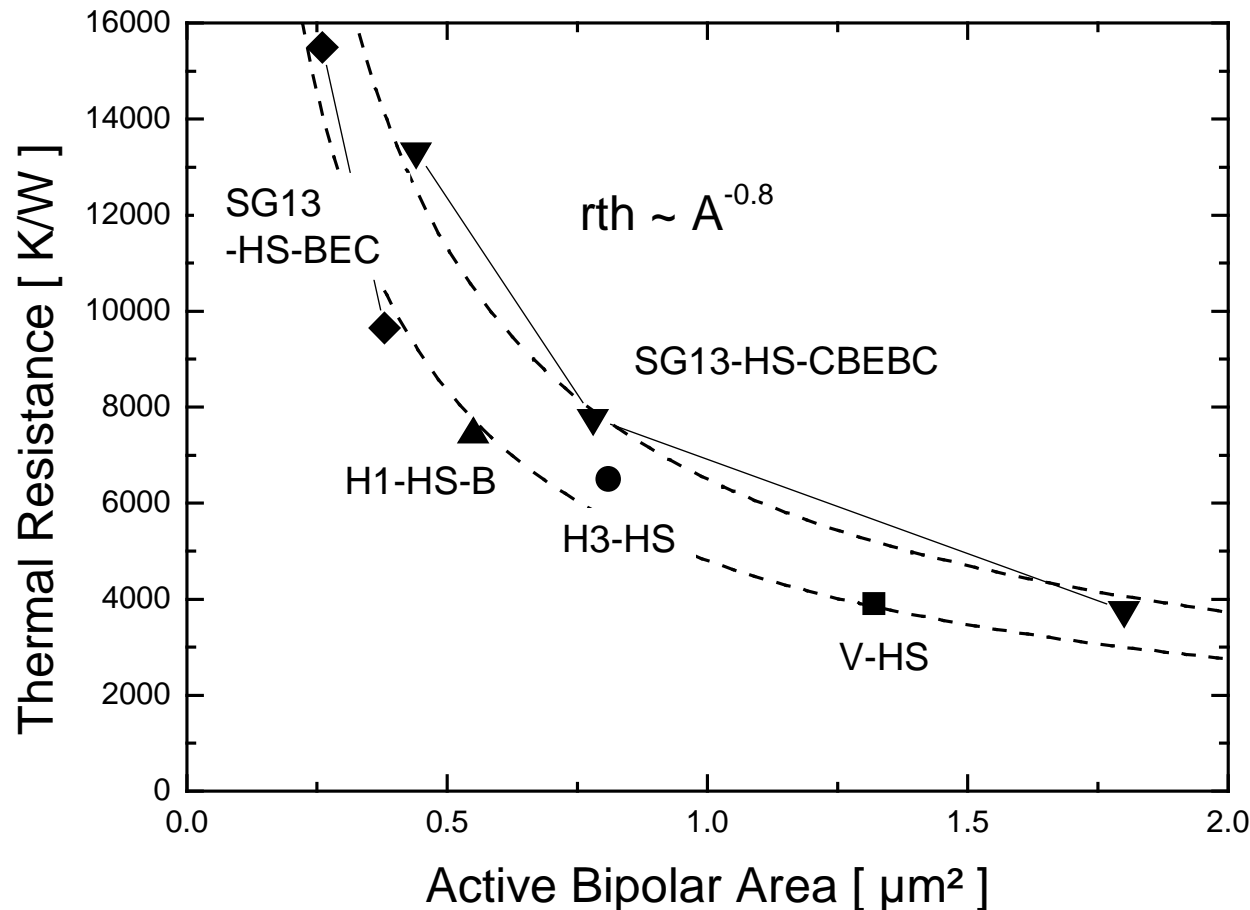
# $\tau_{TH}$ as Function of Emitter Number NX



There is a slight dependence of the thermal time constant on NX:

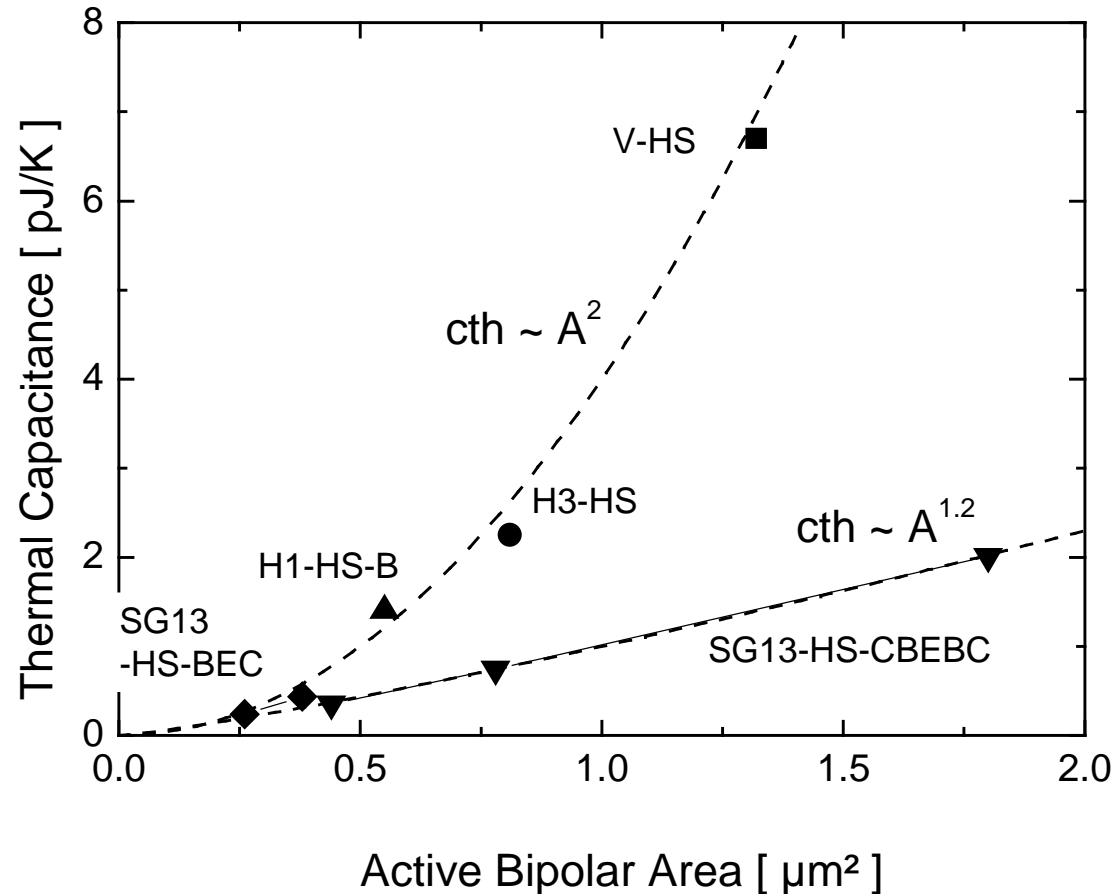
$$\tau_{TH} \sim NX^{0.1}$$

# rth as Function of Active Bipolar Area



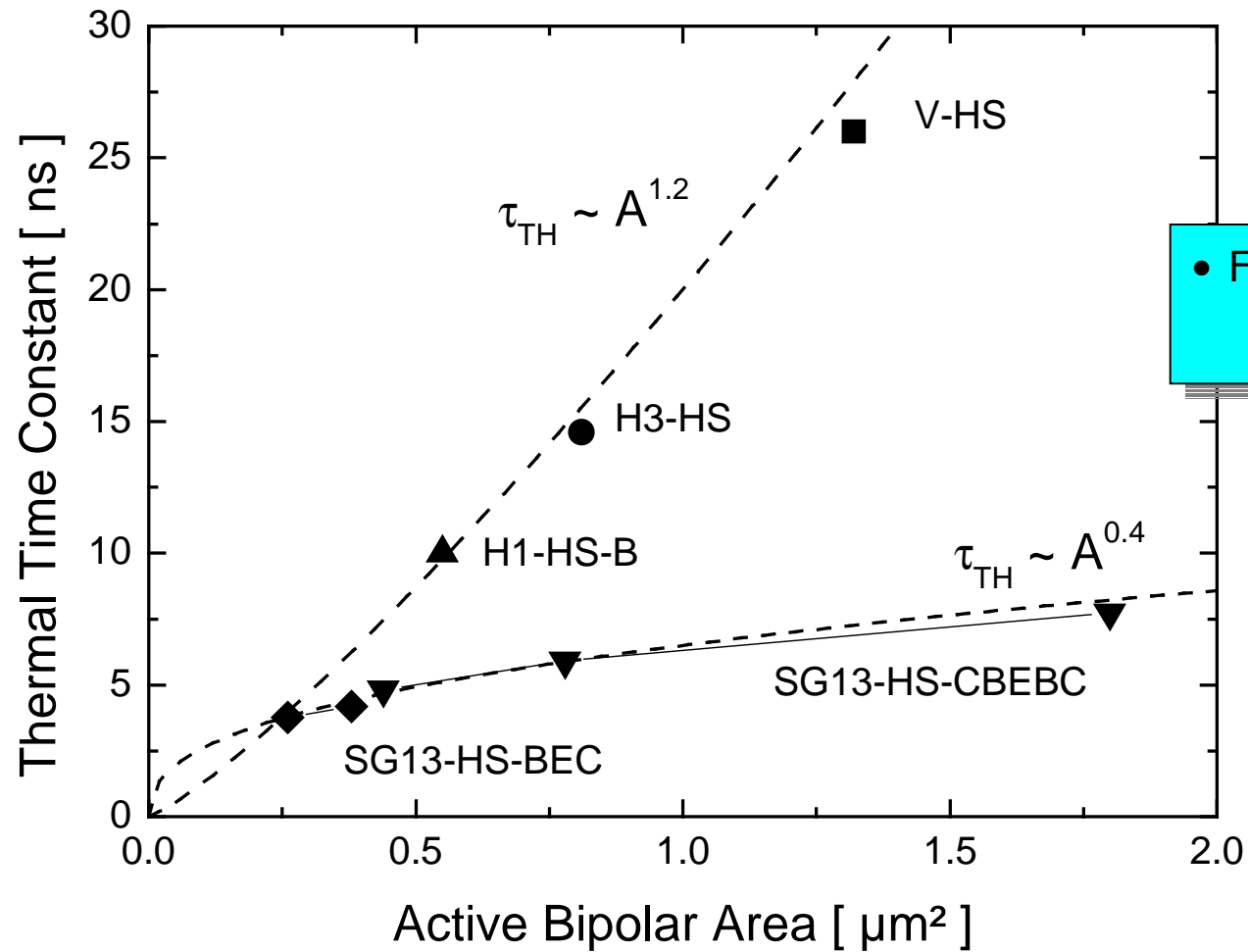
- A  $r_{th} \sim A^{-0.8}$  was usually assumed for IHP scaled models (like for SG13-HS-CBEBC).
- The comparison here shows that it is also valid "inter"-technology.
- The pre-factor depends on the layout type.

# cth as Function of Active Bipolar Area



- Simulations of cth by a customer predicted:  $cth \sim A^2$ .
- For BEC this fits well to the current "inter"-technology results.

# $\tau_{TH}$ as Function of Active Bipolar Area



• Finally, one gets for BEC  
 $\tau_{TH} \sim A^{1.2}$

# Summary

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- Presented a simple extraction of  $c_{th}$  for HS-HBTs by modeling  $Y_{out}$  in the low frequency range of a standard 50 MHz - 50 GHz NWA.
- Thermal time constant is a function of active bipolar area size and scales  $\sim A^{1.2}$  for BEC configuration. For CBEBC a lower rise  $\sim A^{0.4}$  has been observed.