

EUROPEAN MICROWAVE WEEK 2015

SIX DAYS • THREE CONFERENCES • ONE EXHIBITION

PALAIS DES CONGRÈS, PARIS, FRANCE
SEPTEMBER 6 - 11, 2015

Exhibition Opening Hours:

- Tuesday 8th September: 9.30 – 18.00
- Wednesday 9th September: 9.30 – 17.30
- Thursday 10th September: 9.30 – 16.30

Impact of physical effects and compact modeling on mm-wave circuit performance

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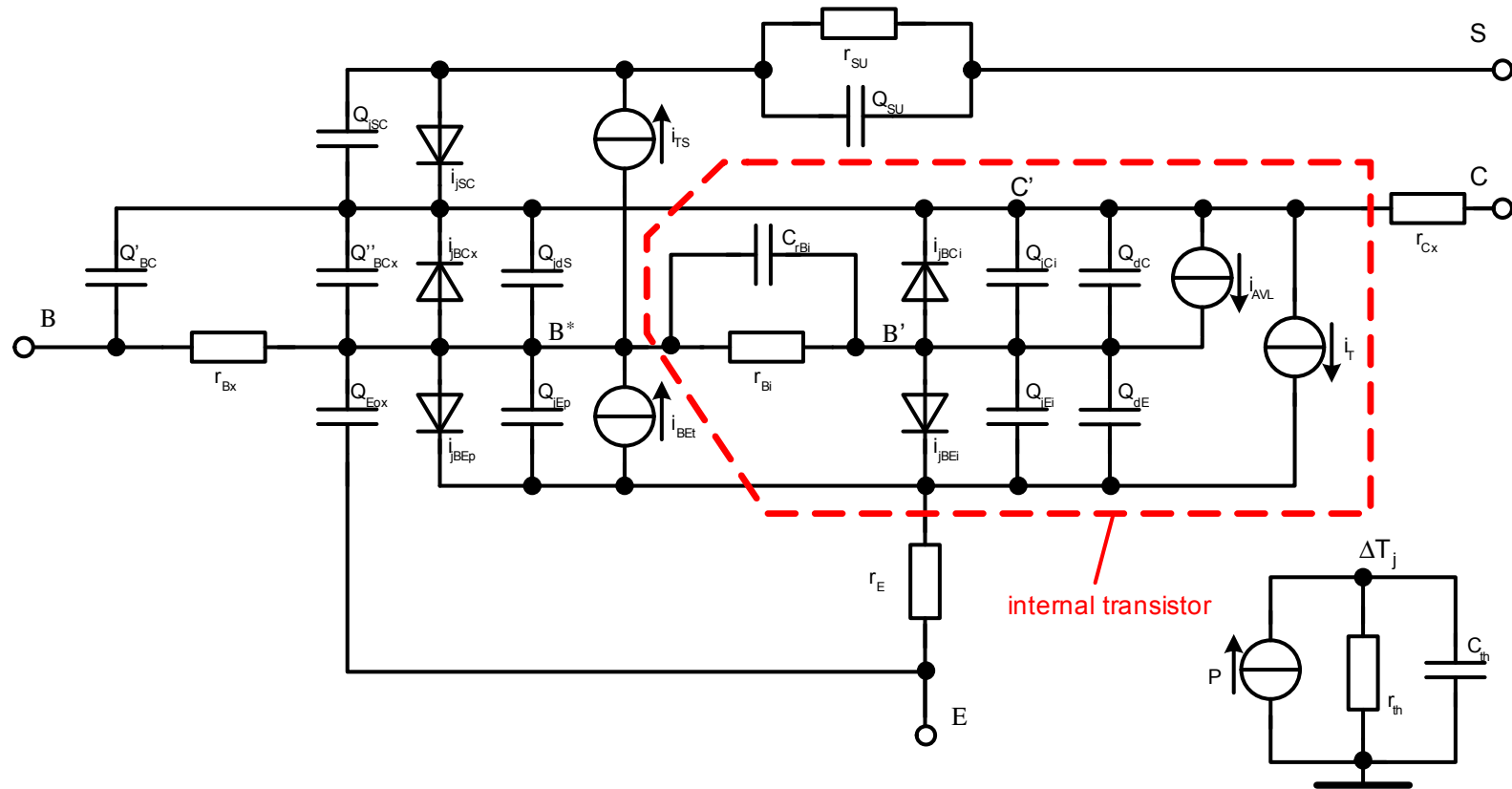
WS12: EuMIC - SiGe for mm-Wave and THz

Goals of the workshop

- Understanding of the basic concepts of HICUM/L2
 - core components and equations
 - equivalent circuit
 - transfer current
 - minority charges
- Impact of physical effects on circuit performance
 - focus on a few important effects
 - application example 1 - PA (numerical device simulation)
 - application example 2 - PA (realistic design)

HICUM/L2

- Physics-based compact model for bipolar transistors
 - including HBT related features
 - supported by CMC
 - available in all commercial circuit simulators



Transfer current - GICCR

- 1D transport equation of electrons => npn transistor
- similar derivation of hole current of pnp transistor

$$J_n = q\mu_n \left[V_T \frac{dn}{dx} + nE \right] = q\mu_n \frac{d\phi_n}{dx}$$

(ϕ_n => quasifermi-potential of electrons)

- rewritten for transfer current

$$I_T = \frac{qA_E V_T \overline{\mu_{nr} n_{ir}^2}}{\int h(x)p(x)dx} \left[\exp\left(\frac{V_{B'E'}}{V_T}\right) - \exp\left(\frac{V_{B'C'}}{V_T}\right) \right]$$

=> weighted hole charge

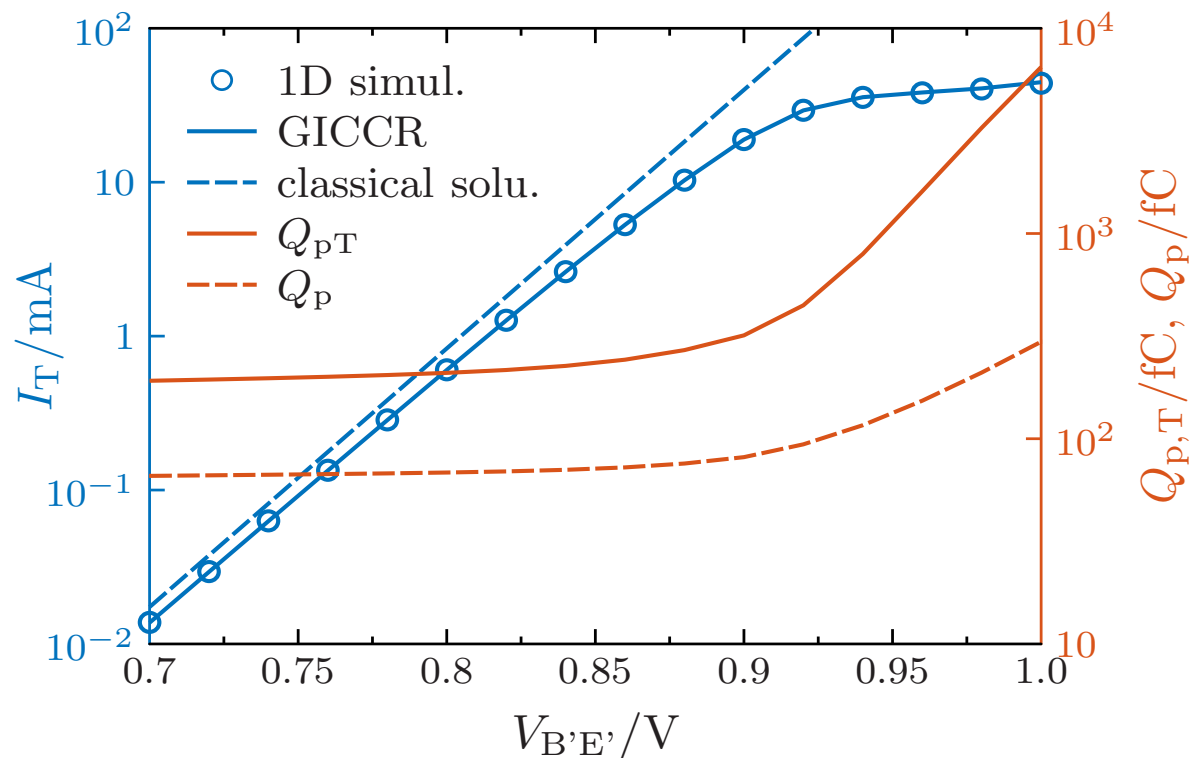
$$Q_{p,T} = q \int h(x)p(x)dx = q \int \frac{\overline{\mu_{nr} n_{ir}^2}}{\mu_n(x) n_i^2(x)} p(x)dx$$

Weighted Hole Charge

- Calculation of the transfer current by using charges

$$Q_{p,T} = Q_{p0} + h_{jEi}Q_{jEi} + h_{jCi}Q_{jCi} + h_{f0}i_{Tf}\tau_{f0} + h_{fE}Q_{Ef} + Q_{Bf} + h_{fC}Q_{pC}$$

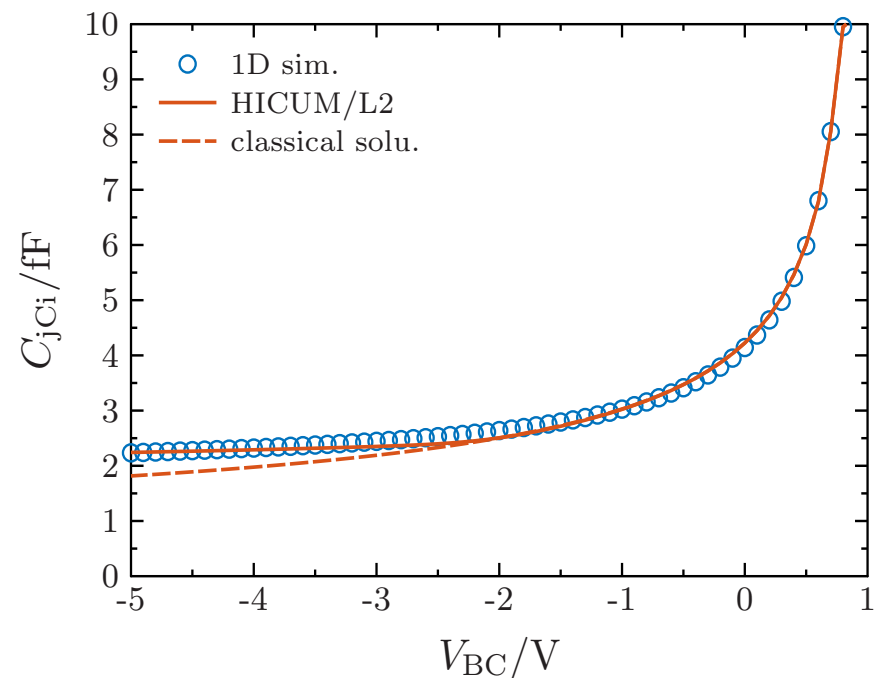
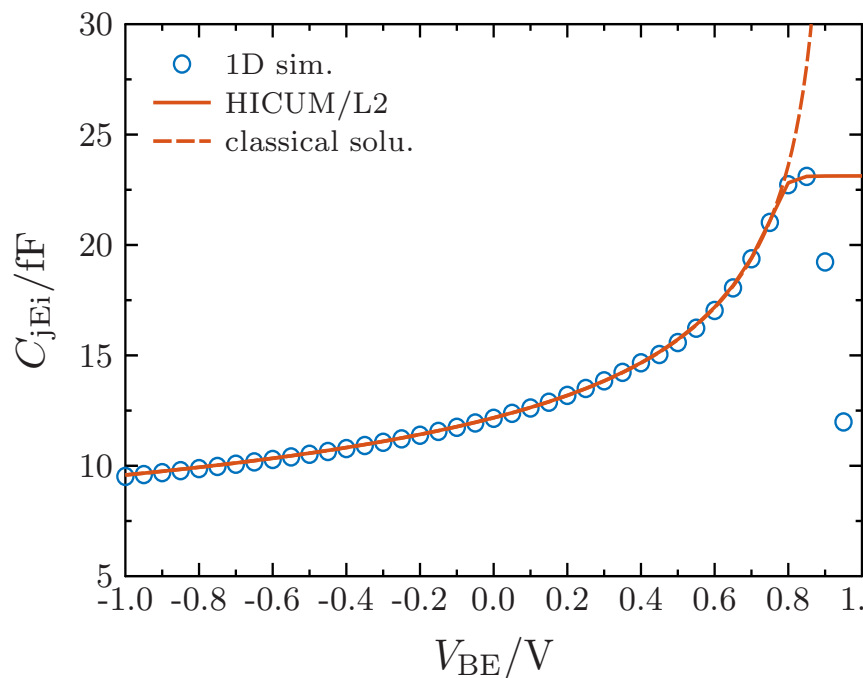
=> separately measured quantities



Charge Modeling

Depletion charges

- Two different models available
 - variable limit of maximum capacitance value => $C_{jE(i,p)}$
 - punch-through effect => $C_{jC(i,x)}$, C_{jS}



Charge Modeling

Mobile charges

- Low and high current component

$$\tau_f = \tau_{f0} + \Delta\tau_f$$

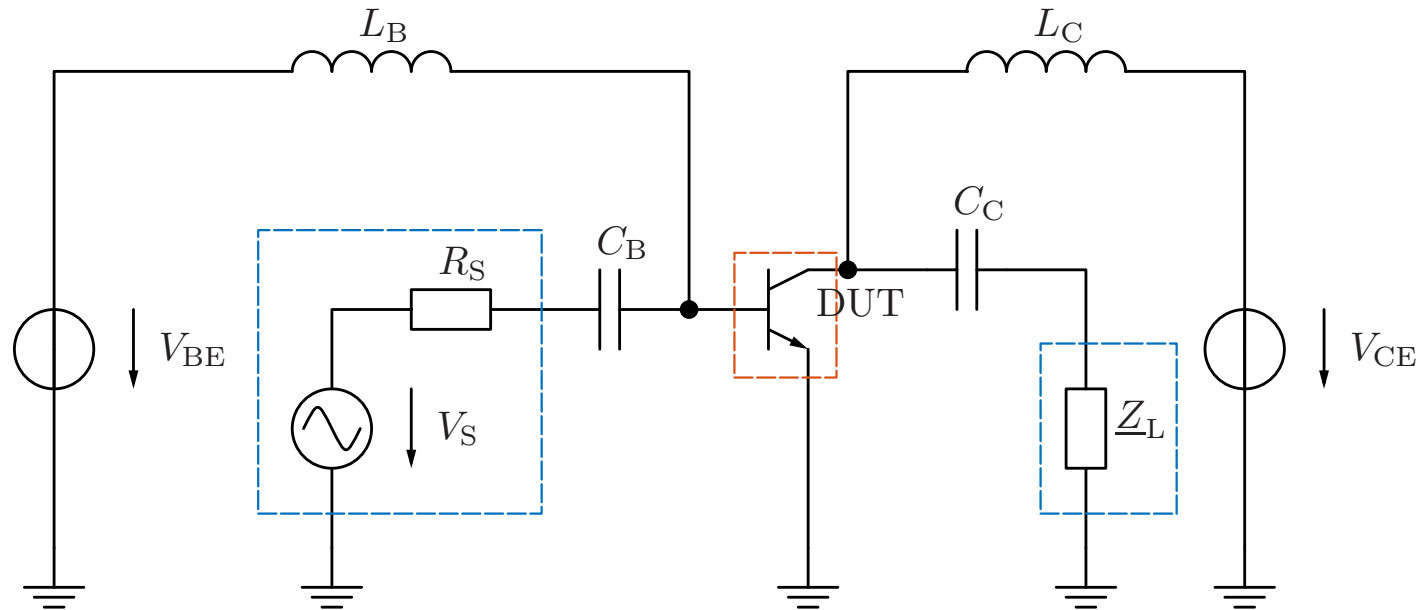
- Low current component including:
 - base width modulation => decrease of τ_f with V_{CB}
 - finite carrier velocity in BC-SCR => increase of τ_f with V_{CB}
- High current component including:
 - weak transit time increase at medium current densities => $f_{T,peak}$
 - strong charge increase due to Kirk-effect and BC-barrier term
- Version 2.30 released in 2011, actual version 2.33
 - version 2.34 to be released in 2015

HICUM/L2 Version 2.3x

- Main changes
 - bandgap effects on transfer current
 - improved knee-current modeling (by physics-based weight factors)
 - improved temperature models of the transfer current
 - BC-barrier term
 - temperature dependent thermal resistance

Application Example 1 - PA

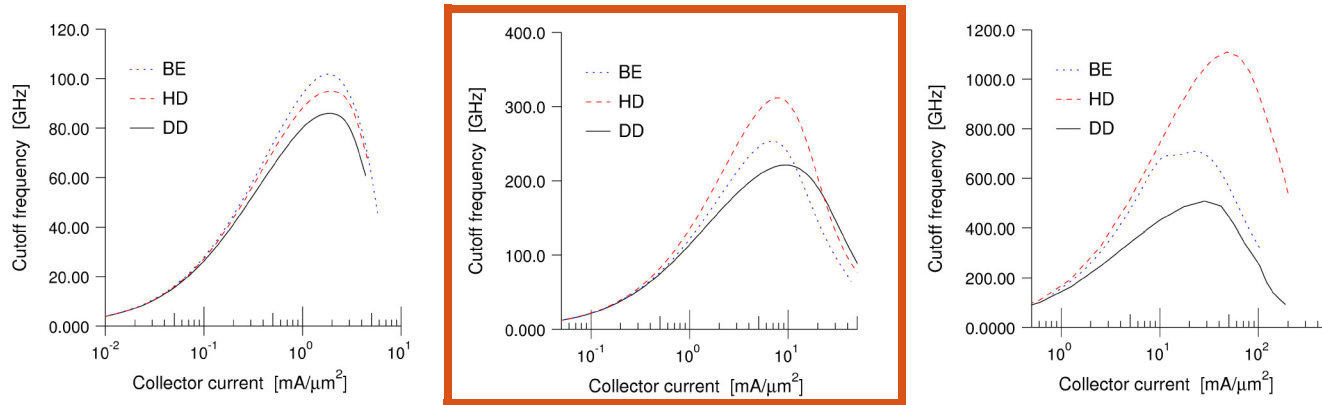
- Simple PA circuit with power source and load impedance



transistor **DUT** simulated as
numerical 1D device
compact model HICUM/L2

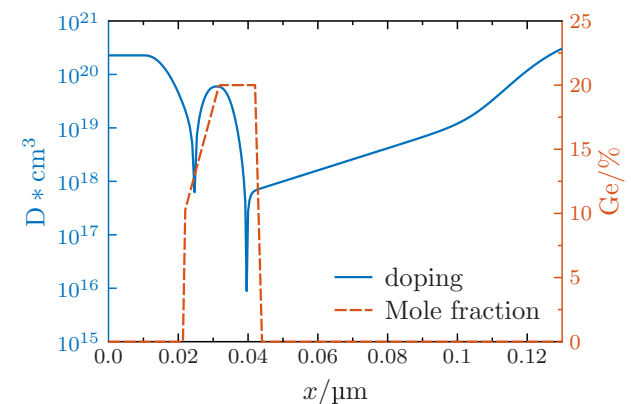
Numerical 1D Transistor

- Drift-Diffusion simulation for profile with $f_T=250$ GHz



=> limits of DD model

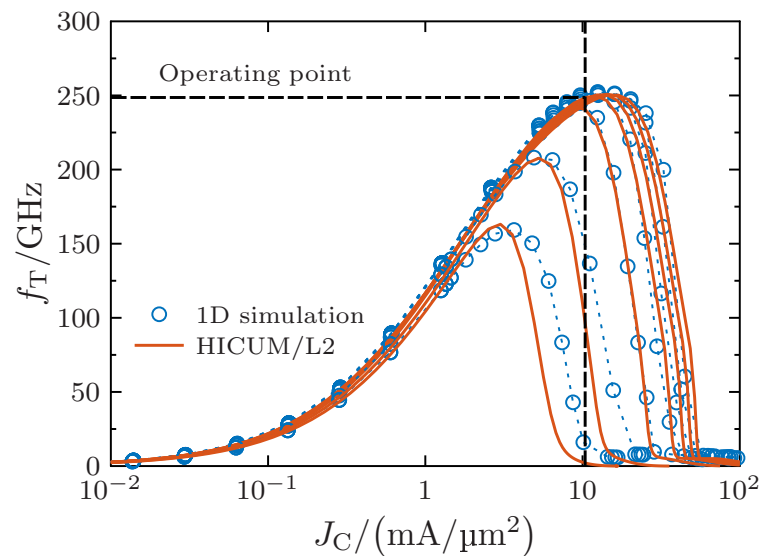
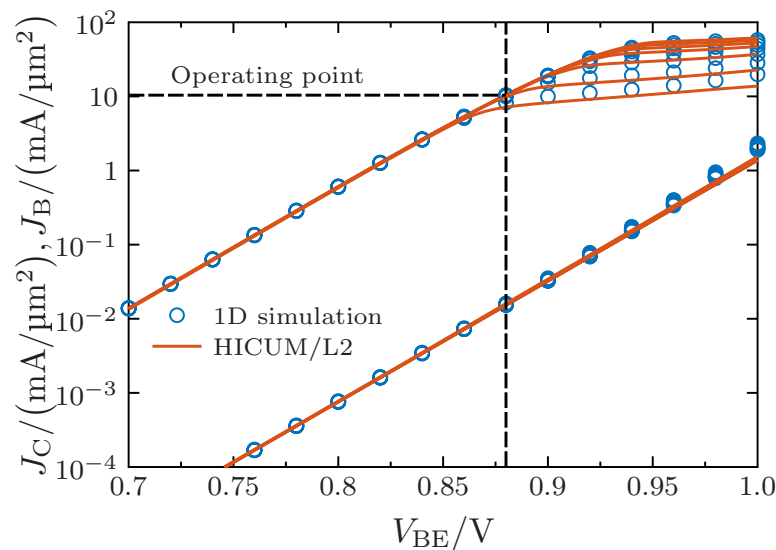
length of internal transistor: 130 nm
 base width: 15 nm
 internal collector width: 70 nm
 maximum base doping: $6 \cdot 10^{19} \text{ cm}^{-3}$
 $J_C @ f_{T,\text{peak}}$: $10 \text{ mA}/\mu\text{m}^2$
 $B_{VCE0} @ V_{BE}=0.7 \text{ V}$: 1.5 V



[S.-M. Hong, C. Jungemann, "Electron transport in extremely scaled SiGe HBTs," BCTM 2009, S. 67-74.]

HICUM/L2 Model

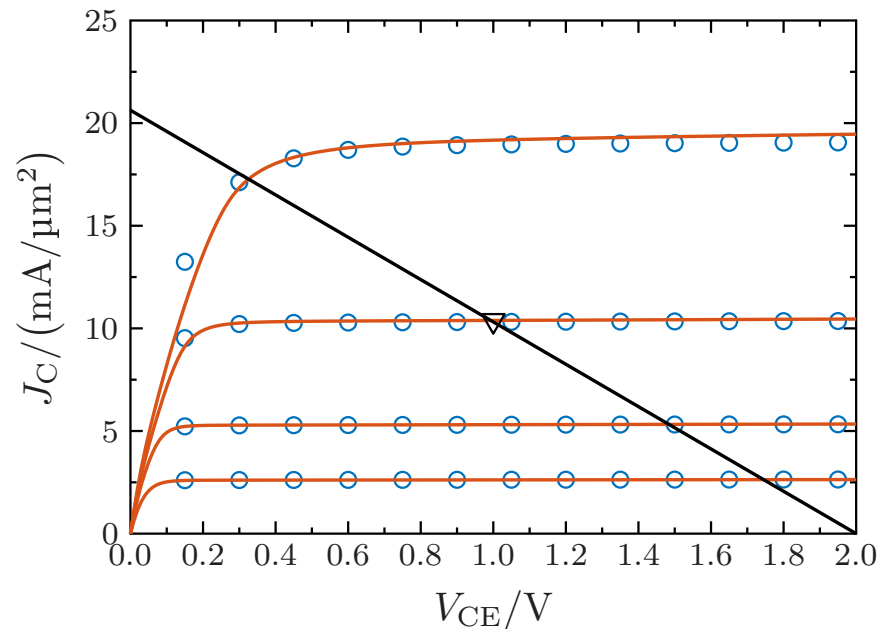
- Usage of latest available version
- extraction based on standard characteristics (DC, small signal AC)



- extraction of all parameter corresponding to 1D transistor

Power Amplifier

- Operating point close to $f_T \Rightarrow$ strong impact of high current effects



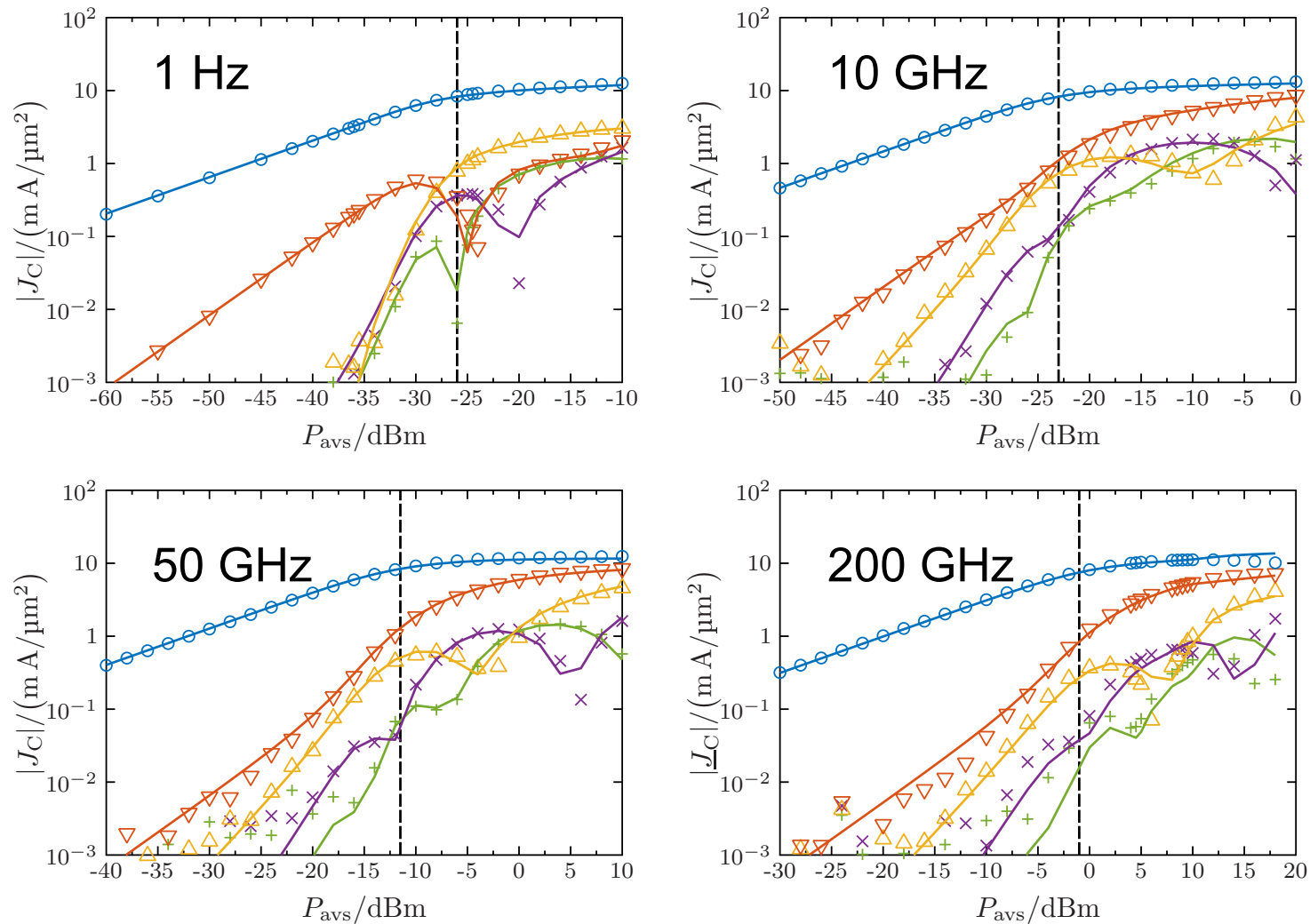
- 1D transistor used with $A_E = 1 \mu m^2 \Rightarrow$ Load resistance: $R_S = 100 \Omega$
close to $50 \Omega \Rightarrow$ realistic environment
- Focus on harmonic distortion

Simulation

- for numerical 1D simulations, only transient simulation possible
- transformation into frequency domain
- Fundamental frequencies
 - 1 Hz: no impact of dynamic currents => verification of static current
 - 10 GHz: quasi-static behavior => verification of charges
 - 50 GHz: 5th harmonic at peak f_T => starting influence of NQS effects
 - 200 GHz: close to peak f_T => 5th harmonic at 1 THz
- Focus on output power in frequency domain

Output Current

Frequency domain results



Nonlinear Modeling

- Accurate non-linear large-signal modeling with HICUM/L2
 - up to very high frequencies far beyond $f_{T,peak}$

=> Which physical effects are significant?

- Discussed here:

High-current effects

- compression at high input power

=> saturation

=> transfer current modeling

- high-current effects in charges due to strong increase of carriers

=> impact on I_C (via $Q_{p,T}$)

=> impact on Q_f

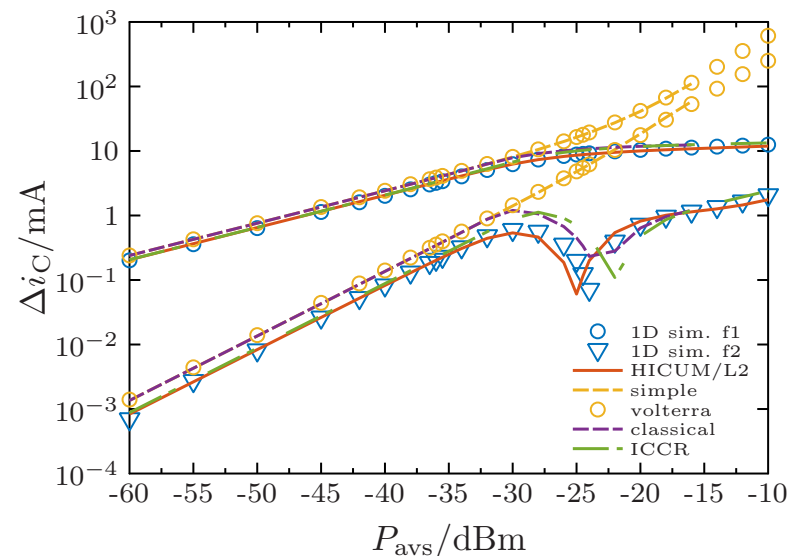
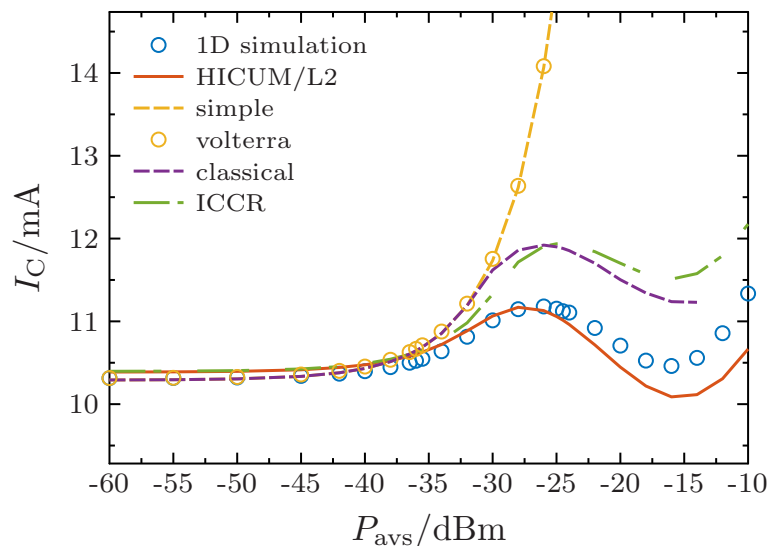
Compression (1 Hz)

- Transfer current modeled by:

simple equation: $I_T = I_S \exp\left(\frac{V_{BE}}{V_T}\right)$ (no saturation, no BC current)

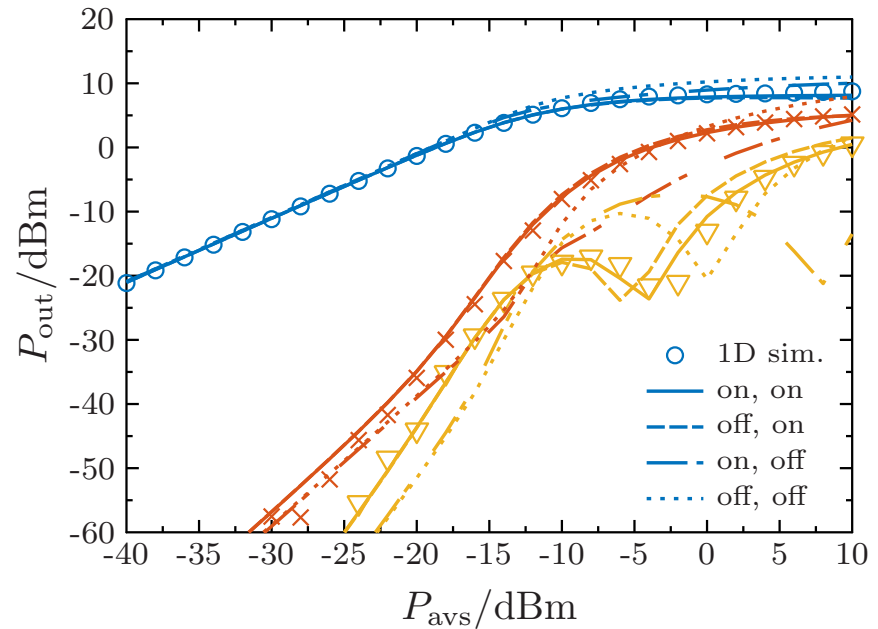
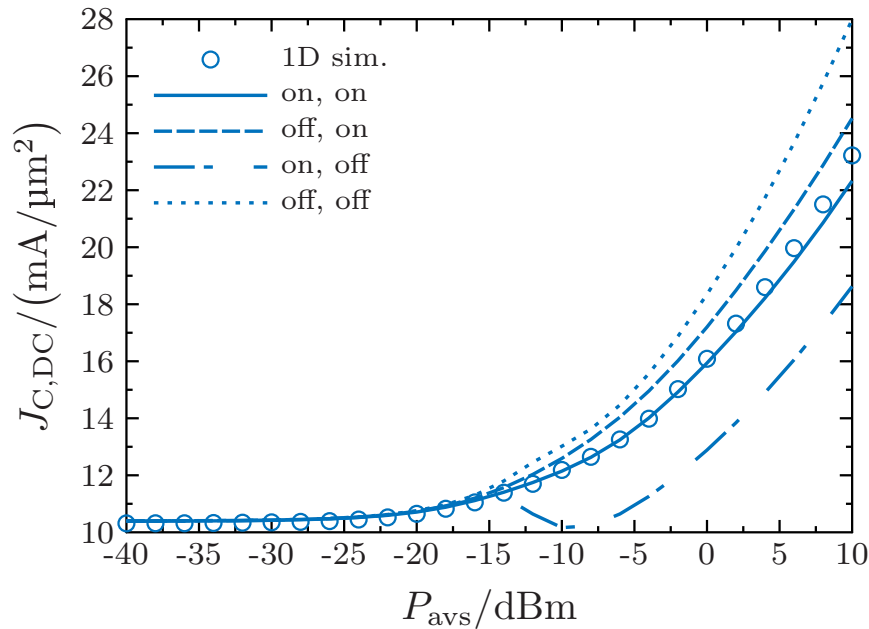
classical equation: $I_T = I_S \left[\exp\left(\frac{V_{BE}}{V_T}\right) - \exp\left(\frac{V_{BC}}{V_T}\right) \right]$ (saturation, const. I_S)

ICCR: $Q_{p,T} = Q_{p0} + Q_{j,T} + h_{f0} i_{Tf} \tau_{f0}$ (no high-current effects on I_T)



High-Current Effects (50 GHz)

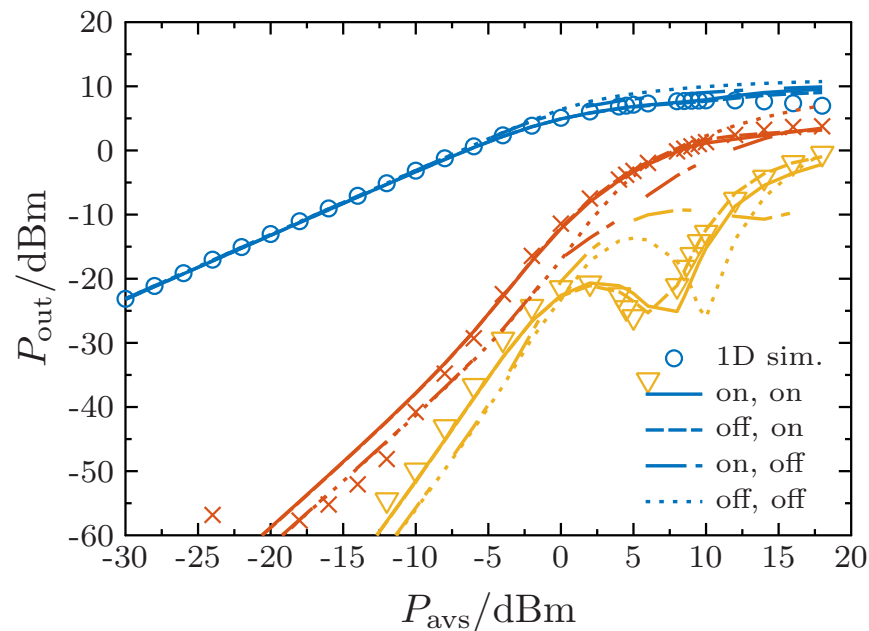
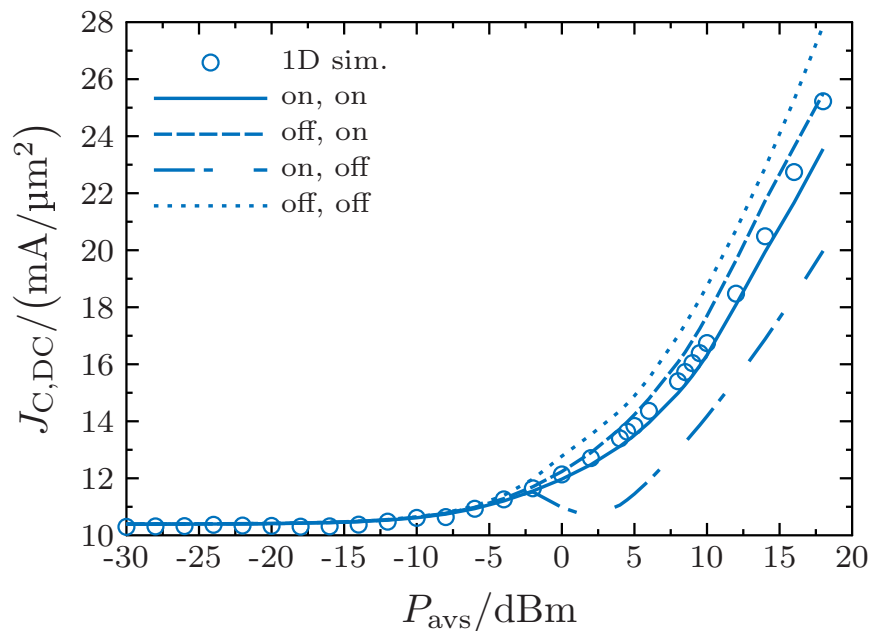
- Legend here: high current effects in $Q_{p,T} \Rightarrow I_C, Q_p$



=> accurate charge modeling required

High-Current Effects (200 GHz)

- Second and third harmonic above $f_{T,peak}$

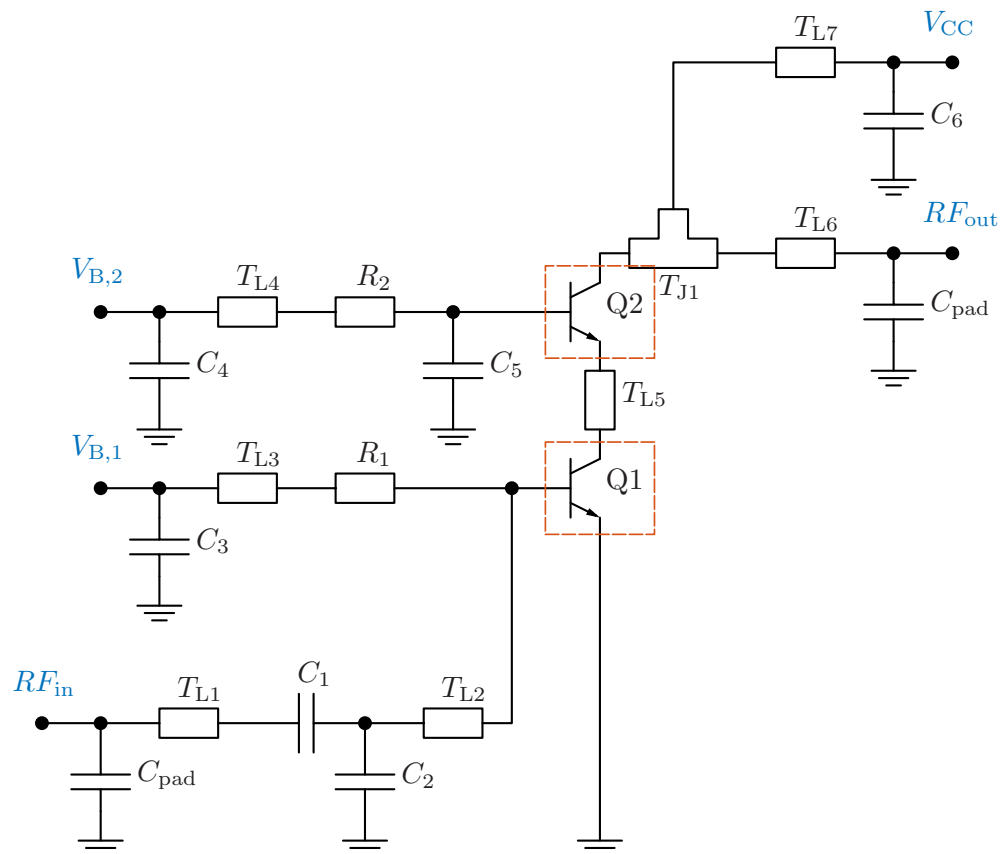


=> similar results to 50 GHz

even more emphasize on the charge due to high frequencies

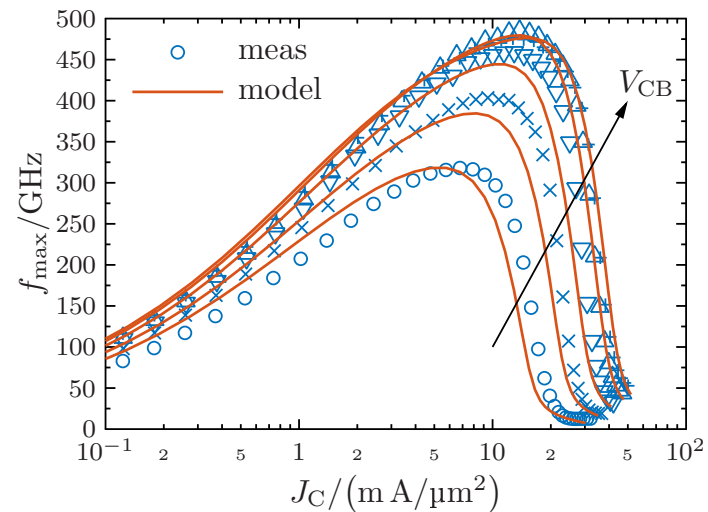
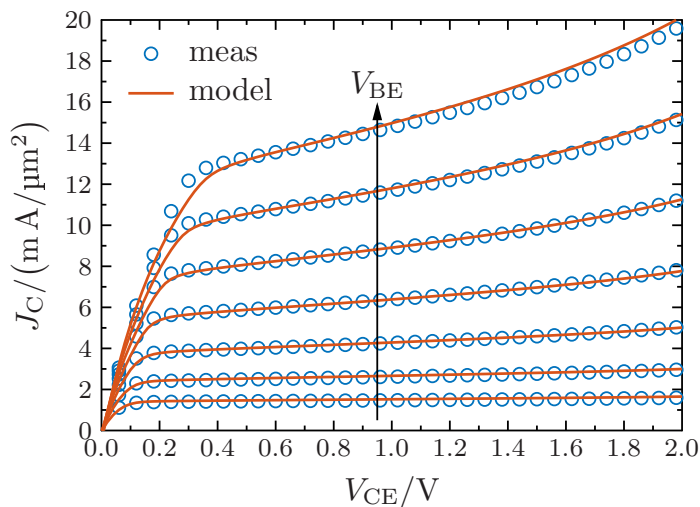
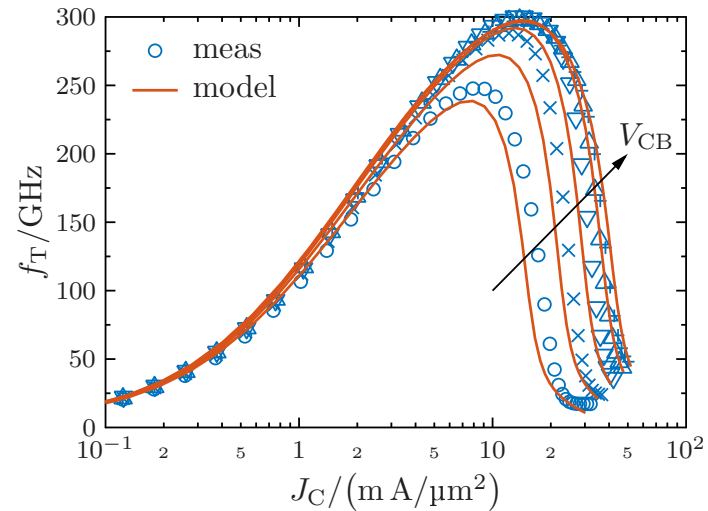
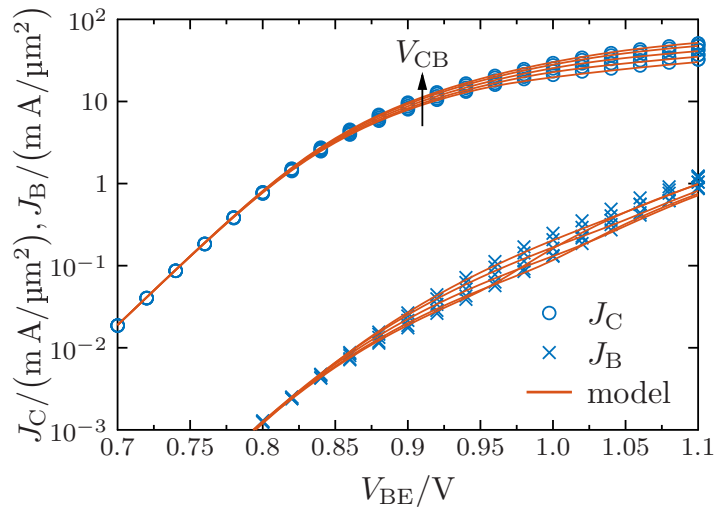
Application Example 2 – 2-stacked PA

- Circuit designed in IHPs SG13G2 technology
 - transistors with $f_{T,peak}=300$ GHz and $f_{max,peak}=500$ GHz
 - cascode connection to increase available voltage swing
 - transistors biased at $V_{BE}=0.91$ V
 $V_{CE}=1.1$ V
- $\Rightarrow$ close to $f_{T,peak}$
- operating frequency: 94 GHz



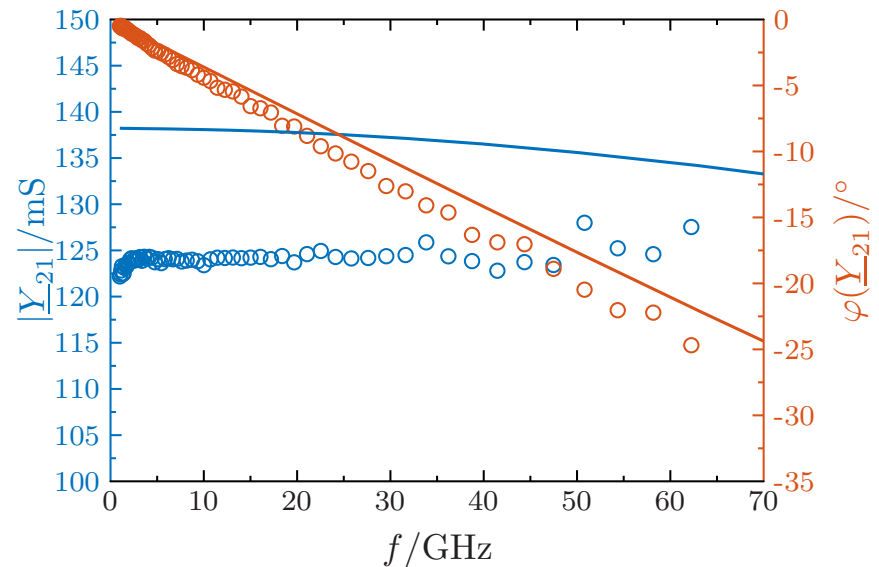
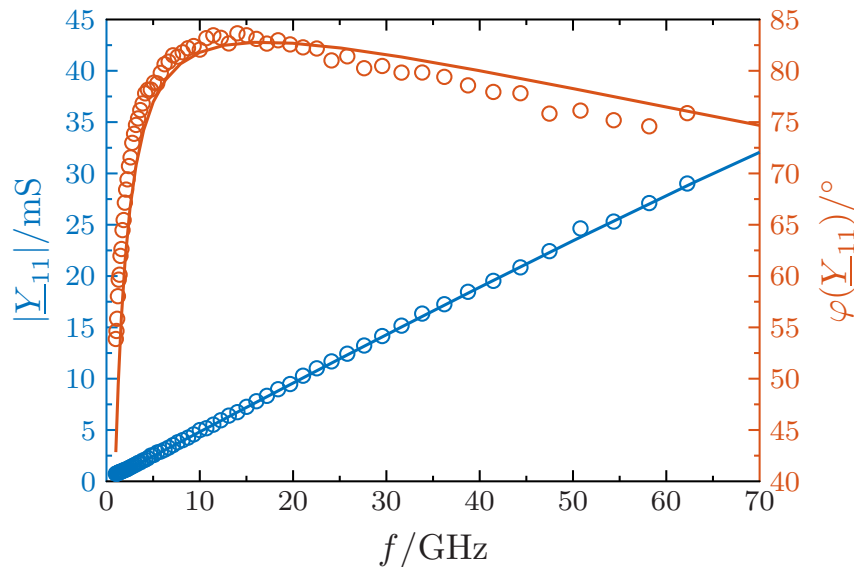
Experimental results - transistor

Linear modeling (selected results)



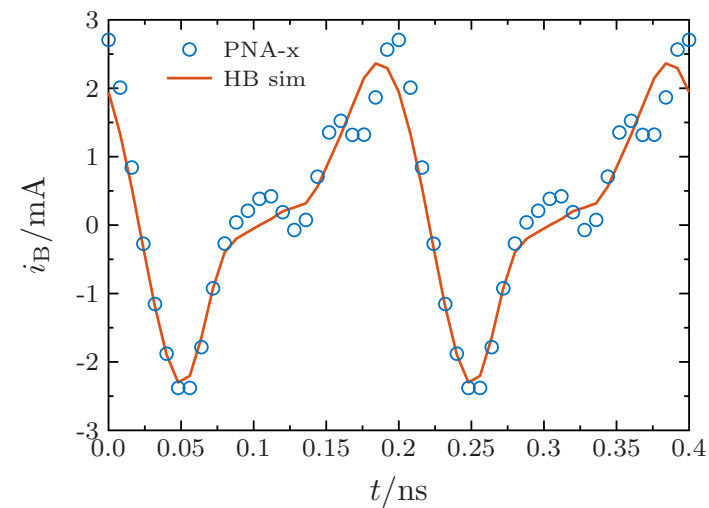
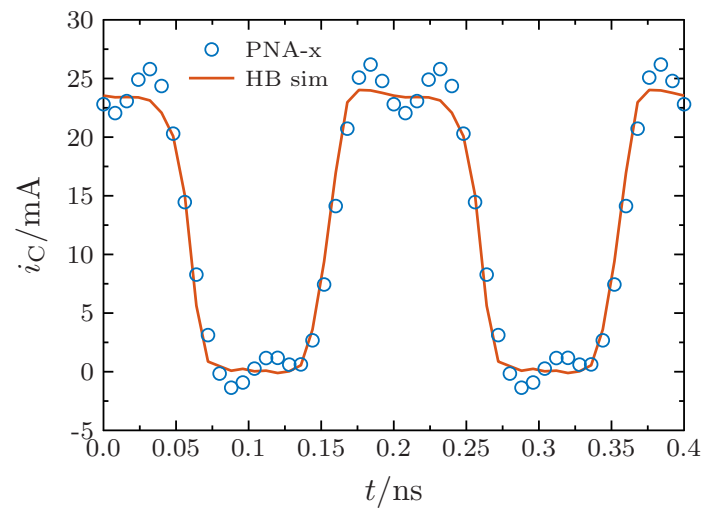
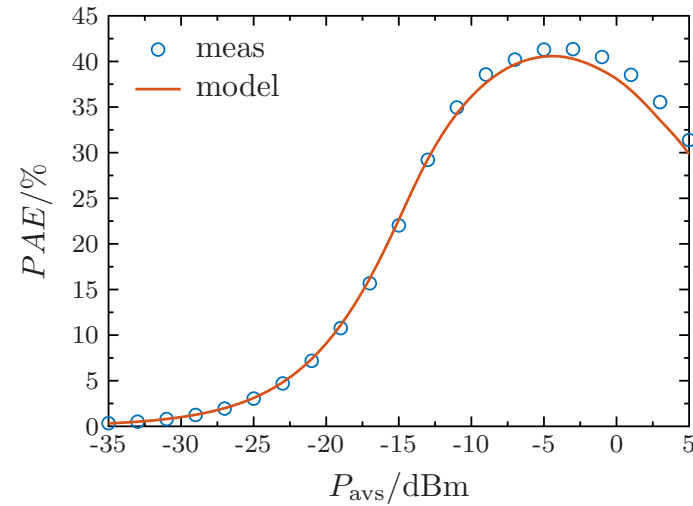
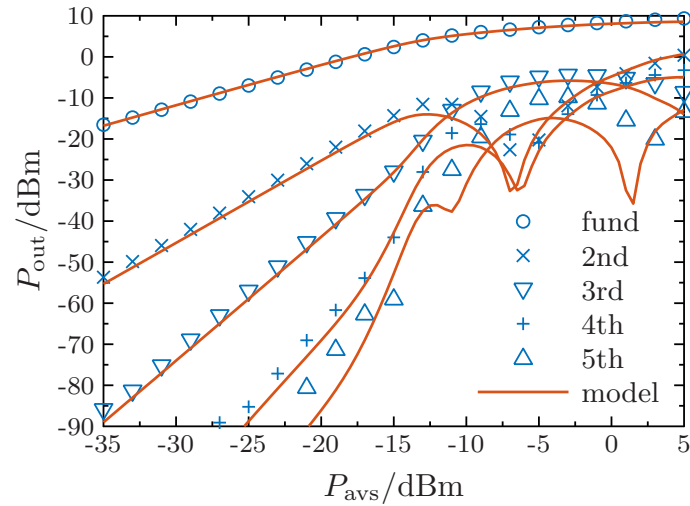
Experimental results - transistor

Small-signal ($V_{BE}=0.9$ V, $V_{CB}=0.3$ V)



Experimental results - transistor

Large-signal ($V_{BE}=0.875$ V, $V_{CE}=1$ V, $f_0=5$ GHz, $P_{avs}=-5$ dBm)



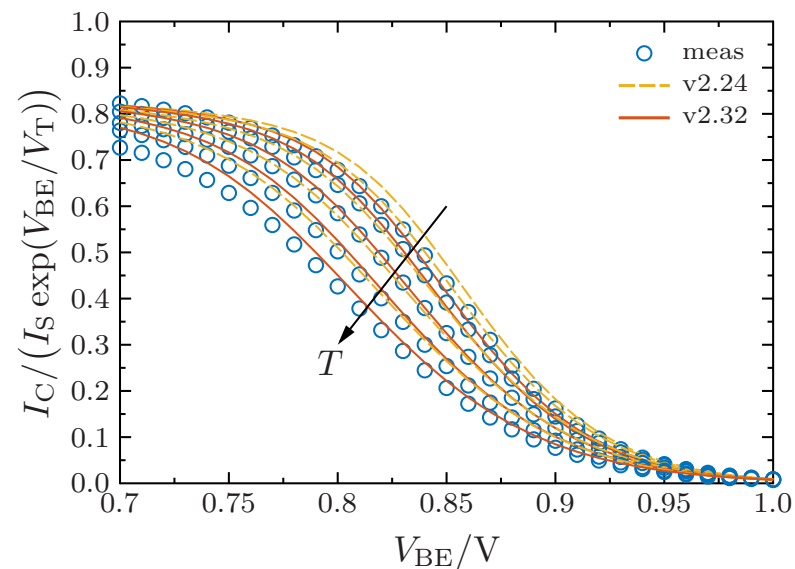
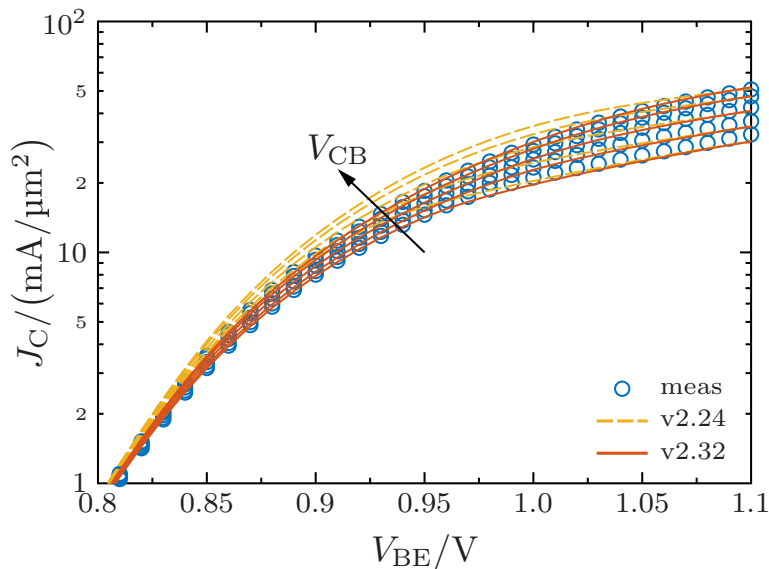
HICUM/L2 Version 2.2x version 2.3x

- Improved modeling of the transfer current
 - weight factor h_{f0} for medium injection => knee-current modeling

$$Q_{p,T} = Q_{p0} + h_{jEi} Q_{jEi} + h_{jCi} Q_{jCi} + h_{f0} i_{Tf} \tau_{f0} + h_{fE} Q_{Ef} + Q_{Bf} + h_{fC} Q_{pC}$$

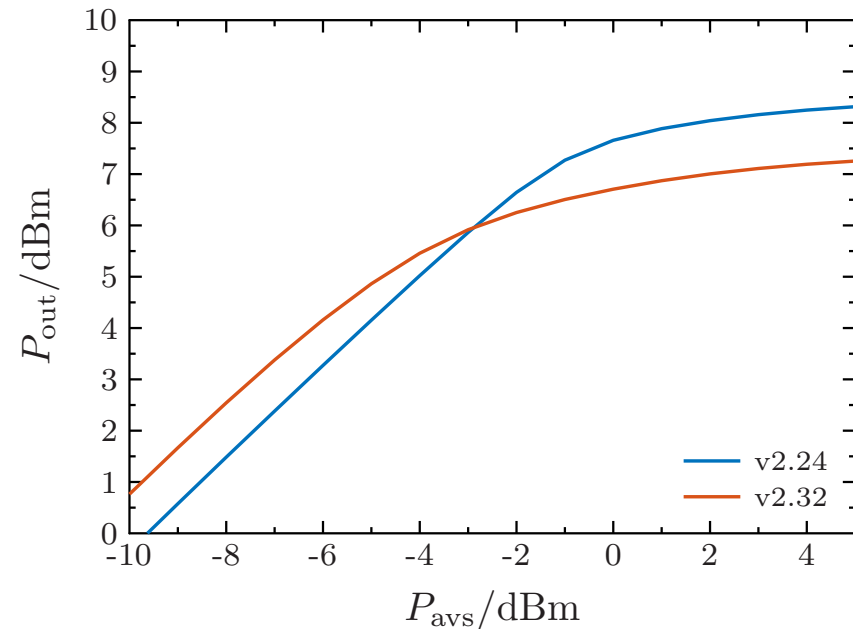
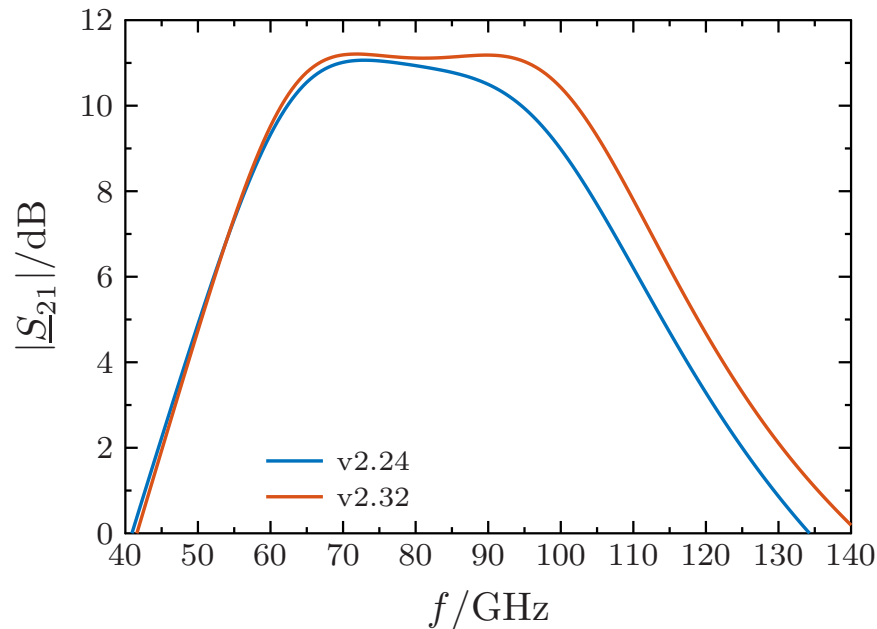
- temperature dependent weight factors => correct impact of self-heating

$$h(T) = h(T_0) \exp\left(\frac{V_{gB} - V_g}{V_T}\right)$$



HICUM/L2 Version 2.2x version 2.3x

Small-signal and large-signal results

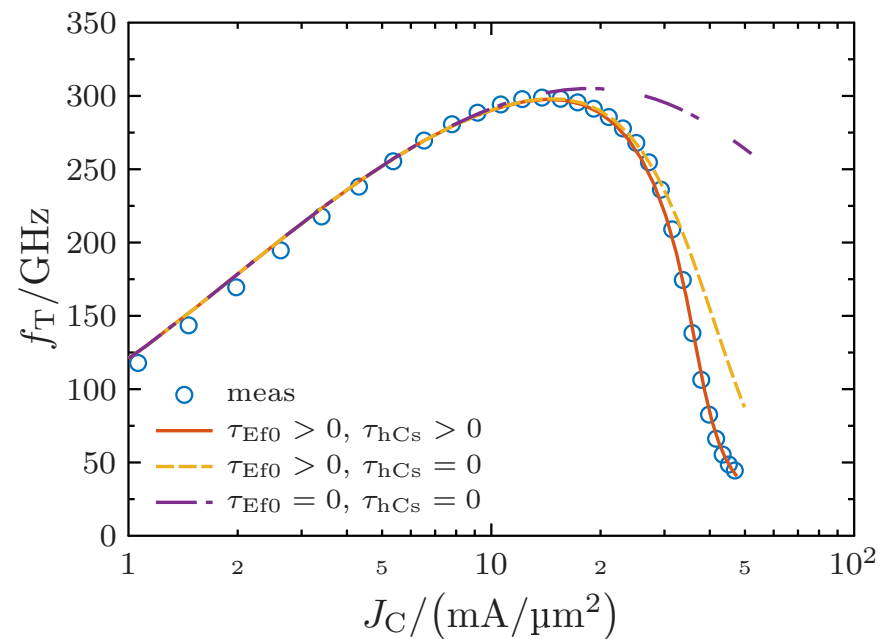
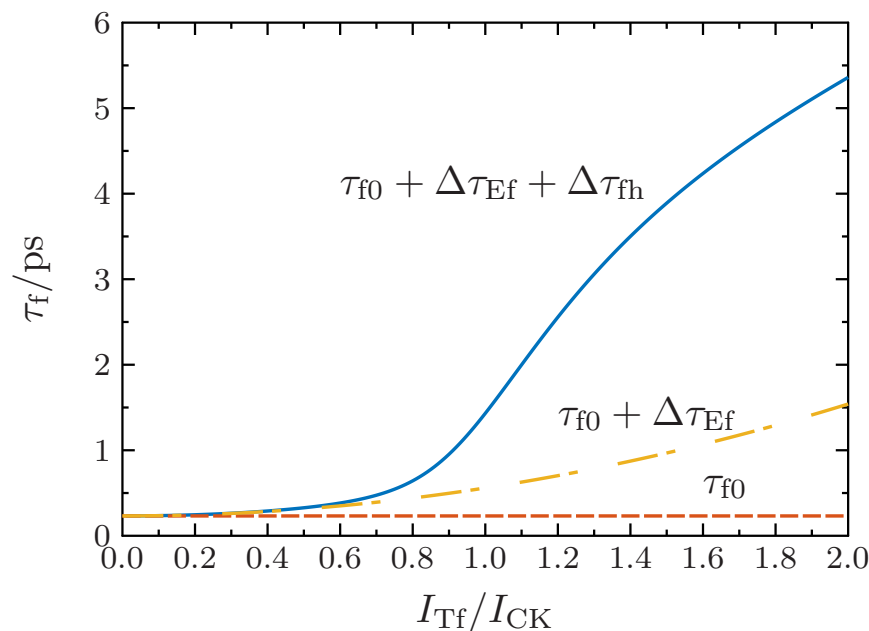


=> reduction of power at target frequency
significant differences in compression behavior

High-Current Transit Time

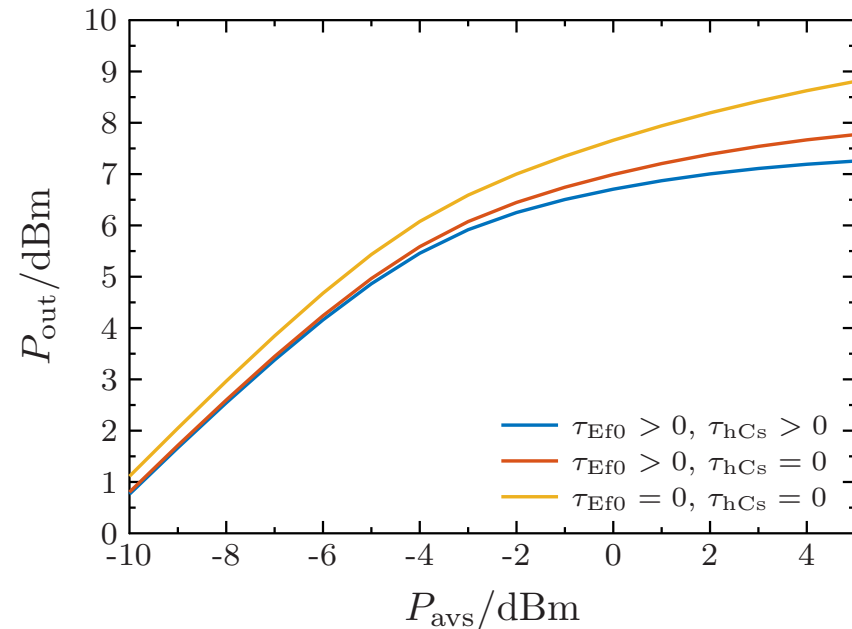
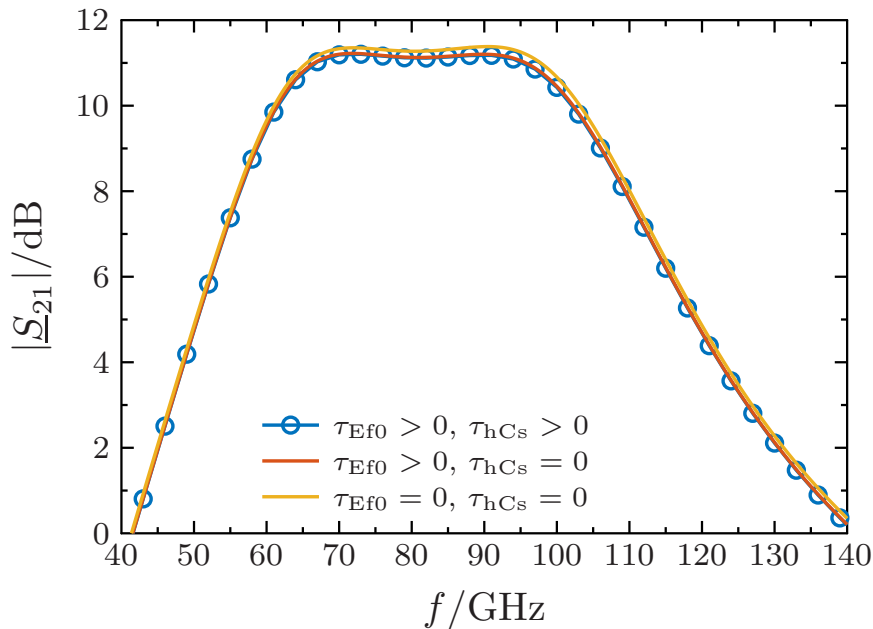
$$\tau_f = \tau_{f0} + \Delta\tau_{Ef} + \Delta\tau_{fh}$$

- τ_{f0} => medium injection
- $\Delta\tau_{Ef}$ => before onset of high current effects
- $\Delta\tau_{fh}$ => high current effects



High-Current Transit Time

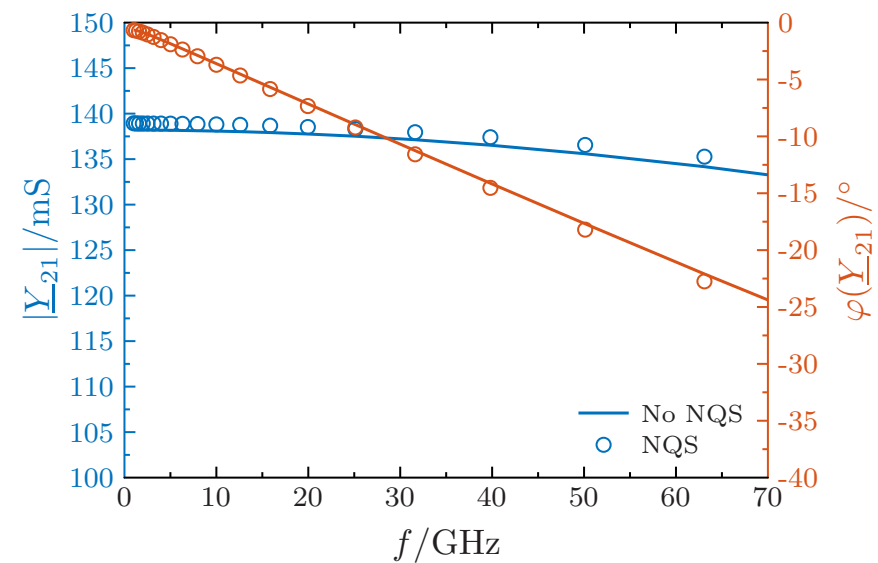
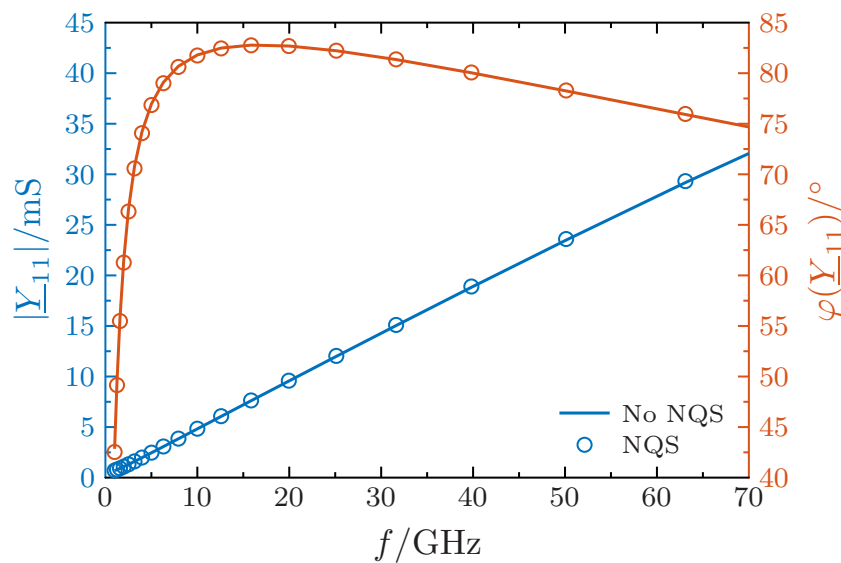
Small-signal and large-signal results



=> less influence of small signal results
(due to operating point)
different modeling of the compression

NQS Effects

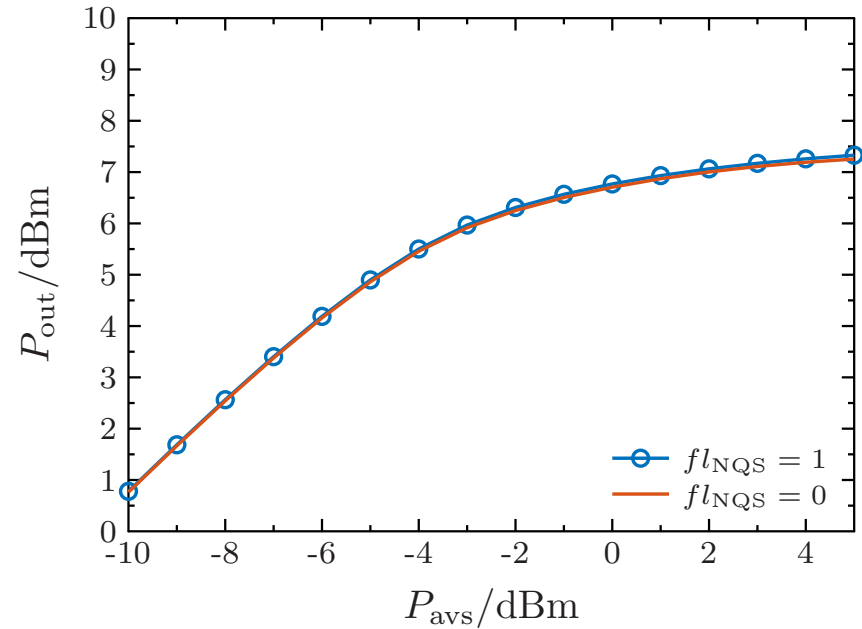
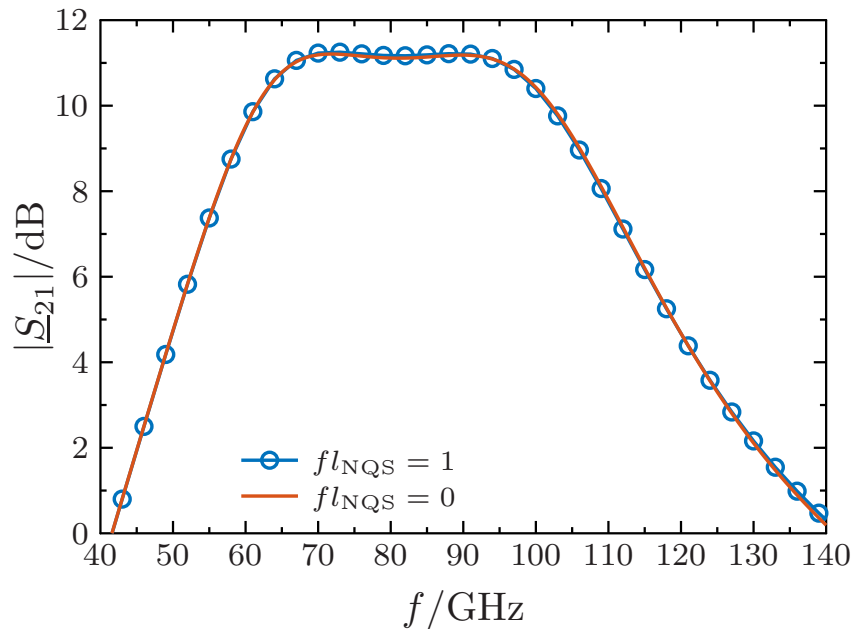
- Delay in input charge and output current
 - in HICUM: modeled by adjacent networks
 - first order delay for Q_f
 - second order delay for I_{Tf}



=> almost no impact for given transistor

NQS Effects

Small-signal and large-signal results



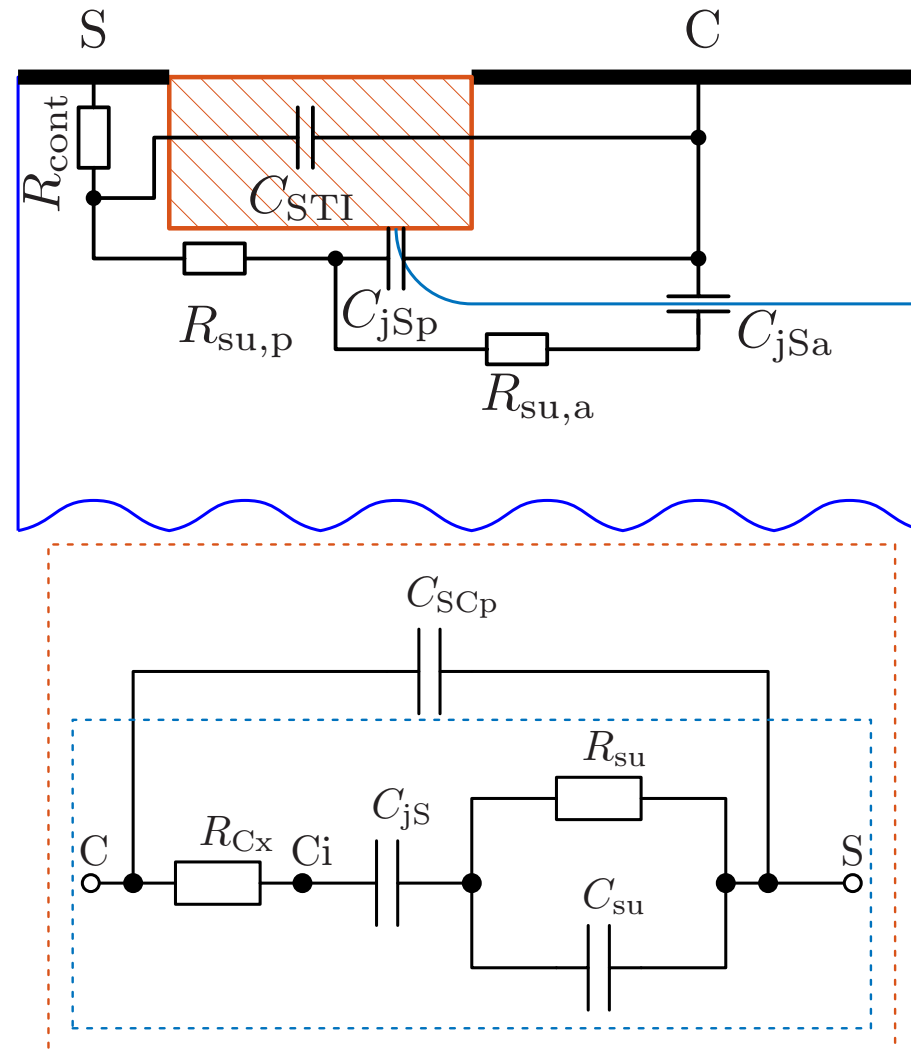
=> no visible impact

[cf. also:

C. Raya, B. Ardouin, "Model verification through benchmark circuits", 15th HICUM Workshop, Böblingen, 2015.]

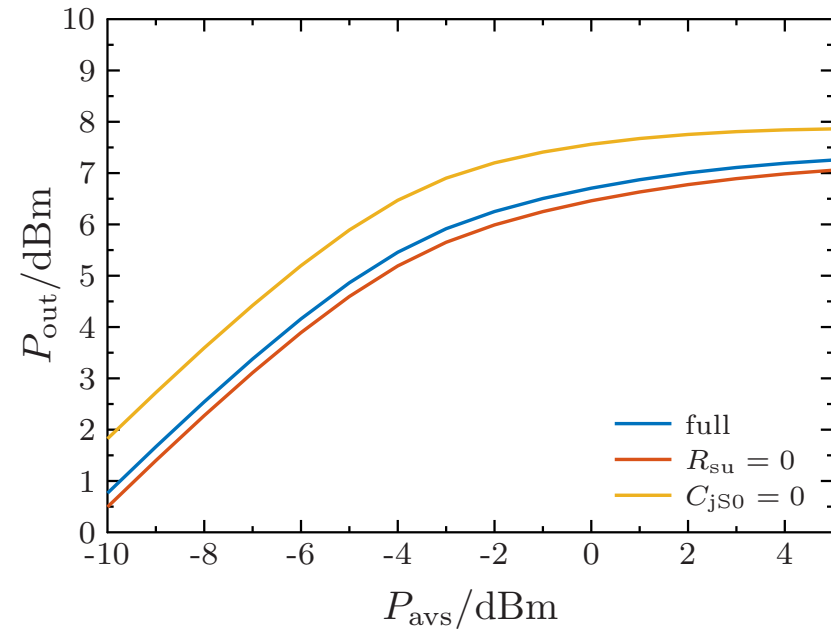
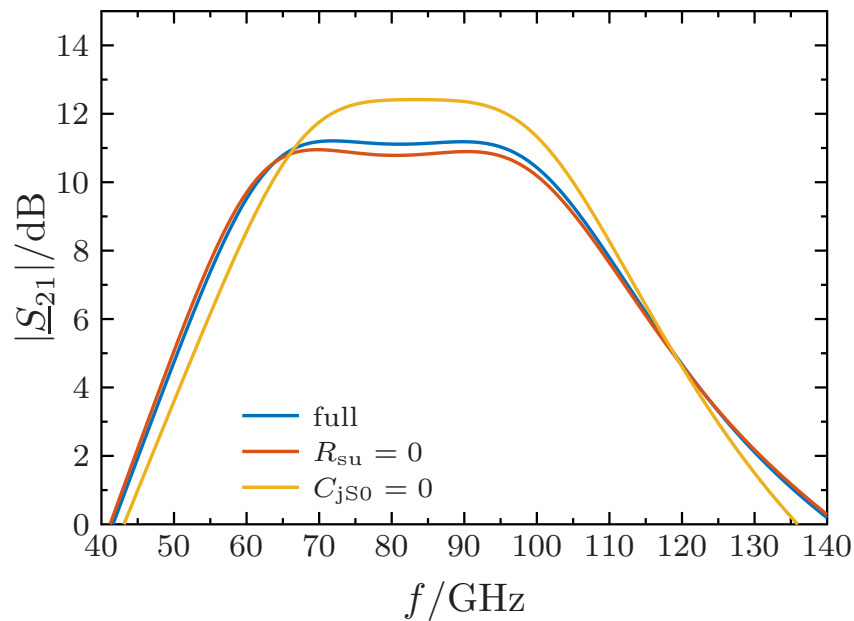
Substrate Effects

- Substrate capacitance due to pn-junction (SC) or trench oxide



Substrate Effects

Small-signal and large-signal results



=> strong influence of substrate capacitance
due to impact on output conductance

=> substrate coupling required for actual correct
value of substrate capacitance at given frequency

Summary

- Accurate nonlinear large-signal modeling capabilities of HICUM/L2
 - highlight of the important model features
 - high-current effects on charges and transfer current
 - new model version
 - substrate coupling effects
 - parameter extracted on standard DC and small-signal data sufficient for accurate large-signal modeling
- Impact on two circuits were shown
 - numerical simulations are required to overcome limitations by equipment
 - excellent agreement with respect to numerical results
 - experimental results for 2-stacked PA not yet available